

Sec 7-3: Binomial Radical Expressions.

Simplify each:

$$\begin{aligned}
 1. \quad & 3\sqrt{50} + 7\sqrt{24} - 8\sqrt{54} - 9\sqrt{32} \\
 & 3\sqrt{25 \cdot 2} + 7\sqrt{4 \cdot 6} - 8\sqrt{9 \cdot 6} - 9\sqrt{16 \cdot 2} \\
 & 3 \cdot 5\sqrt{2} + 7 \cdot 2\sqrt{6} - 8 \cdot 3\sqrt{6} - 9 \cdot 4\sqrt{2} \\
 & 15\sqrt{2} + 14\sqrt{6} - 24\sqrt{6} - 36\sqrt{2} = -21\sqrt{2} - 10\sqrt{6}
 \end{aligned}$$

$$\begin{aligned}
 2. \quad & 4\sqrt{7}(5\sqrt{11} - 3\sqrt{7}) \\
 & 20\sqrt{77} - 12 \cdot 7 \\
 & = 20\sqrt{77} - 84
 \end{aligned}$$

3. Simplify.

$$5\sqrt{2}(9\sqrt{2} - 6\sqrt{10})$$

$$45 \cdot 2 - 30\sqrt{10}$$

$$90 - 30\sqrt{10}$$

Multiplying 2 binomial radical expressions

$$(5 + \sqrt{6})(4 - 3\sqrt{6})$$

$$= 20 - 11\sqrt{6}$$

	5	$+\sqrt{6}$
4	20	$+4\sqrt{6}$
$-3\sqrt{6}$	$-15\sqrt{6}$	$-3 \cdot 6 = -18$

Simplify each.

$$1. (\sqrt{7} + 2\sqrt{2})(5\sqrt{7} - \sqrt{2})$$

$$= 5 \cdot 7 - \sqrt{7 \cdot 2} + 10\sqrt{7 \cdot 2} - 2 \cdot 2$$

$$= 35 - \sqrt{14} + 10\sqrt{14} - 4 = 31 + 9\sqrt{14}$$

$$2. (10 + 7\sqrt{3})^2 = (10 + 7\sqrt{3})(10 + 7\sqrt{3})$$

$$= 100 + 70\sqrt{3} + 70\sqrt{3} + \underbrace{49 \cdot 3}_{147}$$

$$= 247 + 140\sqrt{3}$$

Simplify: $(m + 5)(m - 5)$

These are called
conjugates

$$= m^2 - 5^2$$

$$= m^2 - 25$$

$$(a + b)(a - b) = a^2 - b^2$$

Simplify:

$$(7 + \sqrt{11})(7 - \sqrt{11})$$

$$7^2 - (\sqrt{11})^2$$

$$= 49 - 11$$

$$= 38$$

Rationalize the denominator.

$$\begin{aligned} \frac{7}{8 + \sqrt{5}} \cdot \frac{8 - \sqrt{5}}{8 - \sqrt{5}} &= \frac{56 - 7\sqrt{5}}{8^2 - (\sqrt{5})^2} \\ &= \frac{56 - 7\sqrt{5}}{64 - 5} \\ &= \frac{56 - 7\sqrt{5}}{59} \end{aligned}$$