

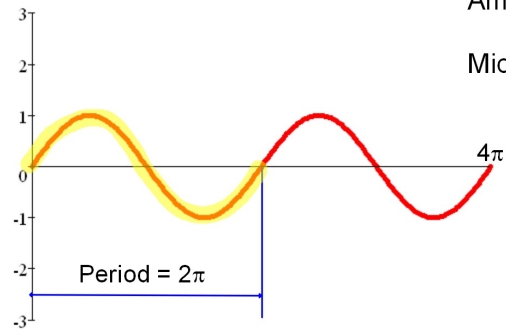
Parent Function:

$$y = \sin \theta$$

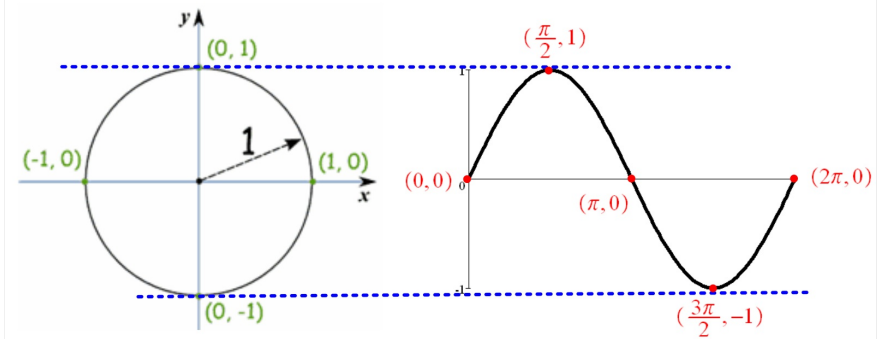
Period = 2π

Amplitude = 1

Midline: $y = 0$

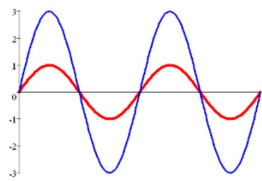


The Parent Function $y = \sin \theta$



1. $y = 3\sin \theta$

$y = \sin \theta$



$$y = a \sin \theta$$

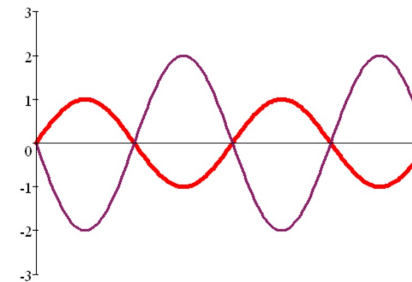
a = Amplitude

Stretch or Shrink
Factor.

$$y = -2\sin \theta$$

$$y = \sin \theta$$

$y = -2\sin \theta$ is upside down
and twice as tall as the
parent function $y = \sin \theta$



$$y = a\sin\theta$$

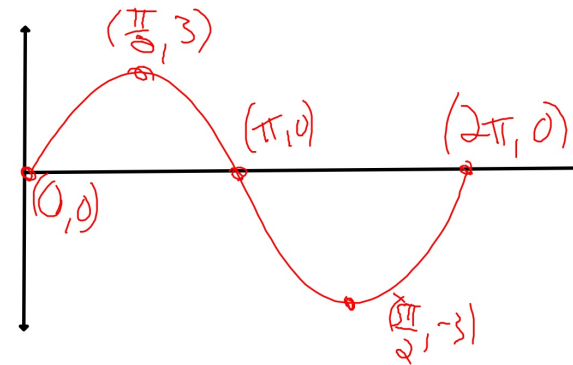
$|a|$ = Amplitude (vertical stretch or shrink factor)

$a < 0$ x-axis reflection
upside down

Sketch one period of the graph of

$$y = 3\sin\theta$$

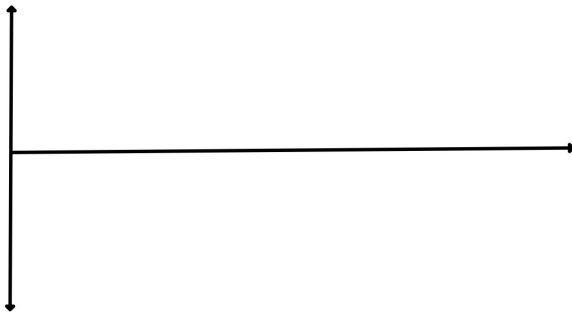
Label the coordinates of all x-intercepts, minimums, and maximums.



