

Theorem**Factor Theorem**

The expression $x - a$ is a linear factor of a polynomial if and only if the value a is a **zero** of the related polynomial function.

Factor this quadratic

$$x^2 + 3x - 4 = (x + 4)(x - 1)$$

Summary**Equivalent Statements about Polynomials**

- ① -4 is a **solution** of $x^2 + 3x - 4 = 0$.
- ② -4 is an **x-intercept** of the graph of $y = x^2 + 3x - 4$.
- ③ -4 is a **zero** of $y = x^2 + 3x - 4$.
- ④ $x + 4$ is a **factor** of $x^2 + 3x - 4$.

Find this quotient without a calculator.

$$\begin{array}{r}
 1341 \text{ R}5 \\
 18 \overline{) 24,143} \\
 \underline{18} \\
 61 \\
 \underline{54} \\
 74 \\
 \underline{72} \\
 23 \\
 \underline{18} \\
 5
 \end{array}$$

How to deal with
a remainder

$$\frac{24,143}{18} =$$

Ways to deal with a
remainder

$$\begin{array}{r}
 1341 \text{ R}5 \\
 18 \overline{) 24,143} \\
 \underline{18} \\
 61 \\
 \underline{54} \\
 74 \\
 \underline{72} \\
 23 \\
 \underline{18} \\
 5
 \end{array}$$

$$\frac{24,143}{18} = \begin{cases} 1341 \text{ R}5 \\ 1341 \frac{5}{18} \\ 1341.\overline{27} \end{cases}$$

Sec 6-3: Polynomial Division.

1. Find this quotient:

Polynomial Long Division

$$(5x^3 + 13x^2 + 5x - 2) \div (x + 2) =$$

$$\begin{array}{r} \text{Quotient: } 5x^2 + 3x - 1 \\ x+2 \overline{) 5x^3 + 13x^2 + 5x - 2} \\ \underline{-(5x^3 + 10x^2)} \\ 3x^2 + 5x \\ \underline{-(3x^2 + 6x)} \\ -x - 2 \\ \underline{-(-x - 2)} \\ 0 \end{array}$$

2. Find this quotient:

$$(3x^3 - 8x^2 + 11x - 1) \div (x - 4) =$$

$$\begin{array}{r} \text{Quotient: } 3x^2 + 4x + 27 \text{ R } 107 \\ x-4 \overline{) 3x^3 - 8x^2 + 11x - 1} \\ \underline{-(3x^3 - 12x^2)} \\ 4x^2 + 11x \\ \underline{-(4x^2 - 16x)} \\ 27x - 1 \\ \underline{-(27x - 108)} \\ 107 \end{array}$$