

An object is shot into the air. The following equation gives the height of the object as a function of time since launch.

$$h(t) = -16t^2 + 144t + 65$$

- Find the maximum height of the object and the time it takes to reach that height.
- Find the time it takes the object to reach a height of 200 feet.
- Find the time it takes the object to reach a height of 50 feet.

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Vertex

Max height of 389 feet
will occur after 4.5 seconds

Los: $t = \frac{-144}{-32} = 4.5 \text{ sec}$
 $h(4.5) = 389 \text{ ft}$

$$h(t) = -16t^2 + 144t + 65$$

- Find the time it takes the object to reach a height of 200 feet.

$$\begin{aligned} 200 &= -16t^2 + 144t + 65 \\ -200 & \quad -200 \\ 0 &= -16t^2 + 144t - 135 \\ b^2 - 4ac &= 12096 \\ \frac{-144 \pm \sqrt{12096}}{-32} & \quad t = \begin{pmatrix} 1.061 \text{ sec} & 7.94 \text{ sec} \end{pmatrix} \end{aligned}$$

The object will reach a height of 200 feet twice, once on the way up to the max height and again on the way down to the ground. Therefore, both answers make sense.

$$h(t) = -16t^2 + 144t + 65$$

- Find the time it takes the object to reach a height of 50 feet.

$$\begin{aligned} 50 &= -16t^2 + 144t + 65 \\ 0 &= -16t^2 + 144t + 15 \\ b^2 - 4ac &= 21696 \\ \frac{-144 \pm \sqrt{21696}}{-32} &= -0.10 \text{ sec}, \quad \boxed{9.10 \text{ sec}} \end{aligned}$$

the object will reach a height of 50 feet only once, after 9.10 sec. A negative time doesn't make sense.

$$h(t) = -16t^2 + 144t + 65$$

d) Find the time it takes the object to reach the ground.

$$h=0$$

$$0 = -16t^2 + 144t + 65$$

$$b^2 - 4ac = 24,896$$

$$t = \frac{-144 \pm \sqrt{24896}}{-32} = -0.43 \text{ \& } 9.43$$

The object will reach the ground in 9.43 sec
(a negative time doesn't make sense and
it will reach the ground only once)

Ways to solve Quadratic Equations:

- Factoring ✓
- Square Roots ✓
- Quadratic Formula ✓
- Graphing
- Completing the Square Sec 5-7

$$(x + 6)^2 = x^2 + 12x + 36$$

$$(x - 4)^2 = x^2 - 8x + 16$$

$$(x + 11)^2 = x^2 + 22x + 121$$

$$(x - 7)^2 = x^2 - 14x + 49$$

$$(x + 8)^2 = x^2 + 16x + 64$$

$$(x - 5)^2 = x^2 - 10x + 25$$

What relationships do you see here?

$$(x + 6)^2 = x^2 + 12x + 36$$

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$$(x - 7)^2 = x^2 - 14x + 49$$

