

Rationalize each denominator.

$$\begin{aligned}
 1. \quad \frac{9x}{\sqrt{12x^3y}} \cdot \frac{\sqrt{3xy}}{\sqrt{3xy}} &= \frac{9x\sqrt{3xy}}{\sqrt{36x^4y^2}} \\
 &= \frac{9x\sqrt{3xy}}{6x^2y} \\
 &= \frac{3\sqrt{3xy}}{2xy}
 \end{aligned}$$

$$\begin{aligned}
 2. \quad \frac{\sqrt{6a^{13}b^4}}{\sqrt{5a^7b^9}} \cdot \frac{\sqrt{5ab}}{\sqrt{5ab}} &= \frac{\sqrt{30a^{14}b^5}}{\sqrt{5^2a^8b^{10}}} \\
 &= \frac{a^7b^2\sqrt{30b}}{5a^4b^5} \\
 &= \frac{a^3\sqrt{30b}}{5b^3}
 \end{aligned}$$

$$\begin{aligned}
 3. \quad \frac{5Q}{\sqrt[3]{10P^{16}Q^2}} \cdot \frac{\sqrt[3]{10^2P^2Q}}{\sqrt[3]{10^2P^2Q}} &= \frac{5Q\sqrt[3]{100P^2Q}}{\sqrt[3]{10^3P^{18}Q^3}} \\
 &= \frac{5Q\sqrt[3]{100P^2Q}}{10P^6Q} \\
 &= \frac{\sqrt[3]{100P^2Q}}{2P^6}
 \end{aligned}$$

$$\begin{aligned}
 4. \frac{4c^3d}{\sqrt[6]{2c^7d^{15}}} \cdot \frac{\sqrt[6]{2^5c^5d^3}}{\sqrt[6]{2^5c^5d^3}} &= \frac{4c^3d\sqrt[6]{2^5c^5d^3}}{\sqrt[6]{2^6c^{12}d^{18}}} \\
 &= \frac{4c^3d\sqrt[6]{2^5c^5d^3}}{2c^2d^3} \\
 &= \frac{2c\sqrt[6]{2^5c^5d^3}}{d^2}
 \end{aligned}$$

$$\begin{aligned}
 5. \frac{\sqrt{2}-8\sqrt{6}}{\sqrt{6}} \cdot \frac{\sqrt{6}}{\sqrt{6}} &= \frac{\sqrt{12}-8\cdot 6}{6} \\
 &= \frac{2\sqrt{3}-48}{6} \\
 &= \frac{\sqrt{3}-24}{3}
 \end{aligned}$$