

Last year, 2014 the TV you wanted cost \$450.

If each year the price increases 12%, how much will it cost in 2016?

$$y = 450(1.12)(1.12)$$

2015 2016

$$= \$564.48$$

$100\% + 12\% = 112\%$

Last year, 2014 the TV you wanted cost \$450. This year the price increased 12%.

Find the new price.

If each year the price increases 12%, how much will it cost in 2019?

$$y = 450(1.12)(1.12)(1.12)(1.12)(1.12) = 450(1.12)^5 = \$793.05$$

This situation is called Exponential Growth

In the year 2000 the population of a city was 210,000. Each year the population decreased by 4%. Find the population in 2001.

$$100\% - 4\% = 96\%$$
$$(210,000)(.96) = 201,600$$

In the year 2000 the population of a city was 210,000. Each year the population decreased by 4%. Find the population in 2002.

$$y = 210000(.96)(.96)$$
$$= 193,536$$

In the year 2000 the population of a city was 210,000.
Each year the population decreased by 4%.

Find the population in 2005.

$$y = 210,000(0.96)(0.96)(0.96)(0.96)(0.96) = 210,000(0.96)^5$$

This situation is called Exponential Decay

In the year 2000 the population of a city was 210,000.
Each year the population decreased by 4%.

$$100\% - 4\% = 96\% \quad b = 0.96$$

Find the population in 2020.

$$y = 210,000(0.96)^{20} = 92,821$$

Exponential Equations:

Standard Form: $y = a(b)^x$

Initial Amount $\rightarrow a$

Base which is either a growth factor or a decay factor $\rightarrow b$

Number of time periods. $\rightarrow x$

Find the base for each situation:

- Each year there is 20% more. $b = 1.2$ $100\% + 20\% = 120\%$
 $b = 1.20$
- Each day there is 5% less. $b = 0.95$ $100\% - 5\% = 95\%$
 $b = 0.95$
- Each month there is 31.6% more. $b = 1.316$ $100\% + 31.6\% = 131.6\%$
 $b = 1.316$
- Each week there is 17.3% less. $b = 0.827$ $100\% - 17.3\% = 82.7\%$
 $b = 0.827$

State the percent change each exponential equation represents and whether it's an increase or a decrease.

a) $y = 208(0.037)^x$ $\rightarrow 3.7\%$
 $\% \text{ change} = \frac{3.7}{100} \rightarrow 3.7\%$
 $96.3\% - 100 = -96.3\%$
 inc or dec? dec?

b) $y = 15.8(1.408)^x$ $\rightarrow 40.8\%$
 $\% \text{ change} = \frac{40.8}{100} \rightarrow 40.8\%$
 $40.8\% + 100 = 140.8\%$
 inc or dec? inc

Each situation is exponential: $y = a(b)^x$

What would the exponent, x , represent in each situation?

1. Each year there is 20% more. x is # of years
2. Each day there is 5% less. x is # of days
3. Each month there is 31.6% more. x is # of months
4. Each week there is 17.3% less. x is # of weeks

The value of a house in 2006 was \$156,000.
 The value of the house has been decreasing 8.4% each year.

a) Model this situation with an exponential eq.

$100\% - 8.4\% = 91.6\% \rightarrow b = 0.916$ $y = 156,000(0.916)^x$

b) Find the value of the house in 2010.

$x = 2010 - 2006 = 4$ $y = 156,000(0.916)^4 = \$109,826.34$

c) Find the value of the house in 2001.

$x = 2001 - 2006 = -5$ $y = 156,000(0.916)^{-5} = \$241,906.33$

The population of a city has been increasing 3.7% every 2 years. The population in 2005 was 142,900.

$x = \# \text{ of two year periods}$

$100\% + 3.7\% = 103.7\%$

a. Find the population in 2011.

$b = 1.037$

$x = 2011 - 2005 = 6 \div 2 = 3$

$y = 142,900(1.037)^3 = 159,356$

b. Find the population in 2016

$x = 2016 - 2005 = 11 \div 2 = 5.5$ $y = 142,900(1.037)^{5.5} = 174,508$