

### Sec 9-1: Inverse Variation

Inverse Variation: When two quantities have a **constant product**

1. Three equations for Inverse Variation are:

$$\underline{y = \frac{k}{x}}, \quad \underline{k = xy}, \quad \text{and} \quad \underline{x = \frac{k}{y}}$$

2. What does the letter **k** represent?

**The variation constant.**

3. For Direct Variation, as one quantity increases the other quantity also increases.

For Inverse Variation, as one quantity

increases the other quantity decrease

How do you tell if a table of values produces and inverse variation relationship?

See if  $xy$  is a constant product.

a) Inverse Variation? Yes

| X   | Y  | $xy$ |
|-----|----|------|
| -12 | -4 | 48   |
| -6  | -8 | 48   |
| 0.5 | 96 | 48   |
| 16  | 3  | 48   |

If Yes,  $k = 48$

If Yes, equation is:  $xy = 48$  or  $x = \frac{48}{y}$  or  $y = \frac{48}{x}$

b) Inverse Variation? NO

| X  | Y  | $xy$ |
|----|----|------|
| -2 | -8 | 16   |
| 3  | 12 | 36   |
| 5  | 20 |      |
| 9  | 36 |      |

If Yes,  $k =$  \_\_\_\_\_

If Yes, equation is:

c) Inverse Variation? NO

| X | Y  | $xy$ |
|---|----|------|
| 5 | 12 | 60   |
| 6 | 14 | 84   |
| 7 | 16 |      |
| 8 | 18 |      |

If Yes,  $k =$  \_\_\_\_\_

If Yes, equation is:

| X  | Y   |
|----|-----|
| -4 | -36 |
| 16 | 9   |
| 24 | 6   |
| 36 | 4   |

1. Does this table show inverse variation? Yes

2. Find the variation constant.  $K = 144$

3. Write an inverse variation equation.

$$xy = 144$$

4. Find the value of x when y is 80

$$x \cdot 80 = 144 \Rightarrow x = 1.8$$

Suppose that x and y vary inversely. Write a function to model this inverse variation:

x = 30 when y = 9

$$xy = 270$$

This ordered pair is from an inverse variation relationship. Find the variation constant.

(5, 8)

$$K = 40$$

Eq

$$xy = 40$$

For a given amount of Force, mass is inversely proportional to acceleration. You accelerated an 8 pound weight 12 ft/sec<sup>2</sup>. ~~X~~

1. Write an inverse variation equation.

$$K = 96$$

$$xy = 96$$

2. Find the acceleration needed to produce the same force on a 15 pound weight.

$$\frac{8 \cdot 12}{15} = \frac{96}{15}$$

$$x = 6.4 \text{ ft/sec}^2$$

**Combined Variation:** When one variable is related to two or more variables.

**Joint Variation:**

A kind of Combined Variation when a variable varies **directly** with two or more variables.

**Examples of Combined Variations**

| Combined Variation  | Equation Form       |
|---|---------------------|
| z varies jointly with x and y.                              | $z = kxy$           |
| z varies jointly with x and y and inversely with w.         | $z = \frac{kxy}{w}$ |
| z varies directly with x and inversely with the product wy. | $z = \frac{kx}{wy}$ |

W varies directly with M and inversely with Q.  
W = 1 when M = 12 and Q = 18.

1. Write a variation equation.

$$W = k \frac{M}{Q} \quad 1 = k \cdot \frac{12}{18} \rightarrow k = 1.5$$

2. Find W when M = 20 and Q = 48.

$$W = \frac{1.5(20)}{48}$$

$$W = 0.625$$

Model each statement with a variation equation:

1. G varies jointly with M and the square of P and inversely with R.

$$G = \frac{kMP^2}{R} \text{ or } k \frac{MP^2}{R}$$

2. W varies directly with the cube of C and inversely with the product of A and the fourth power of B.

$$W = \frac{C^3 k}{AB^4}$$