Sketch one period of the graph of

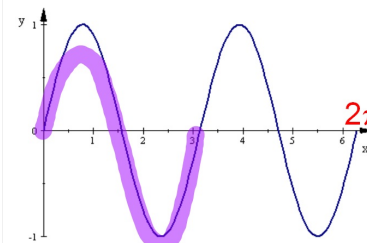
$$y = -5\sin x$$

Label the coordinates of all x-intercepts, minimums, and maximums.



Graph the following and describe what happens to the graph. $x[0, 2\pi]$ $y[-1, 1]$

1. $y = \sin(2\theta)$

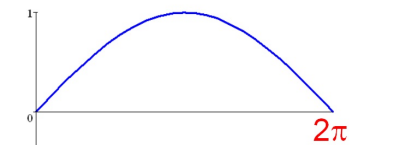


cycles = 2

$$b = 2$$

$$\text{Period} = \pi$$

2. $y = \sin(0.5\theta)$



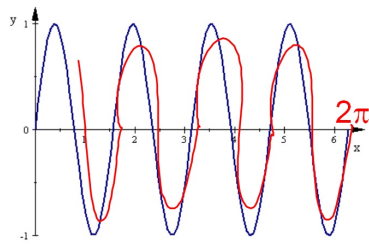
cycles = $\frac{1}{2}$

$$b = \frac{1}{2}$$

$$\text{Period} = 4\pi$$

$$\frac{2\pi}{\frac{1}{2}} = 4$$

3. $y = \sin(4\theta)$

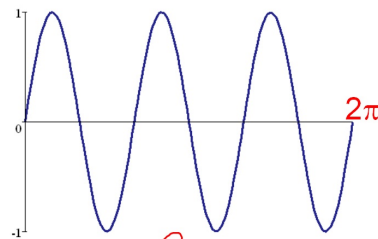


cycles = 4

$b = 4$

Period = $\frac{2\pi}{4} = \frac{\pi}{2}$

4. $y = \sin(3\theta)$



cycles = 3

$b = 3$

Period = $\frac{2\pi}{3}$

Remember the period of $y = \sin x$ is 2π

1. $y = \sin 2x$ $b = 2$ Period = π

2. $y = \sin \frac{1}{2}x$ $b = \frac{1}{2}$ Period = 4π

3. $y = \sin 4x$ $b = 4$ Period = $\frac{\pi}{2}$

4. $y = \sin 3x$ $b = 3$ Period = $\frac{2\pi}{3}$

Start With	b	End With
2π	2	π
2π	$\frac{1}{2}$	4π
2π	4	$\frac{\pi}{2}$
2π	3	$\frac{2\pi}{3}$

What is the relationship between b and the Period?

$b = (2\pi)/\text{Period}$

$y = a\sin b\theta$

notes

Amplitude = a

Period = $\frac{2\pi}{b}$

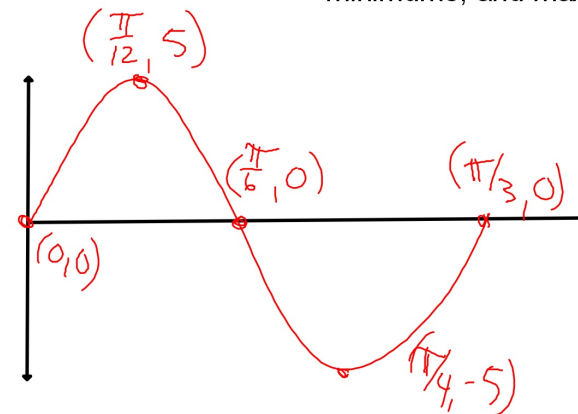
Midline: $y = 0$

Example

Sketch one period of the graph of

$y = 5\sin 6x$

Label the coordinates of all x-intercepts, minimums, and maximums.



