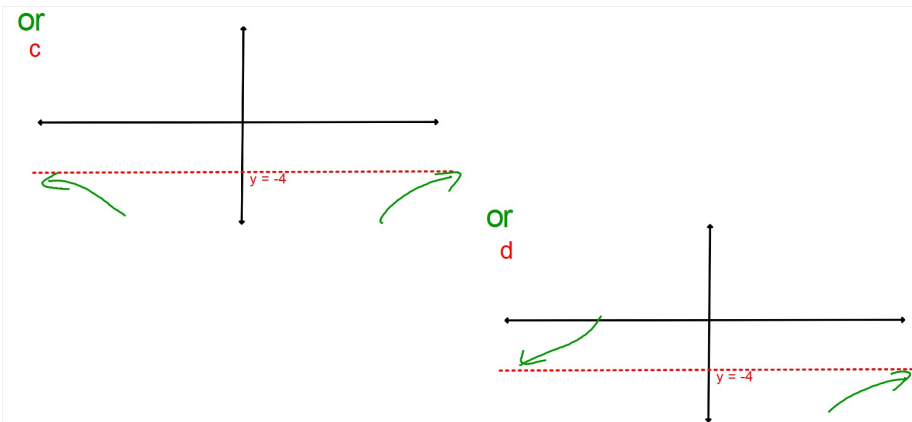
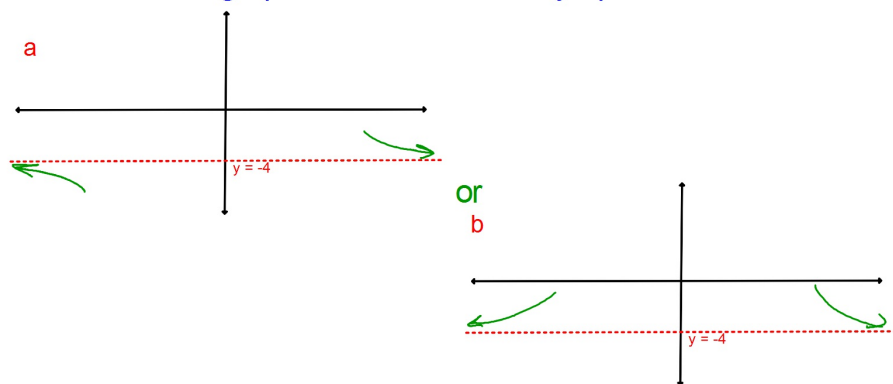
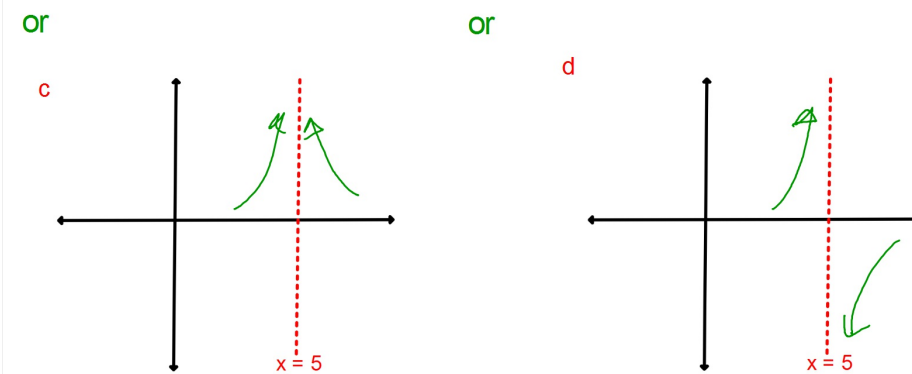
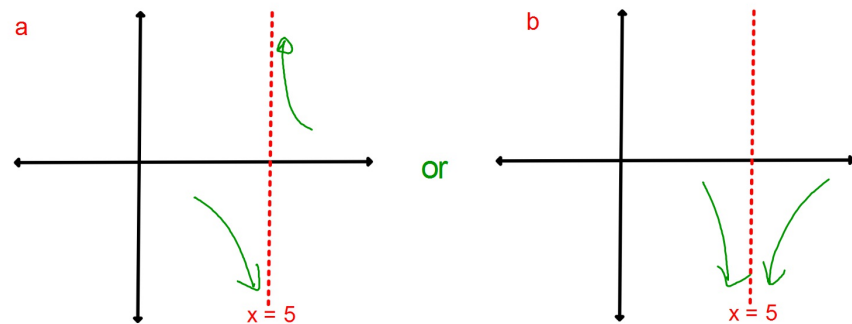


