

Solve.

Solution is: 38

5. $5(x-2)^{\frac{1}{2}} + 1 = 31$

OR

$$\frac{5(x-2)^{1/2} = 30}{5}$$

$$(x-2)^{1/2} = 6$$

$$(\sqrt{x-2})^2 = (6)^2$$
$$x-2 = 36$$

$$x = 38$$

$$((x-2)^{1/2})^2 = (6)^2$$

$$(x-2)^1 = 36$$

$$x = 38$$

Solve. $5 + (2x-3)^{\frac{1}{4}} = 13$

$$\begin{matrix} -5 & -5 \end{matrix}$$

$$(2x-3)^{1/4} = 8$$

$$((2x-3)^{1/4})^4 = (8)^4$$

$$(\sqrt[4]{2x-3})^4 = (8)^4 \quad \text{OR}$$

$$(2x-3)^1 = 4096$$

$$\begin{matrix} 2x-3 = 4096 \\ +3 \quad +3 \end{matrix}$$

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$$\frac{2x}{2} = \frac{4099}{2}$$

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$$x = 2049.5$$

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Solve.

Solution is: 41

6. $(2x-1)^{\frac{3}{4}} - 10 = 17$

$$\begin{matrix} +10 & +10 \end{matrix}$$

$$(2x-1)^{3/4} = 27$$

$$(\sqrt[4]{(2x-1)^3})^4 = (27)^4$$
$$\sqrt[3]{(2x-1)^3} = \sqrt[3]{531441}$$

$$\begin{matrix} 2x-1 = 81 \\ +1 \quad +1 \end{matrix}$$
$$\begin{matrix} 2x = 82 \\ \frac{2x}{2} = \frac{82}{2} \\ x = 41 \end{matrix}$$

Solve:

$(x+7)^{\frac{2}{3}} + 5 = 14$

$$\begin{matrix} -5 & -5 \end{matrix}$$

$$\left((x+7)^{2/3} \right)^{3/2} = (9)^{3/2}$$

$$\begin{matrix} x+7 \\ -2 \quad -2 \end{matrix} = 27$$

$$x = 20$$

Solve.

Solution is: -2, 3

$$7. \left(\sqrt[3]{x^2-7}\right)^3 = \left(\sqrt[3]{x-1}\right)^3$$

$$x^2 - 7 = x - 1$$

$$\begin{aligned} x^2 - x - 6 &= 0 & x &= 3, -2 \\ (x-3)(x+2) &= 0 \end{aligned}$$

Solve.

Solution is: 5

$$8. \left((4x-1)^{\frac{1}{2}}\right)^2 = \left((2x+9)^{\frac{1}{2}}\right)^2$$

$$4x-1 = 2x+9$$

$$2x = 10$$

$$x = 5$$

Solve.

Solution is: 3

$$9. (x+13)^{\frac{1}{4}} - (x+1)^{\frac{1}{2}} = 0$$

$$\left[(x+13)^{\frac{1}{4}}\right]^4 = \left[(x+1)^{\frac{1}{2}}\right]^4$$

$$\begin{aligned} x+13 &= (x+1)^2 & x &= (x+4)(x-3) \\ x+13 &= x^2+2x+1 & x &= 3, -4 \\ \cancel{4} & & & \end{aligned}$$