

Use these two functions:

$$f(x) = 6x - 5$$

$$g(x) = 2x + 3$$

Find and simplify $f(g(x))$

$$\begin{aligned} & 6(2x+3) - 5 \\ &= 12x + 18 - 5 \\ &= \boxed{12x + 13} \end{aligned}$$

Use these functions:

$$f(x) = x^2 + 7$$

$$g(x) = x + 5$$

$$h(x) = 2x - 9$$

1. Find $f(g(x))$. Simplify as much as possible.

$$(x+5)^2 + 7$$

$$x^2 + 10x + 25 + 7 = \boxed{x^2 + 10x + 32}$$

2. Find $h(g(x))$. Simplify as much as possible.

$$\begin{aligned} 2(x+5) - 9 &= 2x + 10 - 9 \\ &= \boxed{2x + 1} \end{aligned}$$

$$\begin{array}{|c|c|} \hline x & x+5 \\ \hline x & x^2+5x \\ \hline x+5 & 5x+25 \\ \hline \end{array}$$
$$x^2 + 10x + 25$$

$$(5x - 13)^2 = 25x^2 - 130x + 169$$

\uparrow
 $(5x)(-13) \cdot 2$

Use these functions:

$$f(x) = x^2 + 7$$

$$g(x) = x + 5$$

$$h(x) = 2x - 9$$

Find $h(h(x))$.

$$\begin{aligned} & 2(2x-9) - 9 \\ &= \boxed{4x - 27} \end{aligned}$$

Use these two functions.

$$f(x) = (x+3)^2 - 1 \quad g(x) = \sqrt{x+1} - 3$$

1. Find $f(g(x))$. Simplify as much as possible.

$$= (\sqrt{x+1} - 3 + 3)^2 - 1 = (\sqrt{x+1})^2 - 1$$

2. Find $g(f(x))$. Simplify as much as possible.

$$\sqrt{(x+3)^2 - 1 + 1} - 3$$
$$\sqrt{(x+3)^2} - 3 = x+3-3 = x$$

$$x+1-1 = x$$

Whenever $f(g(x))=x$ and $g(f(x))=x$

the functions $f(x)$ and $g(x)$ are called INVERSES

