

You take a three question True/False quiz.

If you guess on all three problems what is the probability that you pass?

Simulation:

Performing an experiment to model an actual situation.

What could you use to simulate guessing on a True/False question?

How could you simulate guessing on three T/F questions?

You'll use 3 pennies to simulate guessing on three T/F questions.

We'll assign Heads to be a correct answer.

| >Work in pairs | | |
|--|------------------------|---------------------|
| >One person will shake up and drop all three coins on the table | | |
| >The other person will record the results as H or T for each coin. | | |
| >Perform 25 trials | | |
| Trial # | Results of the 3 coins | # guessed correctly |
| Ex: | H,T,T | 1 |
| 1 | | |
| 2 | | |
| 3 | | |
| 4 | | |
| 5 | | |
| 6 | | |
| 7 | | |
| 8 | | |
| 9 | | |
| 10 | | |
| 11 | | |
| 12 | | |
| 13 | | |
| 14 | | |
| 15 | | |
| 16 | | |
| 17 | | |
| 18 | | |
| 19 | | |
| 20 | | |
| 21 | | |
| 22 | | |
| 23 | | |
| 24 | | |
| 25 | | |

times each outcome occurred:

| | # times each outcome occurred: | total |
|-----------|--|------------|
| 3 correct | 1, 1, 4, 5, 4, 4, 2, 3, 3, 3, 7, 2 = | 39 |
| 2 correct | 6, 10, 9, 9, 10, 9, 10, 11, 8, 10, 8, 13 = | 113 |
| 1 correct | 13, 10, 10, 8, 8, 10, 8, 6, 12, 10, 8, 8 = | 111 |
| 0 correct | 5, 4, 2, 3, 4, 2, 5, 5, 2, 2, 2, 1 = | 37 |
| | | <u>300</u> |

Find each experimental Probability as a percent to the nearest tenth.

$$1. P(\text{all correct}) = \frac{39}{300} = 13.0\%$$

$$2. P(\text{none correct}) = 12.3\%$$

$$3. P(\text{pass}) = P(2 \text{ or } 3 \text{ correct}) = \frac{152}{300} = 50.7\%$$

$$4. P(\text{fail}) = P(0 \text{ or } 1 \text{ correct}) = \frac{148}{300} = 49.3\%$$

What is the Theoretical Probability of each?

1. Probability of guessing CORRECTLY on a single question.

$$50\%$$

2. Probability of guessing WRONG on a single question.

$$50\%$$

3. P(all correct)

$$CCC = (.5)(.5)(.5) = .125$$

$$12.5\%$$

4. P(none correct)

$$WWW = (.5)(.5)(.5) = .125$$

$$12.5\%$$

3. P(pass) → P(2 or 3 correct)

P(2 correct)

$$P(3 \text{ correct}) = (.5)(.5)(.5) = .125$$

$$CCW = (.5)(.5)(.5) = .125$$

or

$$CWC = (.5)(.5)(.5) = .125$$

or

$$WCC = (.5)(.5)(.5) = .125$$

$$P(\text{Pass}) = .125 + .125 + .125 + .125$$

$$= .5$$

$$50\%$$

4. P(fail)

$$50\%$$

P(failing) and P(passing) are called **complementary events**

$$P(\text{failing}) + P(\text{passing}) = 100\%$$

$$P(\text{failing}) = 100\% - P(\text{passing})$$

$$P(\text{failing}) = 100\% - 50\% = 50\%$$

What is the complementary event for each?

1. P(Correct) \longrightarrow P(Incorrect)

2. P(ON) \longrightarrow P(OFF)

3. P(Heads) \longrightarrow P(Tails)

4. P(Tuba) \longrightarrow P(Not Tuba)

Suppose you are given this probability:

$$P(\text{Turtle}) = \frac{43}{60}$$

What is the complementary event? $P(\text{NOT TURTLE})$

What is the probability of this complement? $\frac{17}{60}$

Suppose you guess at all three questions of a multiple choice quiz where there are 4 choices for each question (ABCD). What is the probability that you'll pass?

What is the probability that you guess correctly on any one problem? 0.25

All correct: $CCC = (.25)(.25)(.25) = 1.5625\%$

Two correct: $CCW = (.25)(.25)(.75) = 4.6875\%$
 $CWC = (.25)(.75)(.25)$
 $WCC = (.75)(.25)(.25)$

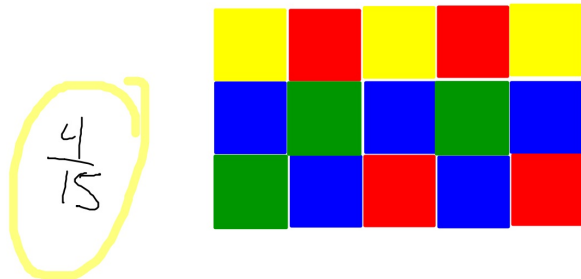
Probability of passing =

$$1.5625\% + 14.0625\% = 15.625\% \text{ chance of passing}$$

Getting all 3 correct

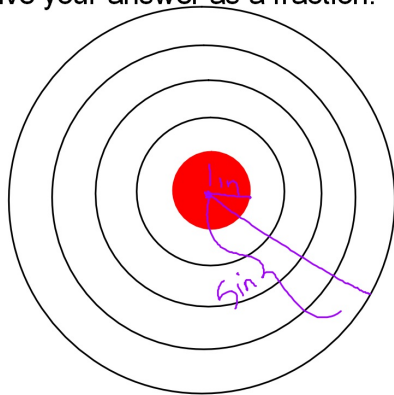
Getting 2 of the 3 correct

You throw a dart at the target below. Assuming the dart lands somewhere on the target, find the probability that it lands on a Red space. All spaces are equal in size.



$$\text{Geometric Probability:} = \frac{\text{Area of Favorable Region}}{\text{Total Area}}$$

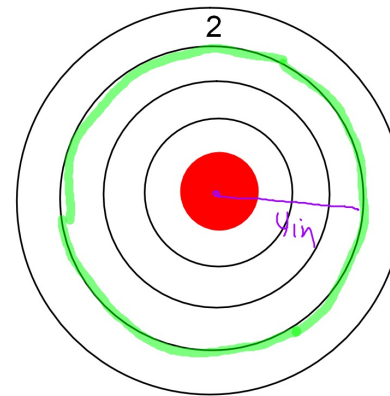
You throw a dart at the target below. Assuming the dart lands somewhere on the target, find the probability that it lands in the bulls-eye. The radius of the bulls-eye is 1 in. The width of each ring is 1 in. Give your answer as a fraction.



$$\frac{\text{Area of Bulls-eye}}{\text{Area of Target}} = \frac{\pi(1\text{in})^2}{\pi(5\text{in})^2} = \frac{1\pi\text{in}^2}{25\pi\text{in}^2} = \frac{1}{25}$$

The outer ring is worth 2 points. Find the probability that the dart lands in the 2 point ring.

$$\text{Area of the 2 pt ring} = \text{Area of the target} - \text{Area of 4th circle}$$



$$\frac{\pi(5\text{in})^2 - \pi(4\text{in})^2}{25\pi\text{in}^2} = \frac{9\pi}{25\pi} = \frac{9}{25}$$