

Solve by completing the square.

$$x^2 + 6x + 15 = 0$$

$$-15 \quad -15$$

$$x^2 + 6x + \underline{9} = -15 + 9$$

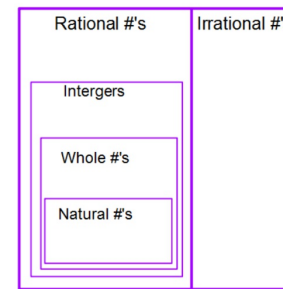
$$\sqrt{(x+3)^2} = \sqrt{-6}$$

NO Real Sol

Sec 5-6

Complex Numbers

Real Numbers



Imaginary Numbers

$$a + bi$$

Imaginary Numbers:

$$\sqrt{-1} = i$$

i is called the imaginary unit.

Simplify each.

1. $\sqrt{24}$

$$\sqrt{4 \cdot 6}$$
$$\sqrt{4} \cdot \sqrt{6}$$
$$2\sqrt{6}$$

2. $\sqrt{-24} = 2i\sqrt{6}$

$$\sqrt{-1 \cdot 4 \cdot 6}$$
$$\sqrt{-1} \cdot \sqrt{4} \cdot \sqrt{6}$$
$$i \cdot 2 \cdot \sqrt{6}$$

Simplify each.

$$1. \quad \sqrt{-98}$$

$$= \sqrt{-49 \cdot 2}$$

$$= 7i\sqrt{2}$$

$$2. \quad \sqrt{-256}$$

$$= 16i$$

$$3. \quad \sqrt{-39}$$

$$= i\sqrt{39}$$

$$4. \quad 5\sqrt{-18}$$

$$= 5\sqrt{-9 \cdot 2}$$

$$= 5 \cdot 3i\sqrt{2}$$

$$= 15i\sqrt{2}$$

The terms Complex Number and Imaginary Number are quite often used interchangeably.

Even though they are NOT the same thing!

Complex Numbers:

any number that can be written
in the form: $a + bi$ (a and b can be any real #)

Standard Form
of a Complex
Number

Real
Part

Imaginary
Part

Real Number: when $b=0$

Imaginary Number: when $b \neq 0$ (a may or may not be zero)

Examples of Imaginary #'s: $10 - 7i$ or $13i$

Write each as a Complex Number in Standard Form $a + bi$

$$1. \quad 2 + \sqrt{-9}$$

$$= 2 + 3i$$

$$2. \quad \sqrt{-12} - 5$$

$$= -5 + \sqrt{-12} \rightarrow \sqrt{4 \cdot 3}$$

$$= -5 + 2i\sqrt{3}$$

Simplify each expression:

$$1. \quad (6 - \sqrt{-64}) + (5 + \sqrt{-49})$$
$$(6 - 8i) + (5 + 7i) = 11 - i$$

$$2. \quad (-11 + \sqrt{-9}) - (6 - \sqrt{144})$$
$$(-11 + 3i) - (6 - 12)$$
$$(-11 + 3i) - (-6) = -5 + 3i$$