

Remember, the vertex is either the maximum or the minimum of a quadratic function.

The max/min value of a quadratic function is.....the y-coordinate of the vertex

When a max/min of a quadratic occurs is.....the x-coordinate of the vertex

A ball is shot into the air with an initial velocity of 80 ft/sec from the top of a 50 ft tall building. The following equation models the height (ft) of the object as a function of time (sec).

$$h(t) = -16t^2 + 80t + 50$$

LOS:
 $x = \frac{-80}{-32} = 2.5$
 (2.5, 150)
 The maximum is the VERTEX

- Find the time it takes the object to reach its maximum height.
2.5 sec
- Find the maximum height of the object. 150 ft

For each quadratic find the following:

- The equation of the LOS
- The coordinates of the vertex
- The y-intercept.

1. $y = -3x^2 + 12x - 5$

a. LOS: $x = 2$

b. Vertex: $(2, 7)$

c. y-int -5

2. $y = 4(x + 6)^2 - 11$

a. LOS: $x = -6$

b. Vertex: $(-6, -11)$

c. y-int 133
 $\left\{ \begin{array}{l} (0+6)^2 \\ 4(36) \\ 144-11 \end{array} \right.$ replace x with zero and simplify.

For each quadratic find the following:

- The equation of the LOS
- The coordinates of the vertex
- The y-intercept.

3. $y = 7x^2 - 8$ $b = 0$

a. LOS: $x = 0$

b. Vertex: $(0, -8)$

c. y-int -8

4. $y = -2x^2 + 8x$ $c = 0$

a. LOS: $x = \frac{-8}{-4} = 2$

b. Vertex: $(2, 8)$

c. y-int 0

In general, if the function $y = f(x)$ is transformed the following way:

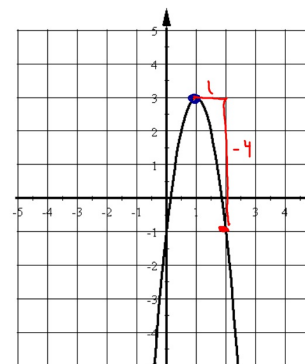
$$y = a f(x - h) + k$$

The parent function has been:

- Stretched/Shrunk vertically by a factor of a
- Reflected over x-axis if $a < 0$
- Translated horizontally h units.
- Translated vertically k units.

Write the equation of this parabola in Vertex Form.

1.



1 right, 3 up

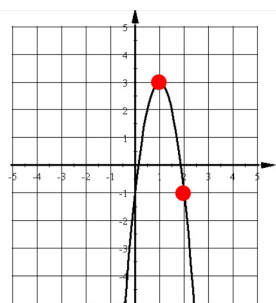
Vertex (1, 3)

$$y = a(x - 1)^2 + 3$$

$$y = -4(x - 1)^2 + 3$$

compared to the parent function

This shows that this graph is 4 times taller but upside down compared to the parent function: $a = -4$



Another way to find a :

Using the vertex of (1, 3) you can get this much of the equation:
 $y = a(x - 1)^2 + 3$

Use the coordinates of ANY other point on the graph: If you pick (2, -1)

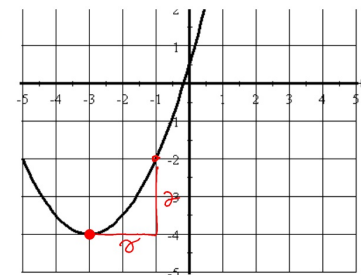
replace x with 2 and y with -1 then solve for a . $\rightarrow -1 = a(2 - 1)^2 + 3$

The eq is: $y = -4(x - 1)^2 + 3$

$$\begin{aligned} -1 &= a(1)^2 + 3 \\ -1 &= a + 3 \\ -4 &= a \end{aligned}$$

Write the equation of this parabola in Vertex Form.

2.



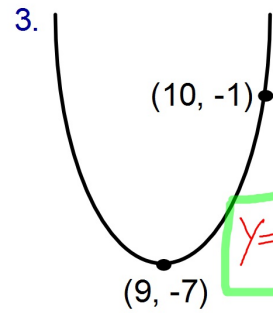
Vertex: (-3, -4)

$$y = \frac{1}{2}(x + 3)^2 - 4$$

compared to the parent function

this shows that this graph is half as tall as the parent function: $a = 1/2$

Write the equation of this parabola in Vertex Form.



$$y = 6(x - 9)^2 - 7$$

9 right 7 down

$$y = a(x - 9)^2 - 7$$

$$-1 = a(10 - 9)^2 - 7$$

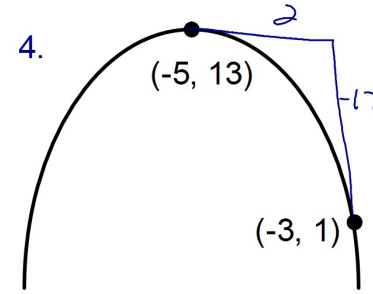
$$-1 = a(1) - 7$$

$$-1 = a - 7$$

$$+7 \quad +7$$

$$6 = a$$

Write the equation of this parabola.



$$y = -3(x + 5)^2 + 13$$

Compared to the parent function:

2 -12

This shows that this graph is three times taller and upside down: $a = -3$