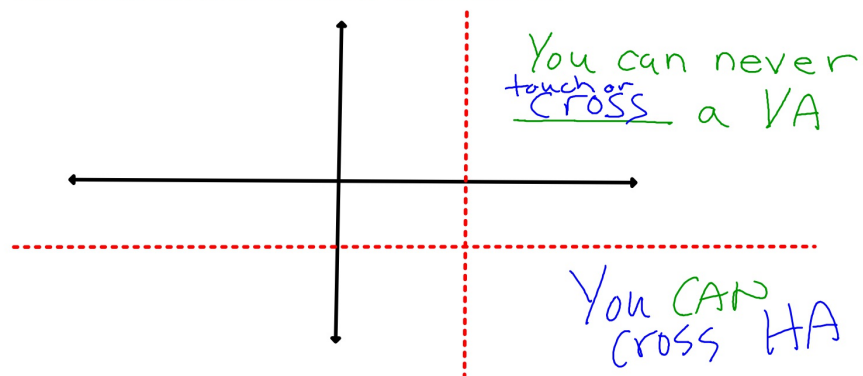
# End behavior of graph with Horizontal Asymptotes:



# Behavior of graph around a Vertical Asymptote:

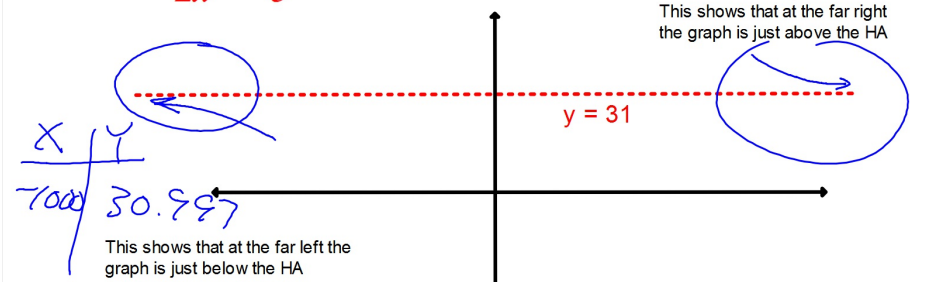


What is the difference between a HA and a VA?

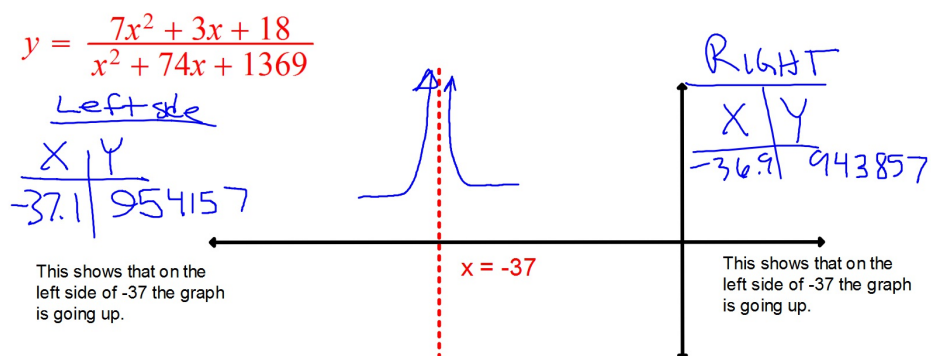


Use the Table function to sketch the End Behavior of this function whose HA is  $y = 31$

$$y = \frac{62x^2 + 6x - 1}{2x^2 - 5}$$



Use the Table function to sketch the behavior of the graph on the left and right side of the VA  $x = -37$



What are the vertical asymptotes?

$$y = \frac{x(2x + 1)}{(x - 1)(x + 4)}$$

VA:  $x = 1$

VA:  $x = -4$

what does the graph do on the left and right of each VA?

| x          | y          | x          | y          |
|------------|------------|------------|------------|
| Left Side  | -5.143 NEG | Left Side  | 561.88 POS |
| Right Side | 60.882 POS | Right Side | -54.12 NEG |

