

1. Simplify each. Use absolute value symbols when necessary.

a) $\sqrt[5]{54m^{18}n^{12}p^{23}}$

$$\begin{array}{cccc} \sqrt[5]{54} & \sqrt[5]{m^{18}} & \sqrt[5]{n^{12}} & \sqrt[5]{p^{23}} \\ \wedge & \downarrow & \downarrow & \wedge \\ \sqrt[5]{9 \cdot 6} & 6 & & p^{22} p^1 \\ 3\sqrt[5]{6} & m^9 & n^6 & p^{11}\sqrt[5]{p} \end{array}$$

$$3|m^9|n^6|p^{11}\sqrt[5]{6p}$$

b) $\sqrt[5]{g^{14}h^{27}j^{43}}$

$$g^2 h^5 j^8 \sqrt[5]{g^4 h^2 j^3}$$

2. Simplify.

$$\begin{array}{cccc} \sqrt{32} & + & \sqrt{108} & - & \sqrt{98} & + & \sqrt{75} \\ \wedge & & \wedge & & \wedge & & \wedge \\ 16 \cdot 2 & & 36 \cdot 3 & & 49 \cdot 2 & & 25 \cdot 3 \\ 4\sqrt{2} & + & 6\sqrt{3} & - & 7\sqrt{2} & + & 5\sqrt{3} \\ -3\sqrt{2} & + & 11\sqrt{3} & & & & \end{array}$$

3. Rationalize each denominator. Simplify answer.

a) $\frac{18}{\sqrt[3]{2a^2b^7}} \cdot \frac{\sqrt[3]{4ab^2}}{\sqrt[3]{4ab^2}}$

$$\sqrt[3]{2^3 a^3 b^9}$$

$$\frac{9\cancel{18} \cdot \sqrt[3]{4ab^2}}{\cancel{2}ab^3}$$

b) $\frac{15}{\sqrt[4]{3x^5y^{19}}} \cdot \frac{\sqrt[4]{27x^3y}}{\sqrt[4]{3^3x^3y}} = \frac{\cancel{5} \cancel{3} \sqrt[4]{27x^3y}}{\cancel{3} x^3 y^5}$

$\sqrt[4]{3^4 x^8 y^{20}}$

c) $\frac{7}{5 - \sqrt{11}} \cdot \frac{5 + \sqrt{11}}{5 + \sqrt{11}} = \frac{7(5 + \sqrt{11})}{25 - 11} = \frac{7(5 + \sqrt{11})}{14} = \frac{5 + \sqrt{11}}{2}$

4. Solve this radical equation:

$$\sqrt[4]{5x+21} - 3 = x$$

$$(\sqrt[4]{5x+21})^2 = (x+3)^2$$

$$5x+21 = x^2+6x+9$$

$$0 = x^2+x-12$$

$$(x+4)(x-3)$$

$$x = -4, 3$$