

2. A company wants to maximize its profit. The following function models the company's profit as a function of the number of components it manufactures:

$$P(c) = -0.075c^2 + 240c + 27,500$$

a) Find the company's maximum profit.

\$219,500

THIS IS THE VERTEX

$$\begin{aligned} & \text{LOS} = \frac{-240}{2(-0.075)} = 1600 \\ & \text{Replace } c \text{ with } 1600 \end{aligned}$$

b) How many components should it manufacture to realize this maximum profit?

1600 components

Find the y-intercept for each parabola.

Replace x with zero

In a quadratic this is always the constant.

1. $y = -4x^2 + 6x$

$$-4(0)^2 + 6(0)$$

$$y = 0$$

2. $y = 9x^2 - 12 + 3x$

$$y\text{-int} = -12$$

Find the equation for the LOS of each parabola.

$$\text{LOS: } x = -\frac{b}{2a}$$

1. $y = 7x^2 + 8x - 11$

$$x = \frac{-8}{2(7)} = -\frac{4}{7}$$

$$x = -\frac{4}{7}$$

2. $y = -2x^2 + 24$

$$x = \frac{0}{2(-2)}$$

$$x = 0$$

Find the coordinates of the Vertex for each parabola.

Find LOS first, this is the x-coordinate of the Vertex.

To find the y-coordinate replace x with the LOS.

1. $y = 3x^2 + 36x - 19$

2. $y = -5x^2 + 18$

$$\begin{aligned} & \frac{-36}{2(3)} \rightarrow (-6, -127) \\ & \text{Replace } x \text{ with } -6 \end{aligned}$$

$$\begin{aligned} & \frac{0}{2(-5)} \rightarrow (0, 18) \\ & \text{Replace } x \text{ with } 0 \end{aligned}$$

Does each parabola have a Maximum or a Minimum?

1. $y = 0.0015x^2 - 87x - 101$

a is pos $\rightarrow$  $\rightarrow$ min

2. $y = -126x + 508x^2 + 93$

a is pos $\rightarrow$  $\rightarrow$ min

Find all EXACT real solutions for each quadratic using square roots.

1. $313 - 5x^2 = 153$
 $-313 \quad -313$

$-5x^2 = -160$
 $\frac{-5}{-5} \quad \frac{-160}{-5}$

$\sqrt{x^2} = \sqrt{32} = \sqrt{16 \cdot 2}$
 $\pm 4\sqrt{2}$

2. $2(x-1)^2 + 7 = 57$
 $-7 \quad -7$

$\frac{2(x-1)^2}{2} = \frac{50}{2}$

$\sqrt{(x-1)^2} = \sqrt{25}$

$x-1 = \pm 5$

$\begin{matrix} x-1=5 & x-1=-5 \\ +1 & +1 \end{matrix}$

$x = 6, -4$