

AND

OR

AND

For dinner Eric said that he will eat a salad AND a hamburger.

- Eric ate only a salad. Is his original statement true or false? *False*
- Eric ate only a hamburger. Is his original statement true or false? *False*
- Eric ate both a salad and a hamburger. Is his original statement true or false? *True*

A statement involving the word AND is only true if:  
**BOTH parts are true.**

OR

Amani said that tonight she would study OR listen to music.

- Amani only studied. Is her statement true or false? *True*
- Amani only listened to music. Is her statement true or false? *True*
- Amani studied and listened to music. Is her statement true or false? *True*

A statement involving the word OR is true if:

- Only one of the statmens is true
- or
- If both statements are true

$$13 < 4x + 5 < 21$$

This compound inequality  
is really a combination of  
the two following inequalities:

$$4x+5>13 \text{ AND } 4x+5<21$$

Solve.

$$\begin{array}{r} 13 < 4x + 5 < 21 \\ -5 \quad -5 \quad -5 \\ \hline 8 < 4x < 16 \\ \hline 2 < x < 4 \end{array}$$

or

$$\begin{array}{r} 4x+5>13 \text{ AND } 4x+5<21 \\ -5 \quad -5 \quad -5 \quad -5 \\ \hline 4x > 8 \quad 4x < 16 \\ \hline x > 2 \text{ AND } x < 4 \end{array}$$

### Compound Inequalities

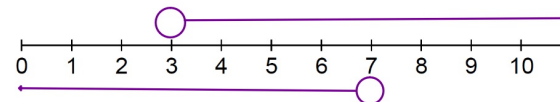
Two inequalities connected with one of the following words:

AND

OR

Inequalities connected with the word AND:

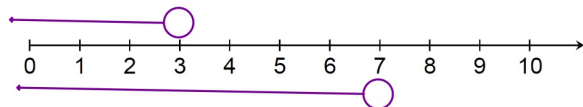
$$w > 3 \text{ AND } w < 7$$



Can be written as one inequality:  $3 < w < 7$

Inequalities connected with the word AND:

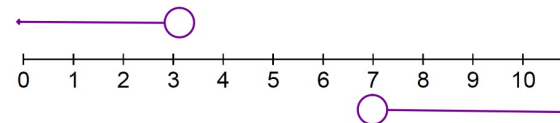
$$w < 3 \text{ AND } w < 7$$



Can be written as one inequality:  $w < 3$

Inequalities connected with the word AND:

$$w < 3 \text{ AND } w > 7$$



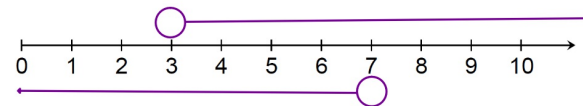
Can be written as NO SOLUTION

When you graph two inequalities connected with the word AND the final solution is:

Where they OVERLAP

Inequalities connected with the word OR:

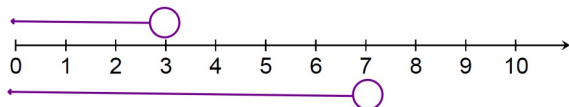
$$w > 3 \text{ OR } w < 7$$



Can be written as ALL REAL NUMBERS

Inequalities connected with the word OR:

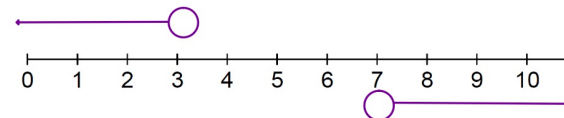
$$w < 3 \text{ OR } w < 7$$



Can be written as one inequality:  $w < 3$

Inequalities connected with the word OR:

$$w < 3 \text{ OR } w > 7$$



Can only be written as  $w < 3 \text{ OR } w > 7$

When you graph two inequalities connected with the word **OR** the final solution is:

Anywhere the graph is shaded. (for either or both inequalities)

What would have to be true for a compound inequality using the word **AND** to have **NO SOLUTION**?

- There are no numbers that make both inequalities true.
- Graphs of inequalities don't overlap anywhere.

What would have to be true for a compound inequality using the word **AND** to have a solution of **ALL REAL NUMBERS**?

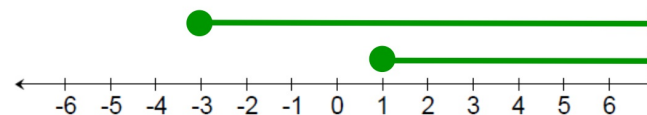
- The solution to BOTH inequalities must be All Real Numbers.
- Both graphs must be the entire number line.

What would have to be true for a compound inequality using the word **OR** to have **NO SOLUTION**?

- Both inequalities must be **NO SOLUTION**.

What would have to be true for a compound inequality using the word **OR** to have a solution of **ALL REAL NUMBERS**?

- The solutions to the two inequalities combined must contain all real numbers.
- Graphs must point in opposite directions and overlap.



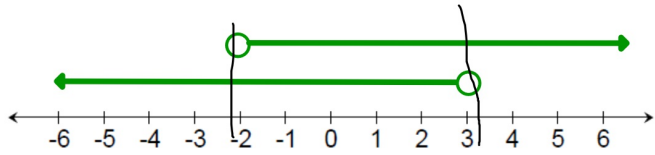
What is the solution to the above compound inequality using the word....

**AND**

$$x \geq 1$$

**OR**

$$x \geq -3$$



What is the solution to the above compound inequality using the word....

AND  
 $-2 < x < 3$

OR  $Q$