

You can now finish hwk #22

Sec 6-4: Solving Polynomial Equations:

1. Graphing

a. Finding Zeros

One side must equal zero

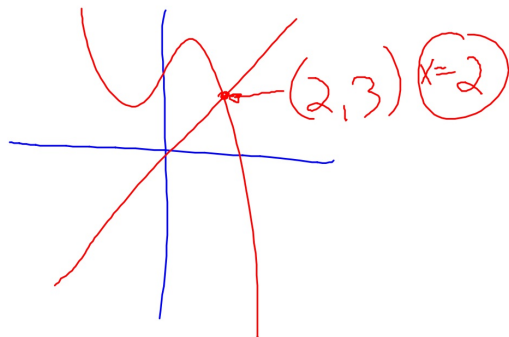
b. Finding Intersections

Graph the two sides of the equation separately.

2. Factoring

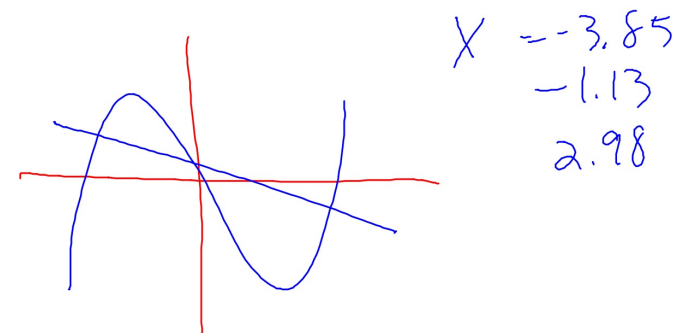
Solve this polynomial equation by graphing.

$$-2x^3 + 4x^2 - x + 5 = 2x - 1$$



Solve this polynomial equation by graphing.

$$x^3 + 2x^2 - 11x - 12 = -0.5x + 1$$



Factor each completely.

1. $3x^3 - 3x^2 - 126x$

2. $8x^2 - 2x - 15$

3. $8x^2 - 98$

1. $3x^3 - 3x^2 - 126x$

$3x(x^2 - x - 42)$
 $\begin{array}{c|cc} x & x^2 & 6x \\ \hline -7 & -7x & -42 \end{array}$
 $\begin{array}{r} -42 \\ -7 \\ -1 \end{array}$
 $3x(x-7)(x+6)$

2. $8x^2 - 2x - 15$

$\begin{array}{r} -120 \\ -12 \end{array} \begin{array}{r} 10 \\ -2 \end{array}$
 $\begin{array}{c|cc} 4x & 8x^2 & -12x \\ \hline 5 & 10x & -15 \end{array}$
 $(2x-3)(4x+5)$

3. $8x^2 - 98$

$2(4x^2 - 49)$
 $2(2x+7)$

Expand. $(x^2 - 5)(x^2 + 3) = x^4 - 5x^2 + 3x^2 - 15$
 $x^4 - 2x^2 - 15$

Factor. $x^4 + 3x^2 - 28$ Factoring using a Quadratic Pattern

$-4 \begin{array}{c} -28 \\ +7 \end{array}$ $\begin{array}{c} (x^2 - 4)(x^2 + 7) \\ (x \pm 2)(x^2 + 7) \end{array}$

Find all solutions by factoring.

Yes, you must make one side equal to zero in order to solve by factoring!

1. $8x^3 + 44x^2 - 24x = 0$

$4x(2x^2 + 11x - 6)$
 $4x(2x - 1)(x + 6)$

$x = 0, \frac{1}{2}, -6$

$\begin{array}{c} -12 \\ +12 \end{array} \begin{array}{c} -1 \\ 11 \end{array}$

2. $x^4 - 14x^2 - 32 = 0$

$(x^2 - 16)(x^2 + 2)$ $\begin{array}{c} -32 \\ -16 \end{array} \begin{array}{c} 2 \end{array}$

$\pm 4, \pm i\sqrt{2}$

of solutions to polynomial equations.

When you include both real and imaginary solutions a polynomial of degree n will have exactly n solutions.



Find all solutions by factoring.

3. $7x^3 - 35x = 0$

$7x(x^2 - 5) = 0$

$x = 0, \pm\sqrt{5}$

4. $5x^5 - 80x = 0$

$5x(x^4 - 16)$

$5x(x^2 - 4)(x^2 + 4)$
 $(x+2)(x-2)$

$x = 0, \pm 2, \pm 2i$