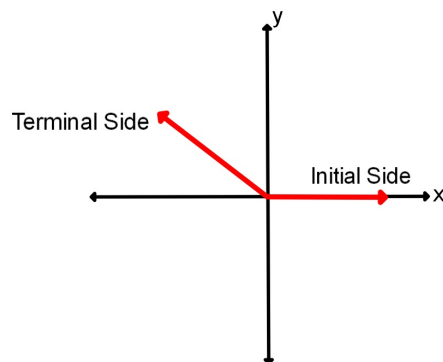


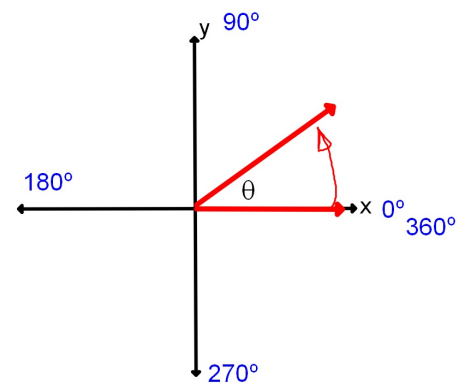
Sec 13-2 Angles in Standard Position:

- Vertex is at the origin
- One ray is on the positive x-axis.



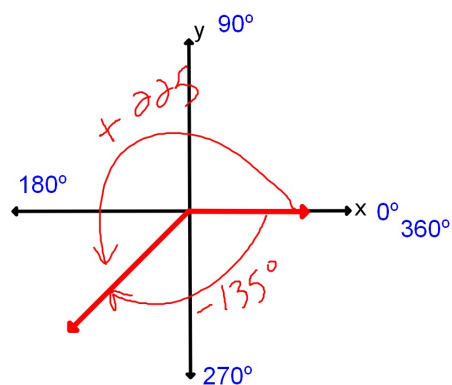
Measuring an angle in standard position:

- 0° is on the positive x-axis
- Positive angles are measured Counter-Clockwise



The terminal side is in the middle of the third quadrant.
Give two possible measures for this angle.

$$\theta = -135^\circ \quad \theta = 225^\circ$$



Can you give 2 more possible measures of this angle?

$$\theta = -495^\circ$$

$$\theta = 585^\circ$$

Coterminal Angles: Angles in standard position that have the same terminal side.

They start and stop in the same spot but aren't the same angle. How could this be?

Find a positive and a negative coterminal angle for each given angle.

To find coterminal angles take the original angle and \pm multiples of 360°

1. $\theta = 800^\circ$

2. $\theta = -70^\circ$

Pos 1160° or 440°

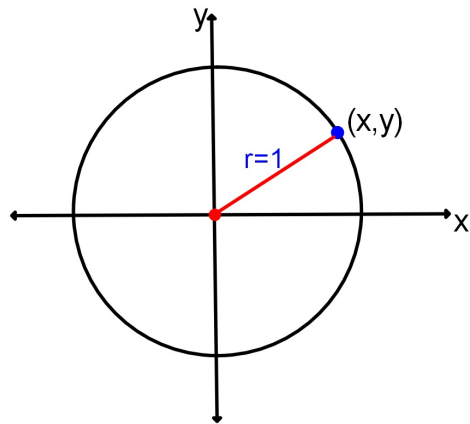
NEG -280°

pos 290°

NEG -430°

The Unit Circle:

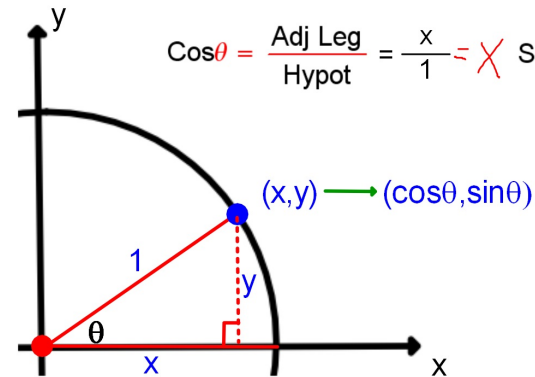
A circle whose center is at the origin and its radius = 1.



