

Rationalize each denominator. Simplify, assume all variables are positive.

1. $\frac{8a}{\sqrt{12a^3b^5}}$

2. $\frac{15c^3d}{\sqrt[3]{3c^7d^5e}}$

3. $\frac{7}{\sqrt[4]{7g^2h^9k^{23}}}$

4. $\frac{8P^3Q\sqrt[3]{3PQ^2}}{\sqrt[5]{4P^{11}Q^{32}R^8}}$

ANSWERS

Rationalize each denominator. Simplify, assume all variables are positive.

$$\begin{aligned} 1. \frac{8a}{\sqrt{12a^3b^5}} & \cdot \frac{\sqrt{3ab}}{\sqrt{3ab}} \\ &= \frac{8a\sqrt{3ab}}{\sqrt{36a^4b^6}} = \frac{8a\sqrt{3ab}}{6a^2b^3} \\ &= \boxed{\frac{4\sqrt{3ab}}{3ab^3}} \end{aligned}$$

$$\begin{aligned} 3. \frac{7}{\sqrt[4]{7g^2h^9k^{23}}} & \cdot \frac{\sqrt[4]{7^3g^2h^3k}}{\sqrt[4]{7^3g^2h^3k}} \\ &= \frac{7\sqrt[4]{7^3g^2h^3k}}{\sqrt[4]{7^4g^4h^{12}k^{24}}} = \frac{7\sqrt[4]{7^3g^2h^3k}}{7gh^3k^6} \\ &= \boxed{\frac{\sqrt[4]{7^3g^2h^3k}}{gh^3k^6}} \end{aligned}$$

$$\begin{aligned} 2. \frac{15c^3d}{\sqrt[3]{3c^7d^5e}} & \cdot \frac{\sqrt[3]{3^2c^2de^2}}{\sqrt[3]{3^2c^2de^2}} \\ &= \frac{15c^3d\sqrt[3]{3^2c^2de^2}}{\sqrt[3]{3^3c^9d^6e^3}} \\ &= \frac{15c^3d\sqrt[3]{3^2c^2de^2}}{3c^3d^2e} = \boxed{\frac{5\sqrt[3]{9c^2de}}{de}} \end{aligned}$$

$$\begin{aligned} 4. \frac{8P^3Q\sqrt[3]{3PQ^2}}{\sqrt[5]{4P^{11}Q^{32}R^8}} & \cdot \frac{\sqrt[5]{4^4P^4Q^3R^2}}{\sqrt[5]{4^4P^4Q^3R^2}} \\ &= \frac{8P^3Q\sqrt[5]{3 \cdot 4^4P^5Q^5R^2}}{\sqrt[5]{4^5P^{15}Q^{35}R^{10}}} \\ &= \frac{8P^4Q^2\sqrt[5]{3 \cdot 4^4R^2}}{4P^3Q^7R^2} = \boxed{\frac{2P\sqrt[5]{3 \cdot 4^4R^2}}{Q^5R^2}} \end{aligned}$$