Amplitude = 5

Period =

$\frac{2\pi}{6} = \frac{\pi}{3}$

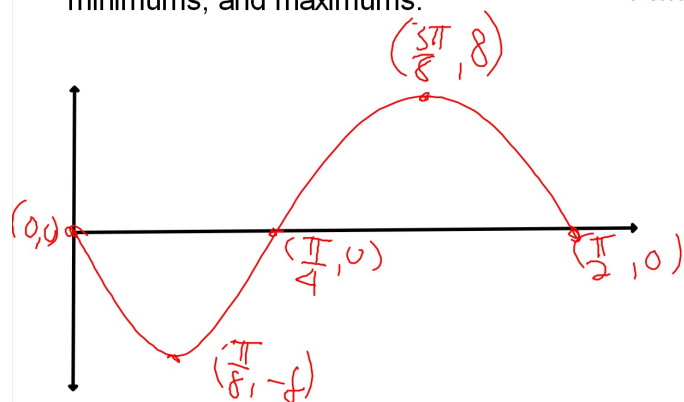
Sketch one period of the graph of

$$y = -8\sin 4x$$

Label the coordinates of all x-intercepts, minimums, and maximums.

Amplitude =

$$\text{Period} = \frac{2\pi}{4} = \frac{\pi}{2}$$



Sketch one period of the graph of

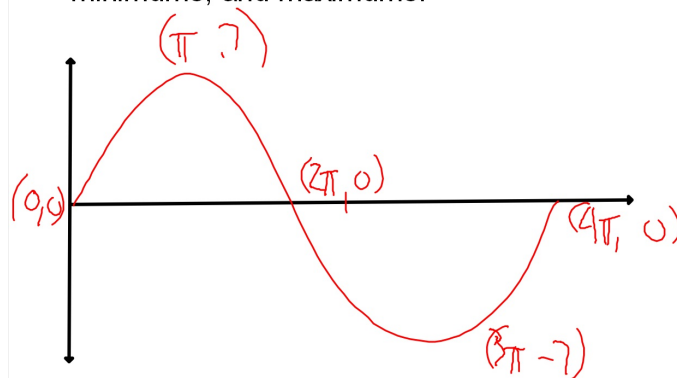
$$y = 7\sin\left(\frac{x}{2}\right) \rightarrow y = 7\sin\left(\frac{1}{2}x\right)$$

Label the coordinates of all x-intercepts, minimums, and maximums.

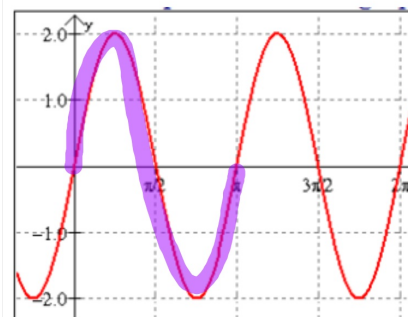
Amplitude =

Period =

$$\frac{2\pi}{\frac{1}{2}} = 4\pi$$



Write the equation of this sine function as $y = a\sin bx$



Amplitude = 2

$a = 2$

$$\text{Period} = \pi = \frac{2\pi}{b}$$

$$y = 2\sin 2x$$

$b = 2$

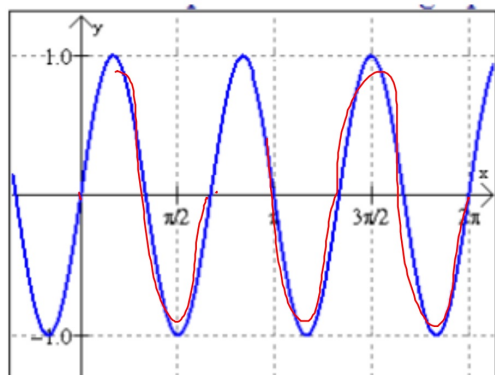
$$\text{Period} = \frac{2\pi}{b}$$

$$b = \frac{2\pi}{\text{Period}}$$

or

$b = \# \text{ of periods in } 2\pi$

Write the equation of this sine function.



$$y = \sin 3x$$

Amplitude = 1

Period = $\frac{2\pi}{3}$ $b=3$

$$b = \frac{2\pi}{\text{period}}$$
$$\frac{2\pi}{\frac{2\pi}{3}}$$
$$2\pi \cdot \frac{3}{2\pi}$$