

Solve this system of equations.

This would probably be easiest using Elimination.

$$\begin{aligned} 3(8x - 5y = -23) &\rightarrow 24x - 15y = -69 \\ 4(6x + 7y = 15) &\rightarrow -24x + 28y = 60 \\ \hline -43y &= -129 \\ y &= 3 \end{aligned}$$

Using one of the original equations substitute 3 for y and solve for x:

$$6x + 7y = 15 \rightarrow 6x + 7(3) = 15$$

$$6x + 21 = 15$$

$$6x = -6$$

$$x = -1$$

Sol is: (-1, 3)

When using matrices to solve a system of equations both equations must be in Standard Form.

When you solve you will always do this:

$$\begin{bmatrix} X \\ Y \end{bmatrix} = A^{-1} \cdot B$$

Turning a system of equations into a matrix equation:  $A \cdot X = B$

$$8x - 5y = -23$$

$$6x + 7y = 15$$

$$A \cdot X = B$$

Matrix A is called the Coefficient Matrix:

$$2 \times 2$$

$$\begin{bmatrix} 8 & -5 \\ 6 & 7 \end{bmatrix}$$

Matrix X is called the Variable Matrix:

$$2 \times 1$$

$$\begin{bmatrix} X \\ Y \end{bmatrix}$$

Matrix B is called the Constant (or Answer) Matrix:

$$2 \times 1$$

$$\begin{bmatrix} -23 \\ 15 \end{bmatrix}$$

Solve this by doing:

$$X = A^{-1} \cdot B = \begin{bmatrix} -1 \\ 3 \end{bmatrix}$$

as an ordered pair the answer is: (-1, 3)

Use matrices to solve this system of equations:

$$11a - 15b = -145$$

$$13b + 8a = 38 \rightarrow \text{rewrite this so that the variables on the left side are in the same order as the top equation}$$

$$11a - 15b = -145$$

$$8a + 13b = 38$$

Write this system as a matrix equation:

$$\begin{bmatrix} 11 & -15 \\ 8 & 13 \end{bmatrix} X = \begin{bmatrix} -145 \\ 38 \end{bmatrix}$$

$$A \cdot X = B$$

$$X = A^{-1} B = \begin{bmatrix} -5 \\ 6 \end{bmatrix}$$

as an ordered pair the answer is: (-5, 6)

Use matrices to solve this system of equations:

$$2.7x - 3.4y = 2.47$$

$$8.6x + 9.5y = 30.23$$

Turn this system into a matrix equation:

$$\overset{A}{\begin{bmatrix} 2.7 & -3.4 \\ 8.6 & 9.5 \end{bmatrix}} X = \overset{B}{\begin{bmatrix} 2.47 \\ 30.23 \end{bmatrix}}$$

$AX = B$

Solve this by doing:

$$X = A^{-1} \cdot B = \begin{bmatrix} 2.3 \\ 1.1 \end{bmatrix}$$

as an ordered pair the answer is: (2.3, 1.1)

Solve.  $\frac{2}{3}x - \frac{5}{6}y = 31$   
 $\frac{7}{4}x + \frac{1}{9}y = 40$

Turn this system into a matrix equation:

$$\overset{A}{\begin{bmatrix} \frac{2}{3} & -\frac{5}{6} \\ \frac{7}{4} & \frac{1}{9} \end{bmatrix}} X = \overset{B}{\begin{bmatrix} 31 \\ 40 \end{bmatrix}}$$

$AX = B$

Solve this by doing:

$$X = A^{-1} \cdot B = \begin{bmatrix} 24 \\ -18 \end{bmatrix}$$

as an ordered pair the answer is: (24, -18)

Use matrices to solve this system of equations:

$$y = 4x - 8 \rightarrow -4x + y = -8$$

$$6x + 7y = -5$$

Turn this system into a matrix equation:

$$\overset{A}{\begin{bmatrix} -4 & 1 \\ 6 & 7 \end{bmatrix}} X = \overset{B}{\begin{bmatrix} -8 \\ -5 \end{bmatrix}}$$

$AX = B$

Solve this by doing:

$$X = A^{-1} \cdot B = \begin{bmatrix} 1.5 \\ -2 \end{bmatrix}$$

as an ordered pair the answer is: (1.5, -2)

Solve this system of equations. Give answer as an ordered triple.

Turn this system into a matrix equation:

$$4x - y + 3z = -5$$

$$-3x + 5y + z = 10$$

$$6x - 7y - 8z = 1$$

$$\overset{A}{\begin{bmatrix} 4 & -1 & 3 \\ -3 & 5 & 1 \\ 6 & -7 & -8 \end{bmatrix}} X = \overset{B}{\begin{bmatrix} -5 \\ 10 \\ 1 \end{bmatrix}}$$

$3 \times 3 \quad 3 \times 1$

$$AX = B$$

Solve this by doing:

$$X = A^{-1} \cdot B = \begin{bmatrix} 1 \\ 3 \\ -2 \end{bmatrix}$$

as an ordered triple the answer is: (1, 3, -2)