

Yesterday we explored what the graph of  $Y = a|x|$  looks like for different values of  $a$ .

$a > 0 \rightarrow$  V-shape opens up       $a < 0 \rightarrow$  V-shape opens down

When  $a > 1$  it is called a vertical stretch factor and the graph is taller.

When  $0 < a < 1$  it is called a vertical shrink factor and the graph is shorter.

**Step 1** Graph  $Y_2 = |x + h|$  or  $Y_2 = |x - h|$  by using different values for  $h$ . Describe how different values of  $h$  affect the graph.

$$y = |x + 5|$$

Graph translates  
5 units LEFT

Vertex will be  $(-5, 0)$

$$y = |x - 3|$$

Graph translates  
3 units RIGHT

Vertex will be  $(3, 0)$

$$y = |x - h|$$

The x-coordinate of  
the vertex is  $h$

**Step 2** Graph  $Y_2 = |x| + k$  or  $Y_2 = |x| - k$  by using different values for  $k$ . Describe how different values of  $k$  affect the graph.

$$y = |x| + 7$$

Graph translates  
7 units UP

Vertex will be  $(0, 7)$

$$y = |x| - 1$$

Graph translates  
1 unit DOWN

Vertex will be  $(0, -1)$

$$y = |x| + k$$

The y-coordinate of  
the vertex is  $k$

Describe the transformation of the parent function  
 $Y = |X|$  and state the coordinates of the vertex.

1.  $y = |x + 11| - 8$

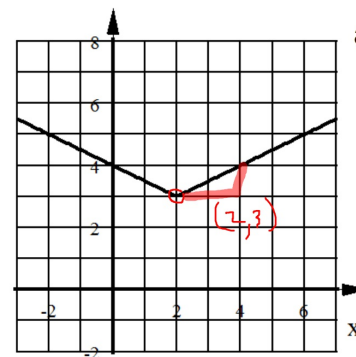
11 left and 8 down  
 $(-11, -8)$

2.  $y = |x - 20| + 13$

20 right and 13 up  
 $(20, 13)$

In general, given  $y = |x - h| + k$ ,  
the coordinates of the vertex are

$(h, k)$

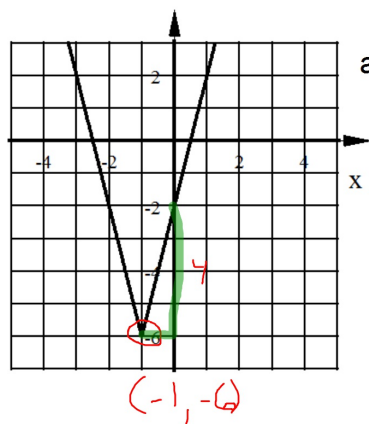


a. Describe the transformation

• 2 right, 3 up, 1/2 as tall

b. Write the equation

$$y = \frac{1}{2} |x - 2| + 3$$



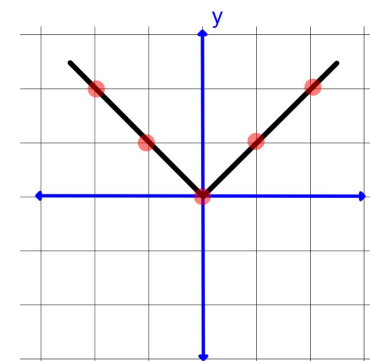
a. Describe the transformation

• 1 left, 6 down, 4x as tall.

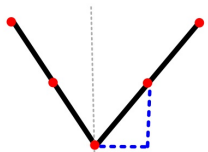
b. Write the equation

$$y = 4 |x + 1| - 6$$

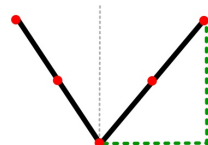
The parent Absolute Value function:  $y = |x|$



The parent Absolute Value function:  $y = |x|$



From the vertex the first "good" point is 1 right and 1 up



From the vertex the second "good" point is 2 right and 2 up

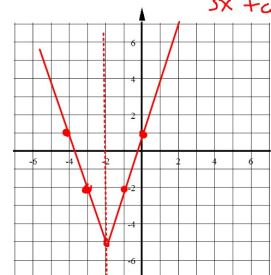
You can then use the Line of Symmetry to find points on the other side.

Using graph paper not a graphing calculator do the following for each Absolute Value function:

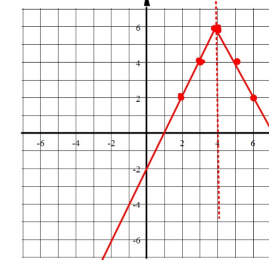
a. Describe the transformation each equation represents.

b. Graph using at least 5 points.

1.  $y = 3|x + 2| - 5$    
 2 left + 5 down   
 3x taller



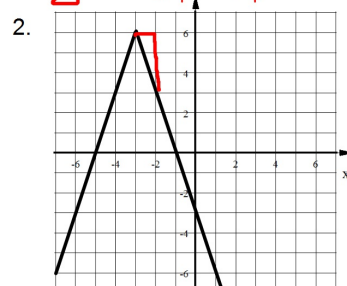
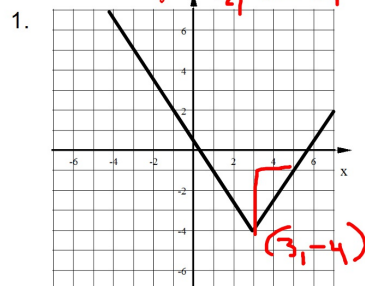
2.  $y = -2|x - 4| + 6$    
 4RT, 6up,   
 upsidedown   
 2x taller



Do the following for each graph:

a. Describe the transformation each equation represents. ✓

b. Write the equation of each.



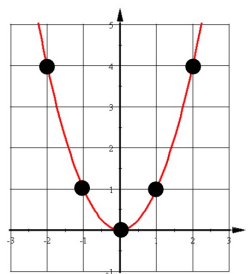
In general, if the function  $y = f(x)$  is transformed the following way:

$$y = a f(x - h) + k$$

The parent function has been:

- Stretched/Shrunk vertically by a factor of  $a$
- Reflected over x-axis if  $a < 0$
- Translated horizontally  $h$  units.
- Translated vertically  $k$  units.

Parent Quadratic Function:  $y = x^2$



Vertex:  $(0,0)$

Line of Symmetry:  $x=0$

First "good" from vertex:

1 right, 1 up

Second "good" point from vertex:

2 right, 4 up

x	y
-2	4
-1	1
0	0
1	1
2	4