

Section 7-6: Function Operations

What do you think each of these means?

$$(f + g)(x)$$

$$f(x) + g(x)$$

$$(f - g)(x)$$

$$f(x) - g(x)$$

$$(f \cdot g)(x)$$

$$f(x) \cdot g(x)$$

$$\left(\frac{f}{g}\right)(x)$$

$$\frac{f(x)}{g(x)}$$

Use these functions:

$$f(a) = 2a^2 + 6a$$

$$g(a) = 4a$$

$$h(a) = a + 3$$

Perform each function operation and state the domain.

1. $(f+h)(a)$ D: $\mathbb{R}$
 $f(a) + h(a) = 2a^2 + 6a + a + 3 = 2a^2 + 7a + 3$
2. $(h - g)(a)$ D: $\mathbb{R}$
 $h(a) - g(a) = a + 3 - 4a = 3 - 3a$
3. $(g \cdot f)(a)$ D: $\mathbb{R}$
 $(2a^2 + 6a) \cdot 4a = 8a^3 + 24a^2$
4. $\left(\frac{f}{g}\right)(a)$ D: $a \neq 0$
 $\frac{2a^2 + 6a}{4a} = \frac{2a(a+3)}{2 \cdot 2a} = \frac{a+3}{2}$

Use these functions:

$$f(x) = x^2 - 3x$$

$$g(x) = x - 7$$

1. Find $f(-5) = (-5)^2 - 3(-5) = 25 + 15 = 40$
2. Find $g(2)$
 $2 - 7 = -5$
3. Find $f(g(2))$
 $f(-5) = 40$

Composite Functions:

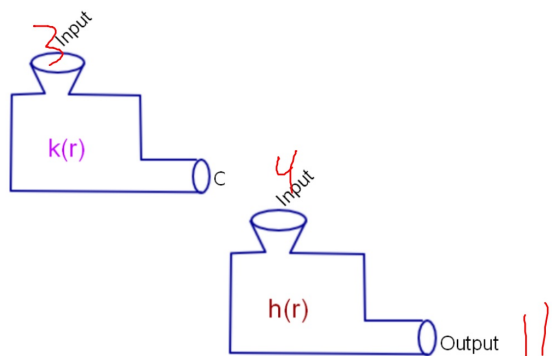
"f of g of x"

$$f(g(x)) \xrightarrow{\text{same as}} (f \circ g)(x)$$

Substitute function g into function f

given: $h(r) = 3r - 1$ $k(r) = r + 1$

find $h(k(3))$



Use these functions: $f(x) = x^2 + 3x$ $g(x) = 5x$

Find each. Simplify.

1. $f(g(x))$

2. $(g \circ f)(x)$

$$\begin{aligned} & (5x)^2 + 3(5x) \\ & \underline{25x^2 + 15x} \end{aligned}$$

3. $f(g(3))$

4. $(g \circ f)(7)$