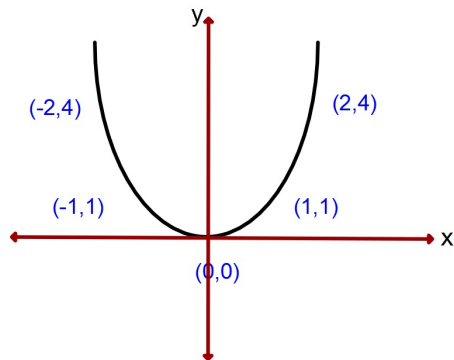
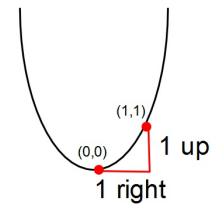


Parent Quadratic Function:

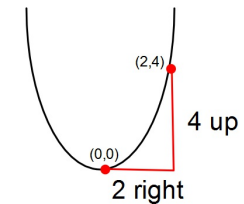
$$y = x^2$$



First "good point" of the parent function $y = x^2$



Second "good point" of the parent function $y = x^2$



You can use these points along with the vertical stretch/shrink factor from the equation to find the first two points from the Vertex then reflect them to finish finding the five points asked for.

Another way to graph a parabola:

Step 1: Find the LOS and Vertex

Step 2: Use the y-intercept and/or the Vertical Stretch or Shrink Factor to find the remaining points.

$$y = ax^2 + bx + c$$

$a > 1$ gives us a Vertical Stretch Factor
(graph is taller than the parent function)

$a < 1$ gives us a Vertical Shrink Factor
(graph is shorter than the parent function)

$a = 1$ means the graph is exactly the same height as the parent function

1. $y = -3x^2 - 6x + 3$

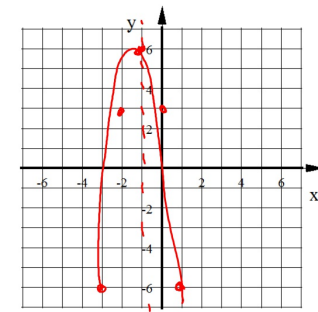
Vertex: $(-1, 6)$

1st good pt

$$\begin{array}{r} 1 \\ \hline 1 \end{array} x - 3 \rightarrow \begin{array}{r} 1 \\ \hline -3 \end{array}$$

2nd good pt

$$\begin{array}{r} 2 \\ \hline 4 \end{array} x - 3 \rightarrow \begin{array}{r} 2 \\ \hline -12 \end{array}$$



2. $y = 2x^2 - 16x + 29$

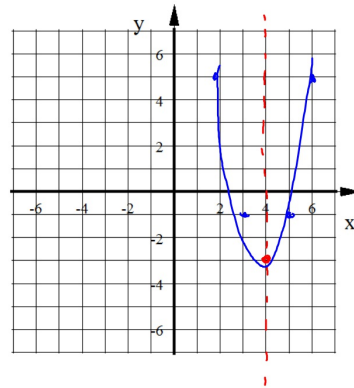
Vertex: (4, -3)

first good point:

$$\begin{array}{|c|} \hline 1 \\ \hline \end{array} \times 2 \rightarrow \begin{array}{|c|} \hline 2 \\ \hline \end{array}$$

second good point:

$$\begin{array}{|c|} \hline 2 \\ \hline \end{array} \times 2 \rightarrow \begin{array}{|c|} \hline 4 \\ \hline \end{array}$$



Graph: $y = 4x^2 - 24x + 29$

LOS $x = \frac{24}{8} = 3$

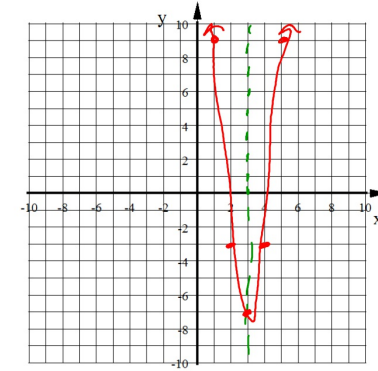
Vertex: (3, -7)

first good point:

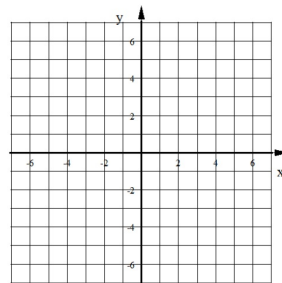
$$\begin{array}{|c|} \hline 1 \\ \hline \end{array} \times 4 \rightarrow \begin{array}{|c|} \hline 4 \\ \hline \end{array}$$

second good point:

$$\begin{array}{|c|} \hline 2 \\ \hline \end{array} \times 4 \rightarrow \begin{array}{|c|} \hline 8 \\ \hline \end{array}$$



Graph: $y = -x^2 + 4x - 2$



Remember, the vertex is either the maximum or the minimum of a quadratic function.

The max/min value of a quadratic function is....the y-coordinate of the vertex

When a max/min of a quadratic occurs is....the x-coordinate of the vertex

A company makes syringes. The following equation models their Profit as a function of the number of syringes made per hour.

$$P(s) = -0.45s^2 + 360s - 1250$$

Vertex
(400, 70750)
S P

1. Find the number of syringes that should be made per hour in order to maximize the company's Profit.

2. What is the maximum Profit?

A company needs to minimize their costs. The equation below gives their weekly costs (C) as a function of the number of hours each employee works (h).

$$C(h) = 6.5h^2 - 455h + 8760$$

Find the minimum costs the company can incur and how many hours each employee should work to reach this minimum.

Min costs = \$ 797.50

hours = 35 hrs

Vertex

(h, C)

LOS: $h = \frac{455}{2(6.5)}$
 $h = 35$

vertex:

(35, 797.5)