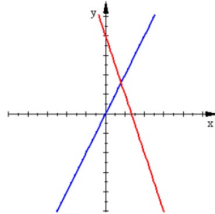


If two lines are graphed together, how many points of intersection can there be?

### 1. One

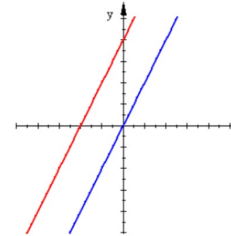
$$y = -2x + 8 \text{ and } y = 2x$$



The intersect because they have different slopes.

### 2. None

$$y = 2x \text{ and } y = 2x + 8$$

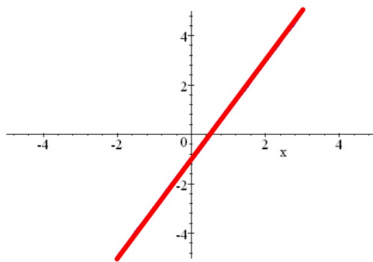


Lines are parallel

This system of equations has NO SOLUTIONS because the lines have the same slope but different y-intercepts.

### 3. Infinitely Many

$$y = 2x - 1 \text{ and } 8x - 4y = 4$$



They are the same line.

This system of equations has MANY SOLUTIONS because the lines have the same slope and same y-intercept.

If two lines are graphed together, how many points of intersection can there be?

One: If the two lines intersect

Lines have different Slopes

None: If the two lines are parallel

Lines have same slope and different y-intercepts.

Many: If they are the same line

Lines have same slope and same y-intercept.

If a system of equations contains two lines that are parallel, then the system of equations has NO solution.

If a system of equations contains two lines that are actually the same line, then the system of equations has infinitely MANY solutions.

If a system of equations contains two lines that intersect, then the system of equations has infinitely ONE solution.

How can you find the number of solutions to a system of linear equations without graphing?

Number of solutions to systems of linear equations

# of Solutions	How do you tell without graphing
One Solution:	Lines have a different slope
No solution:	Parallel Lines <ul style="list-style-type: none"> <li>• same slope</li> <li>• different y-intercept</li> </ul>
Many Solutions:	Same lines <ul style="list-style-type: none"> <li>• same slope</li> <li>• same y-intercept</li> </ul>

How many solutions does each system of linear equations have?

1.  
 $y = 2x - 7$   $m = 2$   
 $4x - 8y = 24$   
 $y = \frac{2x - 4}{-8}$   
 $m = \frac{1}{2}$   
ONE SOL  
 Slopes are different

2.  
 $y = -3x + 1$   $m = -3$   $b = 1$   
 $6x + 2y = 8$   
 $y = \frac{8 - 6x}{2} = 4 - 3x$   $m = -3$   $b = 4$   
NO SOL  
 Lines are parallel

3.  
 $y = \frac{4}{5}x + 2$   $m = \frac{4}{5}$   
 $15x + 12y = 36$   
 $y = \frac{36 - 15x}{12}$   
 Slope will be negative!  
ONE SOL  
 Slopes are different

4.  
 $y = -6x + 5$   
 $12x + 2y = 10$   
 $y = \frac{10 - 12x}{2} = 5 - 6x$   
many sol  
 These are the same line.

You can now finish:

Hwk #2: Use the sheet I've printed for you

The landscaper was paid \$100 for materials then \$8.50 per hour to finish the flower garden.

$$y = 8.50h + 100$$

Another landscaper worked the same number of hours and charged \$140 for materials then \$7.25 per hour to do another project.

$$y = 7.25h + 140$$

Find the number of hours worked if their total bill was the same.

use substitution to create on equation

$$7.25h + 140 = 8.50h + 100$$

$$-7.25h \quad -7.25h$$

$$140 = 1.25h + 100$$

$$-100 \quad -100$$

$$40 = 1.25h$$

$$32_{hrs} = h$$

## Solve this system of equations using SUBSTITUTION

$$y = 4x - 3$$

$$y = -2x + 15$$

Sol's  
(3, 9)

$$y = 4(3) - 3$$

$$= 12 - 3$$

$$y = 9$$

$$4x - 3 = -2x + 15$$

$$+2x \quad +2x$$

$$6x - 3 = +15$$

$$+3 \quad +3$$

$$6x = 18$$

$$x = 3$$

now replace x with 3 & find y

Solve.  $4x - 3(2x - 10) = 24$

$$4x - 6x + 30 = 24$$

$$-2x + 30 = 24$$

$$-30 \quad -30$$

$$-2x = -6$$

$$\div -2 \quad \div -2$$

$$x = 3$$

## Solve this system of equations using SUBSTITUTION

$$y = 4x + 1$$

$$5x + 3y = 37$$

$$y = 4(2) + 1$$

$$= 8 + 1$$

$$y = 9$$

Sol's  
(2, 9)

$$5x + 3(4x + 1) = 37$$

$$5x + 12x + 3 = 37$$

$$17x + 3 = 37$$

$$-3 \quad -3$$

$$17x = 34$$

$$\div 17 \quad \div 17$$

$$x = 2$$