

Factor each completely.

$$12c^2 + cd - 6d^2 = (4c + 3d)(3c - 2d)$$

Factor each completely.

$$-6a^2 + 19a - 10$$

$$-1(6a^2 - 19a + 10)$$

to make factoring easier, always try to make the leading term positive. In this problem, factor out a -1 from all terms then continue factoring.

Expand.

$$(x - 9)^2 = x^2 - 18x + 81$$

Factor.

$$m^2 + 24m + 144 = (m + 12)^2$$

since the constant is a perfect square and b is equal to the square root of the constant doubled....

Factor each.

$$1. g^2 - 12g + 36$$

since the middle term is equal to the square root of 36 then doubled this will result in:

$$(g - 6)^2$$

$$2. c^2 + 34c + 64$$

in this case the middle term isn't the square root of 64 doubled so we just factor as we always do:

if $(a+b)^2 = a^2 + 2ab + b^2$

then, $a^2 + 2ab + b^2 = (a+b)^2$

Perfect Square Trinomials

Find the value of b such that this trinomial could be factored as $(\quad)^2$. Then show its factored form.

$w^2 + bw + 100 = (w + 10)^2$ these are the same sign



The middle term should be:

Take the square root of "c" then double it.

Expand.

$(3c + 7)^2$

$9c^2 + 42c + 49$

$(3c)^2 + (2)(3)(7)c + (7)^2$

Factor.

$4k^2 - 36k + 81$

$\sqrt{4}$

(2)

$\sqrt{81}$

(9)

$2 \times 9 = 18$

Since the middle term is two of these (18)
it will factor this way:

$(2k - 9)^2$

this sign is the same
as the sign of the middle
term in the original problem

Factor.

$25g^2 + 60g + 36$

$\sqrt{25}$

5

$\sqrt{36}$

6

since $5 \times 6 = 30$ and the middle
term(b) is two of these (60)
the final answer will be

$(5g + 6)^2$

Factor. $4m^2 + 20m + 9 = (2m + 1)(2m + 9)$

$\sqrt{4} = 2$ $\sqrt{9} = 3$
 $2 \times 3 = 6$ but the "b" term isn't two of these (12)
 so I can't factor this quick way. This means we continue
 factoring the same way we factor any other trinomial.

~~$\begin{matrix} 36 \\ 2 \times 20 \end{matrix}$~~ \rightarrow $\begin{matrix} 2m & +1 \\ +9 \end{matrix}$

$4m^2$	$+2m$
$+18m$	$+9$

Find the value of b such that this trinomial could be factored as $(\quad)^2$. Then show its factored form.

$$49n^2 - bn + 36 = (7n - 6)^2$$

$\sqrt{49} = 7$ $\sqrt{36} = 6$
 $b = 2(7)(6) = 84$

Factor completely.

$$\begin{aligned}
 & \frac{1}{8} \cdot 8 \left(\frac{1}{8}x^2 + \frac{1}{4}x - 3 \right) \\
 &= \frac{1}{8} (x^2 + 2x - 24) \\
 &= \frac{1}{8} (x + 6)(x - 4)
 \end{aligned}$$

By multiplying by 8 and $\frac{1}{8}$ it's just like you've multiplied by 1. However, I chose to distribute only the 8 in order to eliminate all the denominators, making the trinomial easier to factor. Once the trinomial is factored I simply include the $\frac{1}{8}$ as one of the factors in the final answer.

Factor completely.

$$\begin{aligned}
 & \frac{1}{6} \left(\frac{1}{6}x^2 - \frac{1}{2}x - \frac{14}{3} \right) \\
 &= \frac{1}{6} (x^2 - 3x - 28) \\
 &= \frac{1}{6} (x - 7)(x + 4)
 \end{aligned}$$

Factor completely.

$$\frac{1}{3} \cdot 3 \left(\frac{2}{3}m^2 - \frac{14}{3}m - 12 \right)$$

$$= \frac{1}{3} (2m^2 - 14m - 36)$$

$$= \frac{1}{3} (2m + 4)(m - 9)$$