

Section 9-7: Probability of Multiple Events

Independent Events:

When the outcome of the first event **does NOT** affect the outcome of the second event.

$$P(\text{A and B}) = P(\text{A}) \cdot P(\text{B})$$

Dependent Events:

When the outcome of the first event **DOES** affect the outcome of the second event.

$$P(\text{A and B}) = P(\text{A}) \cdot P(\text{B after A})$$

A nationwide survey found that 72% of people in the United States like pizza. Three people are selected at random. Find each probability as a percent to the nearest tenth.

1. What is the probability that all three like pizza?

$$\underline{.72} \cdot \underline{.72} \cdot \underline{.72} = 37.3\%$$

2. What is the probability that only one of them likes pizza?

$$\underline{.72} \cdot \underline{.28} \cdot \underline{.28} = 5.6\%$$

Mrs. McKenzie needs two students to help her with a science demonstration for her class of 16 girls and 11 boys. She randomly chooses one student who comes to the front of the room. She then chooses a second student from those still seated. Find each probability as a fraction.

1. What is the probability that both students chosen are girls?

$$\frac{16}{27} \cdot \frac{15}{26} = \frac{240}{702}$$

2. What is the probability that one student is a girl and one student is a boy?

$$\frac{16}{27} \cdot \frac{11}{26} = \frac{176}{702}$$

Mutually Exclusive Events:

When two events **CAN'T** happen at the same time.

Are studying for a test and listening to music mutually exclusive events?

NO

Are reading a book and sleeping mutually exclusive?

YES

Are being 5'3" tall and being able to dunk a basketball mutually exclusive?

NO

↪ Mugsy Bogues was an NBA player at 5'3" tall and he could dunk the ball.

Is each pair of events mutually exclusive?

1. Getting an even number or a 5 when you roll a die. *Yes*
2. Getting a multiple of 3 or an even number when you roll a die. *NO*
3. Getting a prime number or an even number when rolling a die. *NO*
4. Rolling a 2 or a 3 on a die. *Yes*

Two events are **NOT** mutually exclusive if:

they **CAN** happen at the same time.

Is each pair of events mutually exclusive?

1. Driving your car and texting. *NO*
2. Driving your car and swimming. *Yes*
3. Two numbers add to 5 and have a product of zero. *NO*
4. Two numbers have an odd product and an odd sum. *Yes*

Probability of (A or B)

If A and B are **NOT** mutually exclusive:

$$P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B)$$

$$P(A \text{ and } B) = P(A) \bullet P(B)$$

(USUALLY)

If A and B **ARE** mutually exclusive:

$$P(A \text{ or } B) = P(A) + P(B)$$

6. Find each probability as a fraction.

a) The probability that it snows today = $\frac{1}{100}$ and the probability that my car doesn't start today = $\frac{2}{75}$

Find $P(\text{snows tomorrow or car doesn't start}) =$

$$\begin{aligned} & \frac{25}{75} \cdot \frac{1}{100} + \frac{2}{75} \cdot \frac{100}{100} - \frac{1}{100} \cdot \frac{2}{75} \\ & = \frac{25}{7500} + \frac{200}{7500} - \frac{2}{7500} \end{aligned}$$

$$\frac{273}{7500}$$

b) The probability that you score more than 10 points in the basketball game is $\frac{3}{8}$ and the probability that you don't score any points is $\frac{1}{6}$.

Find $P(\text{score} > 10 \text{ points or score } 0 \text{ points}) =$

$$\frac{3}{8} + \frac{1}{6} = \frac{9}{24} + \frac{4}{24} = \frac{13}{24}$$

The probability that a hitter strikes out is 12% and the probability that they get a hit is 30%. Find the probability that, in their next at bat, the hitter strikes out or gets a hit.

$$P(\text{strike out or get a hit}) = 12\% + 30\% = 42\%$$