

Sec 9-4 Simplifying the Product or Quotient of Rational Expressions

- Factor all numerators and denominators.
- If multiplying rational expressions you can simplify within the same fraction and/or cross cancel then write as a single fraction.
- Instead of dividing, multiply by **the reciprocal** then simplify. Write answer as a single fraction.
- State restrictions on the variable.

Simplify. State the restrictions on the variables.

$$\frac{8x^4 + 2x^3}{6x^2 - 24x} \cdot \frac{(x+3)(x-2)}{4x^2 + 13x + 3}$$

$\xrightarrow{\text{Factor}} \frac{2x^3(4x+1)}{6x(x-4)} \cdot \frac{(x+3)(x-2)}{(4x+1)(x+3)}$

$= \frac{1 \cdot x^2(x-2)}{3(x-4)} \quad x \neq 0, 4, -\frac{1}{4}, -3$

Restrictions: $x \neq 0, 4, -\frac{1}{4}, -3$

Simplify. State the restrictions on the variables.

$$\frac{x^2 - 16}{9x^2 + 18x} \div \frac{x^2 - 3x - 4}{3x^2 + 6x}$$

$\xrightarrow{\text{Factor}} \frac{(x+4)(x-4)}{9x(x+2)} \times \frac{3x(x+2)}{(x-4)(x+1)} = \frac{3x(x+4)}{9x(x+1)} = \frac{(x+4)}{3(x+1)}$

$x \neq 0, -2, 4, -1$

Simplify. State restrictions on the variable.

$$\frac{x^2 + 3x - 10}{2x^2 + x - 3} \div \frac{x^3 + 5x^2 - 4x - 20}{x^2 + x - 2}$$

$\xrightarrow{\text{Factor}} \frac{(x+5)(x-2)}{(2x+3)(x-1)} \cdot \frac{(x+2)(x-1)}{(x+2)(x-2)(x+5)}$

$= \frac{x-3}{(2x+3)(x-2)} \quad x \neq -\frac{3}{2}, 1, -2, 2, -5$

Hwk #33 Sec 9-4

Pages 511-513

Problems 5, 6, 10, 11, 16, 17, 23, 27, 39

Due Thursday

Simplify.

$$LCD = 36$$

$$\frac{2}{2} \cdot \frac{7}{18} + \frac{11}{12} \cdot \frac{3}{3}$$
$$= \frac{14}{36} + \frac{33}{36} = \boxed{\frac{47}{36}}$$

Find this sum:

$$\frac{(x-4)}{x-4} \cdot \frac{5}{x+3} + \frac{2}{x-4} \cdot \frac{x+3}{x+3}$$

$$\frac{5x-20 + (2x+6)}{(x+3)(x-4)} = \boxed{\frac{7x-14}{(x+3)(x-4)}}$$

Find this sum:

$$\frac{6}{x^2-25} + \frac{7}{x^2-6x+5} \rightarrow \frac{5}{-6}$$

$$\frac{x-1}{x-1} \cdot \frac{6}{(x+5)(x-5)} + \frac{7}{(x-1)(x-5)} \cdot \frac{x+5}{x+5}$$

$$\frac{6x-6 + 7x+35}{(x-1)(x+5)(x-5)} = \boxed{\frac{13x+29}{(x-1)(x+5)(x-5)}}$$