$$(x + 8)^2 = x^2 + 16x + 64$$

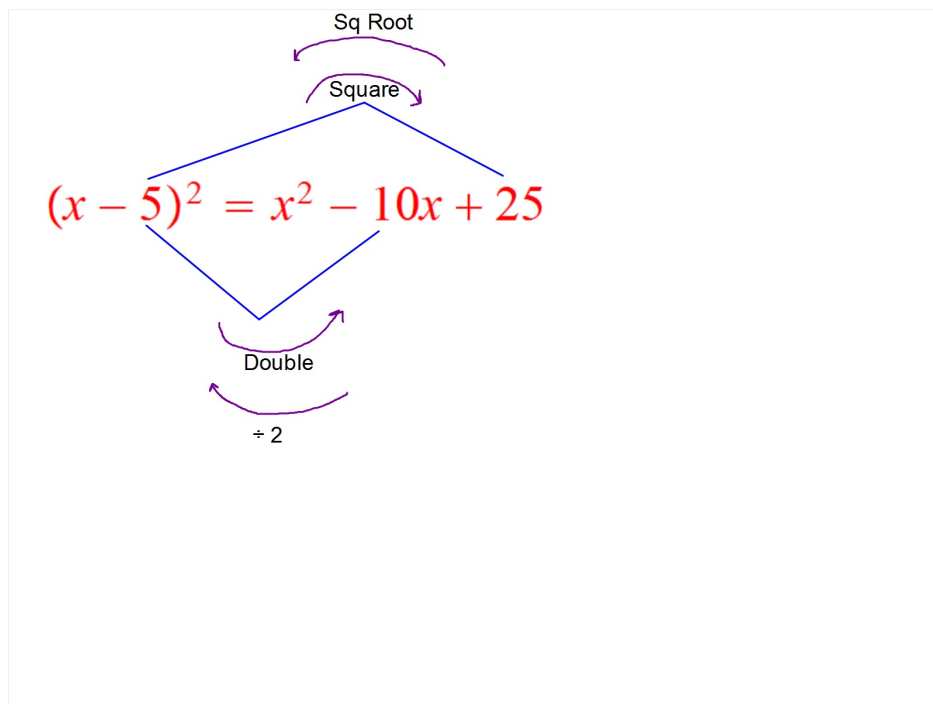
$$(x - 5)^2 = x^2 - 10x + 25$$

$$(x + h)^2 = x^2 + bx + c$$

$$b = 2h \quad b = 2 \cdot \sqrt{c}$$

$$c = h^2 \quad c = \left(\frac{b}{2}\right)^2$$

$$h = \frac{b}{2} \quad h = \sqrt{c}$$



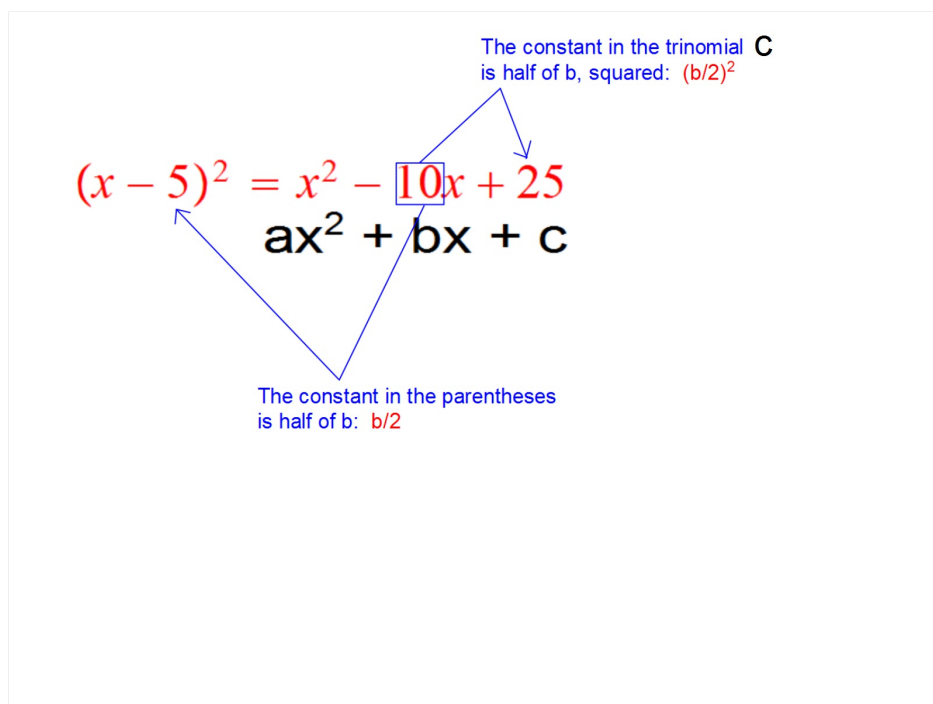
Sec 5-7: Completing the Square

Fill in the blanks.

$$1. \quad x^2 + 20x + \underline{100} = (x + \underline{10})^2$$

$$2. \quad x^2 - 4x + \underline{4} = (x - \underline{2})^2$$

This is called "Completing the Square."



In general, to complete the square:

$$x^2 + 16x + 64 = (x + 8)^2$$

$$x^2 + bx + \left(\frac{b}{2}\right)^2 = \left(x + \frac{b}{2}\right)^2$$

Arrows indicate the steps:

- 1st** (from $x^2 + bx$ to $\left(\frac{b}{2}\right)^2$)
- 2nd** (from $\left(\frac{b}{2}\right)^2$ to $\left(x + \frac{b}{2}\right)^2$)

Complete the square for each.

1. $x^2 - 12x + 36 = (x - 6)^2$

2. $x^2 + 20x + 100 = (x + 10)^2$

3. $x^2 - 2x + 1 = (x - 1)^2$