

1. Simplify. Use Absolute Value symbols as needed.

$$\sqrt[4]{18a^3b^7c^{13}} \cdot \sqrt[4]{9a^6b^{19}c^7}$$

2. Rationalize the denominator.

a) $\frac{48w^2y^7}{\sqrt[6]{4w^9x^6y^{13}}}$

b) $\frac{\sqrt{10} + 4}{\sqrt{5} - \sqrt{2}}$

3. Simplify. Assume all variables are positive. Give fractional answers in reduced form.

$$\left(\frac{16m^4}{n^{\frac{4}{3}}} \right)^{\frac{-3}{2}}$$

4. solve each radical equation.

a) $(5x + 16)^{\frac{1}{4}} = (x + 2)^{\frac{1}{2}}$

b) $\sqrt{12 - x} + 6 = x$

c) $(2x + 1)^{\frac{3}{5}} + 4 = 31$

1. Simplify. Use Absolute Value symbols as needed.

$$\sqrt[4]{18a^3b^7c^{13}} \cdot \sqrt[4]{9a^6b^{19}c^7} = \sqrt[4]{3^4 \cdot 2a^9b^{26}c^{20}} = 3a^2b^6c^5 \sqrt[4]{2ab^2}$$

2. Rationalize the denominator.

$$a) \frac{48w^2y^7}{\sqrt[6]{4w^9x^6y^{13}}} \cdot \frac{\sqrt[6]{2^4w^3y^5}}{\sqrt[6]{2^4w^3y^5}}$$

$$= \frac{48w^2y^7 \sqrt[6]{2^4w^3y^5}}{\sqrt[6]{2^6w^{12}x^6y^{18}}} = \frac{48w^2y^7 \sqrt[6]{2^4w^3y^5}}{2w^2xy^3} = \frac{24y^4 \sqrt[6]{2^4w^3y^5}}{x}$$

$$b) \frac{\sqrt{10}+4}{\sqrt{5}-\sqrt{2}} \cdot \frac{\sqrt{5}+\sqrt{2}}{\sqrt{5}+\sqrt{2}} = \frac{9\sqrt{2}+6\sqrt{5}}{3}$$

$$\begin{array}{|c|c|} \hline \sqrt{50} = 5\sqrt{2} & \sqrt{20} = 2\sqrt{5} \\ \hline +4 & 4\sqrt{5} & 4\sqrt{2} \\ \hline \end{array}$$

$$= 3\sqrt{2} + 2\sqrt{5}$$

3. Simplify. Assume all variables are positive. Give fractional answers in reduced form.

$$\left(\frac{16m^4}{n^{\frac{4}{3}}}\right)^{\frac{3}{2}} = \left(\frac{n^{\frac{4}{3}}}{16m^4}\right)^{\frac{3}{2}} = \frac{n^{\frac{4}{3} \cdot \frac{3}{2}}}{16^{\frac{3}{2}} m^{4 \cdot \frac{3}{2}}} = \frac{n^2}{64 m^6}$$

4. solve each radical equation.

$$a) ((5x+16)^{\frac{1}{4}})^4 = ((x+2)^{\frac{1}{2}})^4$$

$$5x+16 = (x+2)^2$$

$$5x+16 = x^2+4x+4$$

$$0 = x^2 - x - 12$$

$$0 = (x-4)(x+3)$$

$$x = 4, -3$$

$$x = 4$$

$$b) \sqrt{12-x} + 6 = x$$

$$(\sqrt{12-x})^2 = (x-6)^2$$

$$12-x = x^2-12x+36$$

$$0 = x^2 - 11x + 24$$

$$0 = (x-3)(x-8)$$

$$x = 3, 8$$

$$x = 8$$

$$c) (2x+1)^{\frac{3}{5}} + 4 = 31$$

$$((2x+1)^{\frac{3}{5}})^{\frac{5}{3}} = (27)^{\frac{5}{3}}$$

$$2x+1 = 27$$

$$2x = 26$$

$$x = 13$$