Find the exact value of each:

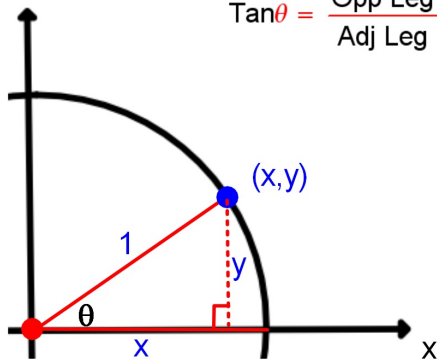
$\cos\theta$ & $\sin\theta$

$$\cos\theta = \frac{\text{Adj Leg}}{\text{Hypot}} = \frac{x}{1} = x \quad \sin\theta = \frac{\text{Opp Leg}}{\text{Hypot}} = \frac{y}{1} = y$$



$\tan\theta$

$$\tan\theta = \frac{\text{Opp Leg}}{\text{Adj Leg}} = \frac{y}{x}$$

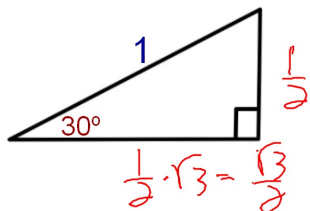


Using the Unit Circle:

Cosine of any angle = **x-coordinate** of the point on the Unit Circle corresponding to that angle.

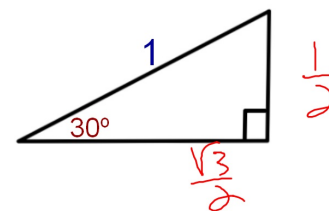
Sine of any angle = **y-coordinate** of the point on the Unit Circle corresponding to that angle.

Tangent of any angle = the ratio of $\frac{\text{y-coordinate}}{\text{x-coordinate}}$ of the point on the Unit Circle corresponding to that angle.



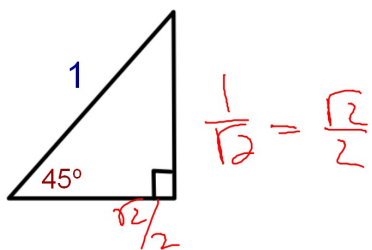
Find the exact value of each:

$$\begin{aligned} 1. \sin 30^\circ &= \frac{1/2}{1} = \frac{1}{2} & 2. \cos 30^\circ &= \frac{\frac{\sqrt{3}}{2}}{1} = \frac{\sqrt{3}}{2} \\ 3. \sin 60^\circ &= \frac{\frac{\sqrt{3}}{2}}{1} = \frac{\sqrt{3}}{2} & 4. \cos 60^\circ &= \frac{1/2}{1} = \frac{1}{2} \end{aligned}$$



Find the exact value of each:

$$\begin{aligned} 1. \tan 30^\circ &= \frac{1/2}{\frac{\sqrt{3}}{2}} = \frac{1}{2} \cdot \frac{2}{\sqrt{3}} = \frac{1}{\sqrt{3}} = \frac{\sqrt{3}}{3} \\ 2. \tan 60^\circ &= \frac{\frac{\sqrt{3}}{2}}{1/2} = \frac{\sqrt{3}}{2} \cdot \frac{2}{1} = \sqrt{3} \end{aligned}$$



Find the exact value of each:

$$\begin{aligned} 1. \sin 45^\circ &= \frac{\frac{\sqrt{2}}{2}}{1} = \frac{\sqrt{2}}{2} & 2. \cos 45^\circ &= \frac{\frac{\sqrt{2}}{2}}{1} = \frac{\sqrt{2}}{2} & 3. \tan 45^\circ &= \frac{\frac{\sqrt{2}}{2}}{\frac{\sqrt{2}}{2}} = 1 \end{aligned}$$