

$$\sin \theta + \cos \theta \cot \theta$$

$$\sin \theta + \cos \theta \cdot \frac{\cos \theta}{\sin \theta}$$

$$\frac{\sin \theta}{\sin \theta} \cdot \frac{\sin \theta}{1} + \frac{\cos^2 \theta}{\sin \theta}$$

$$\frac{\sin^2 \theta}{\sin \theta} + \frac{\cos^2 \theta}{\sin \theta} = \frac{\sin^2 \theta + \cos^2 \theta}{\sin \theta} = \frac{1}{\sin \theta} = \csc \theta$$

$$\sin^2 \theta + \cos^2 \theta = 1$$

$$\sin^2 \theta = 1 - \cos^2 \theta$$

$$\cos^2 \theta = 1 - \sin^2 \theta$$

$$\tan^2 \theta + 1 = \sec^2 \theta$$

$$1 + \cot^2 \theta = \csc^2 \theta$$

$$\frac{\sec \theta}{\sin \theta} - \frac{\sin \theta}{\cos \theta} \cdot \frac{\sin \theta}{\sin \theta}$$

$$\frac{1}{\cos \theta} \cdot \frac{1}{\sin \theta} \rightarrow \frac{1 - \sin^2 \theta}{\cos \theta \cdot \sin \theta} = \frac{\cos^2 \theta}{\cos \theta \cdot \sin \theta} = \frac{\cos \theta}{\sin \theta} = \cot \theta$$

$$\sin^2 \theta + \cos^2 \theta = 1$$

$$\sin^2 \theta = 1 - \cos^2 \theta$$

$$\cos^2 \theta = 1 - \sin^2 \theta$$

$$\tan^2 \theta + 1 = \sec^2 \theta$$

$$1 + \cot^2 \theta = \csc^2 \theta$$

$$\sec \theta \cot \theta - \cot \theta \cos \theta$$

1 +

$$\frac{\sec \theta}{\cot \theta + \tan \theta}$$

1 +

$$\sin x(1 + \cot^2 x)$$

1 +

### Verifying Trig Identities:

Showing that the two sides of the equation really are equal.

When trying to verify/prove an identity you **CAN'T** do the following:

- Move terms from one side of the equation to the other side
- Multiply/divide/square/square root both sides of the equation
- Add/Subtract from both sides of the equation

You are **NOT** solving

You are trying to show the two sides of the equation are equal, therefore, you can't do anything that requires them to be equal.

Two basic techniques:

- Work on one side only and make it look like the other side.  
or
- Work on both sides until they look the same.

Verify this trig identity.

$$\frac{\sec x - \cos x}{\tan x} = \sin x$$

$$\frac{\frac{1}{\cos} - \frac{\cos \cdot \cos}{1}}{\frac{\sin}{\cos}}$$

$$\frac{\frac{1 - \cos^2}{\cos}}{\frac{\sin}{\cos}}$$

$$\frac{\sin^2}{\sin}$$

$$\sin x = \sin x$$

Verify this identity:

$$\frac{\sin x}{\tan x} + \frac{\cos x}{\cot x} = \sin x + \cos x$$

$$\frac{\sin}{\frac{\sin}{\cos}} + \frac{\cos}{\frac{\cos}{\sin}}$$

$$\cancel{\sin} \cdot \frac{\cos}{\cancel{\sin}} + \cancel{\cos} \cdot \frac{\sin}{\cancel{\cos}}$$

$$\cos x + \sin x = \sin x + \cos x$$

Verify this identity:

$$\tan x + \cot x = \sec x \cdot \csc x$$

$$\frac{\sin}{\sin} \cdot \frac{\sin}{\cos} + \frac{\cos}{\sin} \cdot \frac{\cos}{\cos} \quad \frac{1}{\cos} \cdot \frac{1}{\sin}$$

$$\frac{\sin^2 + \cos^2}{\sin \cos}$$

$$\frac{1}{\cos \cdot \sin}$$

$$\frac{1}{\sin x \cdot \cos x} = \frac{1}{\cos x \cdot \sin x}$$

Verify this identity:

$$\sin^2 x \cdot \tan^2 x = \tan^2 x - \sin^2 x$$

$$\sin^2 \cdot \frac{\sin^2}{\cos^2}$$

$$\frac{\sin^2}{\cos^2} - \frac{\sin^2}{1} \cdot \frac{\cos^2}{\cos^2}$$

$$\frac{\sin^4}{\cos^2}$$

$$\frac{\sin^2 - \sin^2 \cos^2}{\cos^2}$$

$$\frac{\sin^2 (1 - \cos^2)}{\cos^2}$$

$$\frac{\sin^2 (\sin^2)}{\cos^2}$$

$$\frac{\sin^4 x}{\cos^2 x} = \frac{\sin^4 x}{\cos^2 x}$$

You should now be able to complete Hwk #32

Practice Sheet Sec 14-1