Handwritten notes for VA: x = 1:  
Left Side: down  
Right Side: up

Handwritten notes for VA: x = -4:  
Left Side: up  
Right Side: down

VA:  $x=1$

On the left side the graph

decreases w/o bound

On the right side the graph

increases w/o bound

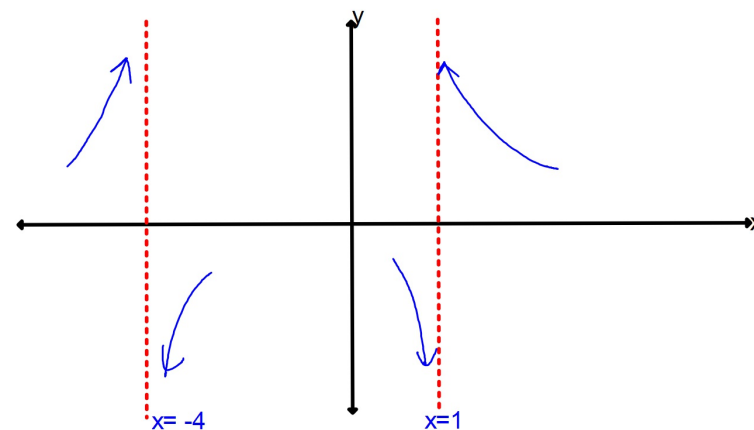
VA:  $x=-4$

On the left side the graph

increases w/o bound

On the right side the graph

decreases w/o bound



### Sign Analysis

$$y = \frac{x(2x+1)}{(x-1)(x+4)}$$

VA:  $x=1$

VA:  $x=-4$

Replace each  $x$  with a number and write down if each factor is POS or NEG. Use this to decide if the entire function is POS or NEG. A POS result means the graph goes UP and a NEG result means the graph goes DOWN.

| x                 | y                               | x                  | y                               |
|-------------------|---------------------------------|--------------------|---------------------------------|
| Left Side<br>0.9  | $\frac{+}{-} = \ominus$<br>down | Left Side<br>-4.1  | $\frac{+}{-} = \oplus$          |
| Right Side<br>1.1 | $\frac{+}{+} = \oplus$<br>up    | Right Side<br>-3.9 | $\frac{-}{+} = \ominus$<br>down |

$$y = \frac{x(2x+1)}{(x-1)(x+4)} = \frac{2x^2+x}{x^2+3x-4}$$

What is the HA?  $y=2$

How does the graph behave at the Right End?

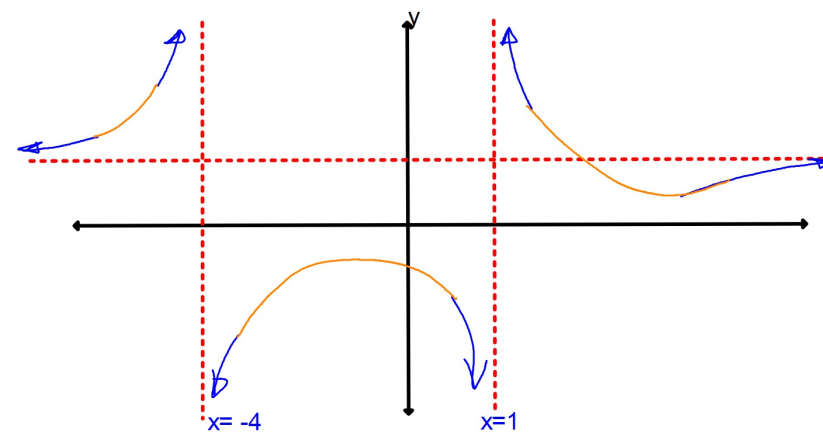
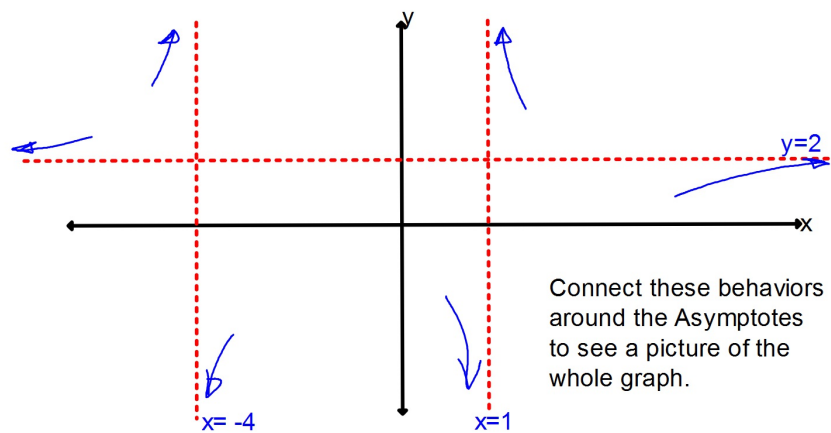
| x    | y     |
|------|-------|
| 1000 | 1.995 |

Less than 2 means the graph is below the HA at the far right.

How does the graph behave at the Left End?

| x     | y     |
|-------|-------|
| -1000 | 2.005 |

Greater than 2 means the graph is above the HA at the far left.



$$y = \frac{x(2x + 1)}{(x - 1)(x + 4)} = \frac{2x^2 + x}{x^2 + 3x - 4}$$

This is the actual graph of this Rational Function

