

Factoring the difference of perfect cubes:

$$a^3 - b^3 = (a - b)(a^2 + ab + b^2)$$

Factoring the sum of perfect cubes:

$$a^3 + b^3 = (a + b)(a^2 - ab + b^2)$$

$$a^3 - b^3 = (a - b)(a^2 + ab + b^2)$$

These Quadratics are NEVER factorable.

Therefore, you can use the Quadratic Formula to find the two solutions from this factor.

$$a^3 + b^3 = (a + b)(a^2 - ab + b^2)$$

Factor completely.

$$250x^4 + 686x$$

$$a^3 + b^3 = (a + b)(a^2 - ab + b^2)$$

$$2x(125x^3 + 343) = 2x(5x+7)(25x^2 - 35x + 49)$$

$$a = 5x$$

$$b = 7$$

Find all complex solutions.

$$8x^3 - 125 = 0$$

$$a^3 - b^3 = (a - b)(a^2 + ab + b^2)$$

$$\begin{aligned} a^3 - b^3 \\ 8x^3 - 125 \end{aligned}$$

$$a = 2x$$

$$b = 5$$

$$(2x - 5)(4x^2 + 10x + 25)$$

$$x = \frac{5}{2}$$

$$b^2 - 4ac = -300$$

$$\frac{-10 \pm \sqrt{-300}}{8}$$

$$\frac{-10 \pm 10i\sqrt{3}}{8}$$

$$\frac{-5 \pm 5i\sqrt{3}}{4}$$

Is each a polynomial?

- Exponents must be whole numbers
- Coefficients must be real numbers

$$y = 4x^3 - 9x^2 + \frac{3}{x} - 7 \rightarrow \frac{3}{x} = 3x^{-1} \quad \text{NO} \quad \text{exponent not a whole \#}$$

$$y = 12x^5 + 13x^3 - 7\sqrt{x} + 10 \rightarrow \sqrt{x} = x^{\frac{1}{2}} \quad \text{NO} \quad \text{exponent not a whole \#}$$

$$f(x) = -3.5x^2 + \frac{2}{9}x - 18.113 \quad \text{Yes}$$

$$f(x) = -x^4 + 11x^3 + 7ix + 22 \rightarrow \text{NO} \quad \text{coefficient not a real \#}$$

Write a possible equation for this graph:

