

Square the constant
to the constant in the trinomial

$$(x - 5)^2 = x^2 - 10x + 25$$

Double the constant
to get the linear term

Sec 5-7: Completing the Square

Fill in the blanks.

$$1. \quad x^2 + 20x + \underline{100} = (x + \underline{10})^2$$

$$2. \quad x^2 - 4x + \underline{4} = (x - \underline{2})^2$$

This is called "completing the square"

The constant in the trinomial
is half of b, squared: $(b/2)^2$

$$(x - 5)^2 = x^2 - \boxed{10}x + 25$$

The constant in the parentheses
is half of b: $b/2$

In general, to complete the square:

$$x^2 + 16x + 64 = (x + 8)^2$$

$$x^2 + bx + \left(\frac{b}{2}\right)^2 = \left(x + \frac{b}{2}\right)^2$$

Complete the square for each.

$$1. x^2 - 12x = (x \quad)^2 \longrightarrow 1. x^2 - 12x + 36 = (x - 6)^2$$

$$2. x^2 + 20x = (x \quad)^2 \longrightarrow 2. x^2 + 20x + 100 = (x + 10)^2$$

$$3. x^2 - 2x = (x \quad)^2 \longrightarrow 3. x^2 - 2x + 1 = (x - 1)^2$$

Solve by completing the square.

$$x^2 + 22x = 5$$

$$x^2 + 22x + 121 = 5 + 121$$

$$\sqrt{(x + 11)^2} = \sqrt{126}$$

$$x + 11 = \pm \sqrt{126} = \pm \sqrt{9 \cdot 14}$$

$$x + 11 = \pm 3\sqrt{14}$$

$$x = -11 \pm 3\sqrt{14}$$

$$x^2 - 14x + 11 = 0$$

Rewrite into: $ax^2 + bx = c$ Form

$$x^2 - 14x = -11$$

$$x^2 - 14x + 49 = -11 + 49$$

$$\sqrt{(x - 7)^2} = \sqrt{38}$$

$$x - 7 = \pm \sqrt{38}$$

$$x = 7 \pm \sqrt{38}$$

Solve $x^2 + 6x - 19 = 0$

$$x^2 + 6x = 19$$

add $(b/2)^2$ to both sides

$$x^2 + 6x + 9 = 19 + 9$$

$$\sqrt{(x + 3)^2} = \sqrt{28}$$

$$x + 3 = \pm 2\sqrt{7}$$

$$x = -3 \pm 2\sqrt{7}$$

Solve by completing the square:

$$x^2 - 10x + 36 = 0$$

$$x^2 - 10x + 25 = -36 + 25$$

$$\sqrt{(x - 5)^2} = \sqrt{-11}$$

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Why can't you solve this equation by completing the square, the way it's written.

$$\frac{5x^2}{5} - \frac{8x}{5} + \frac{3}{5} = 0$$

$$ax^2 + bx + c$$

a must be 1

Therefore, you would have to factor out the 5 or, if it's an equation, divide both sides by 5.

$$x^2 - \frac{8}{5}x + \frac{3}{5} = 0$$

Solve by completing the square.

subtract 3 from both sides

$$5x^2 - 8x + 3 = 0$$

$$5x^2 - 8x = -3$$

Divide both sides by 5

$$x^2 - \frac{8}{5}x = -\frac{3}{5}$$

Add $(b/2)^2$ to both sides and simplify

$$x^2 - \frac{8}{5}x + \frac{16}{25} = -\frac{3}{5} + \frac{16}{25}$$

$$x^2 - \frac{8}{5}x + \frac{16}{25} = \frac{1}{25}$$

Rewrite left side as $()^2$

$$\left(x - \frac{4}{5}\right)^2 = \frac{1}{25}$$

Square root both sides.

$$\sqrt{\left(x - \frac{4}{5}\right)^2} = \sqrt{\frac{1}{25}}$$

$$x - \frac{4}{5} = \pm \frac{1}{5}$$

$$x = \frac{5}{5} \pm \frac{1}{5}$$

Add 4/5 to both sides and simplify