

Algebra 2 Bellwork Thursday, December 4, 2014

Find all EXACT solutions, real and imaginary, of each polynomial equation.

1. $7x^3 - 2x^2 + 21x - 6 = 0$

2. $x^3 - 3x^2 - 13x + 15 = 0$

3. $1296x^4 - 625 = 0$

Use the following formulas to factor each.

Difference of Perfect Cubes: $a^3 - b^3 = (a - b)(a^2 + ab + b^2)$

Sum of Perfect Cubes: $a^3 + b^3 = (a + b)(a^2 - ab + b^2)$

4. $w^3 - 125$

5. $g^3 + 64$

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Answers

Find all EXACT solutions, real and imaginary, of each polynomial equation.

1. $7x^3 - 2x^2 + 21x - 6 = 0$

Handwritten solution for problem 1:

x^2	$7x^3$	$-2x^2$
$+3$	$+21x$	-6

$(7x-2)(x^2+3)=0$
 $x = \frac{2}{7}, \pm i\sqrt{3}$

$x^2 + 3 = 0$
 $\sqrt{x^2} = \sqrt{-3}$
 $x = \pm i\sqrt{3}$

2. $x^3 - 3x^2 - 13x + 15 = 0$

Handwritten solution for problem 2:

x^2	x^3	$-3x^2$
-13	$-13x$	$+15$

$x = -3, 1, 5$
 CAN'T FACTOR THIS WAY, USE A GRAPH -
 THESE DON'T MULTIPLY TO +15!

3. $1296x^4 - 625 = 0$

Handwritten solution for problem 3:

$(36x^2 + 25)(36x^2 - 25)$
 $(36x^2 + 25)(6x + 5)(6x - 5)$
 $\rightarrow 36x^2 + 25 = 0 \rightarrow \sqrt{x^2} = \sqrt{-25/36}$
 $x = \pm 5/6, \pm i 5/6$

Use the following formulas to factor each.

Difference of Perfect Cubes: $a^3 - b^3 = (a - b)(a^2 + ab + b^2)$

Sum of Perfect Cubes: $a^3 + b^3 = (a + b)(a^2 - ab + b^2)$

4. $w^3 - 125$

$w^3 - (5)^3 \rightarrow a = w$
 $b = 5$

$(w - 5)(w^2 + 5w + 25)$

5. $g^3 + 64$

$g^3 + (4)^3 \rightarrow a = g$
 $b = 4$

$(g + 4)(g^2 - 4g + 16)$