



Explicit Formula:

A formula that expresses the n^{th} term using n (term number).

Example: $a_n = (n + 3)^2$

$$9_{10} = 169$$

Write an explicit formula for each sequence

1. 9, 10, 11, 12, ... $a_n = n + 8$
 $n = 1 \quad 2 \quad 3 \quad 4$
2. 20, 30, 40, 50, ... $a_n = \begin{cases} 10(n+1) \\ \text{or} \\ 10n + 10 \\ \text{or} \\ 10(n-1) + 20 \end{cases}$
 $n = 1 \quad 2 \quad 3 \quad 4$
3. $\frac{5}{3}, \frac{10}{4}, \frac{15}{5}, \frac{20}{6}, \dots$ $a_n = \frac{5n}{n+2}$
 $n = 1 \quad 2 \quad 3 \quad 4$

Recursive Formula: Defines the n^{th} term (a_n) using the previous term (a_{n-1})

Example: $a_1 = 16$
 $a_n = a_{n-1} + 7$
 16, 23, 30, 37, 44
 $a_5 = 44$

Write a recursive formula for each sequence.

1. 1664, -416, 104, -26, ...

$$a_1 = 1664$$

$$a_n = \frac{a_{n-1}}{-4}$$

2. 13.5, 16, 18.5, 21, ...

$$a_1 = 13.5$$

$$a_n = a_{n-1} + 2.5$$

Sec 11-2: Arithmetic Sequences

Created by adding the same number each time.

The difference between consecutive terms is constant.

d = Common Difference

Find the Common Difference (**d**) in each Arithmetic sequence.

1. 14, 22, 30, 38, ... **d** = 8

2. 29, 22, 15, 8, ... **d** = -7

$$\mathbf{d} = a_n - a_{n-1} = \text{Any term} - \text{Previous term}$$

Given the following Arithmetic Sequence

16, **x**, 28, ... Find the value of **x**

$$\begin{aligned} 28 - x &= x - 16 \\ 28 + 16 &= 2x \end{aligned} \quad \frac{28 + 16}{2} = x$$

x is called the Arithmetic Mean of 16 and 28.

Find the missing terms of this Arithmetic sequence.

$$34, \underline{40}, \underline{46}, \underline{52}, 58$$

$$\begin{array}{ccccccc} & +4 & & +4 & & +4 & & +4 & & +4 \\ \text{11} & \text{15} & \text{19} & \text{23} & \text{27} & \text{31} \end{array}$$

$$31 - 11 = 20 \div 5 = 4$$

Recursive Formula for an Arithmetic Sequence:

7, 12, 17, 22, ...

Find **d**.

a_1 = Given First Term

$$a_n = a_{n-1} + \mathbf{d}$$

Write a recursive formula for this sequence:

19, 11, 3, -5, ...

$$a_1 = 19$$

$$a_n = a_{n-1} - 8$$

Explicit Formula for an Arithmetic Sequence:

5, 9, 13, 17, 21, ...

Find **d**. $d = 4$

$$a_1 = 5$$

$$a_2 = 5 + 4$$

$$a_3 = 5 + 4 + 4$$

$$a_4 = 5 + 4 + 4 + 4$$

$$a_5 = 5 + 4 + 4 + 4 + 4$$

.

.

.

$$a_n =$$

$$a_n = 5 + (n-1)4$$

Explicit Formula:

$$a_n = a_1 + (n-1)\mathbf{d}$$

Write the explicit formula for this sequence.

-34, -21, -8, 5, ...

1

$$a_n = -34 + (n-1)13$$