

Solve this system of equations.

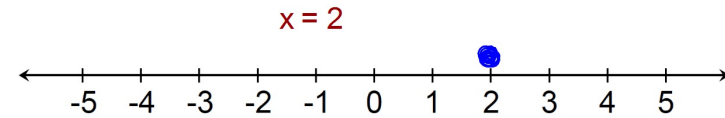
$$\begin{array}{r} 5(6x + 8y = 30) \\ 2(15x + 20y = 75) \end{array} \quad \begin{array}{r} 30x + 40y = 150 \\ 30x + 40y = 150 \\ \hline 0 = 0 \end{array}$$

These are the same line.

This is a true statement and will always be true.

many sol's

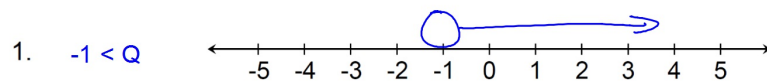
Graph this on a number line:



Number line graph of the solution to an equation:

Just a point on the number line.

Graph each inequality on a number line.



Number line graph of an inequality:

Starting point and a direction.

Is number included?

Yes: shaded circle

No: open circle

An arrow going left or right from the starting point to show ALL the solutions.

You are going to buy some CD's and/or DVD's at the store. CD's cost \$8 each and DVD's cost \$12 each. You can spend up to \$72.

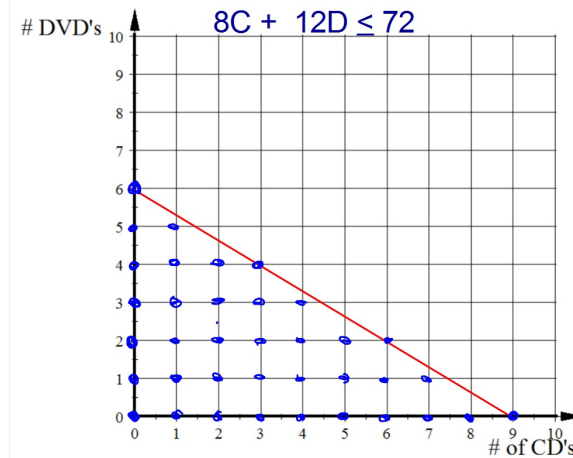
1. Model this situation with an inequality.

$$8C + 12D \leq 72$$

2. How many ways can you spend up to \$72.

You could try to use a table to find all the ways to spend up to \$72 but it would be easy to leave something out and may take a long time. There must be another way.....

C	D	\$
0	0	0
1	0	8
1	1	20
2	0	16
	⋮	
	⋮	

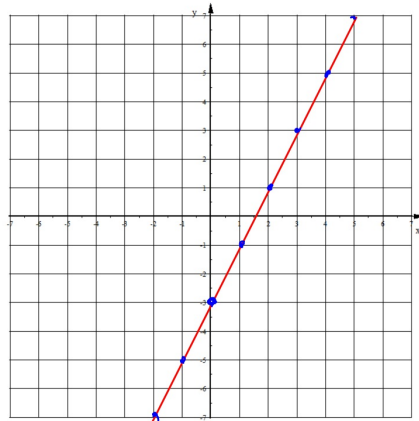


Each point on the line represents spending exactly \$72. Each point below the line represents spending less than \$72.

There are 37 ways to spend up to \$72.

Get a sheet of graph paper and a ruler. Graph this line.

$$y = 2x - 3$$



Graph of a linear EQUATION on the x-y plane:

Just a line on the x-y plane.

Actually it's an infinite number of points all lying in the same line, so close together it appears to be one continuous line.

Graph of a linear EQUATION on the x-y plane:

Just a line on the x-y plane.

Remember:

The graph of an INEQUALITY on a number line is
a **Starting Point** (open or shaded)

and a **Direction** (an arrow indicating ALL rest of the solutions).

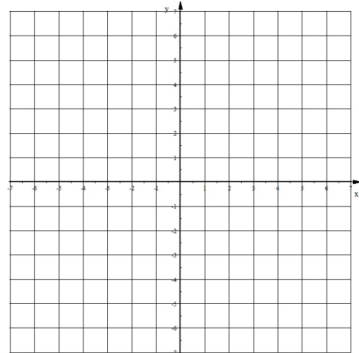
Sec 7-5: Linear Inequalities.

What would the graph of this linear INEQUALITY look like?

$$y \geq 2x - 3$$

Graphing Linear Inequalities on the x-y plane:

$$y \geq 2x - 3$$



Dashed Line
or
Solid Line

Also known as
the Boundary Line

A "Starting Line" and a direction.

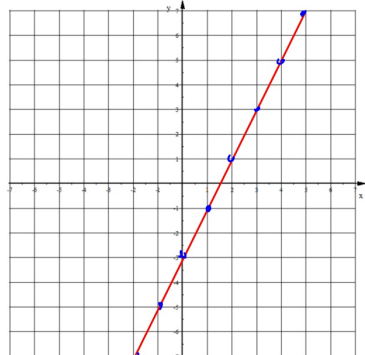
Shade the area on
one side of the line
or on the other side.

Also known as
the Solution Region

Graph of a linear INEQUALITY on the x-y plane:

A line on the graph that is either **SOLID** or **DASHED**
then the area on one side of the line is **shaded** to show
ALL the rest of the solutions.

$$y \geq 2x - 3$$



Graphing the Boundary Line

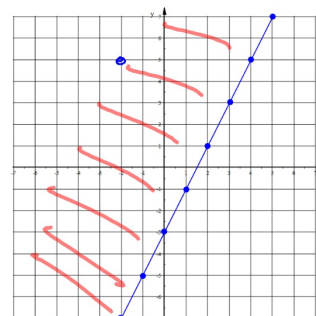
- Put points on the graph to represent the location of the line.

- Connect the points with either a

Solide Line (\leq or \geq) or Dashed Line ($<$ or $>$)

This line is solid because the inequality has the "or equal to" part.

$$y \geq 2x - 3$$



Which side of the line do you shade?

Method 1: Pick any point NOT on the line and see if it makes the inequality true.

- If Point makes inequality true: Shade that side.

- If Point makes inequality false: Shade other side.

If you Test (0,0) $0 \geq 2(0) - 3$
 $0 \geq -3$ IT IS TRUE

Method 2: Works only if inequality is in Slope-Intercept Form

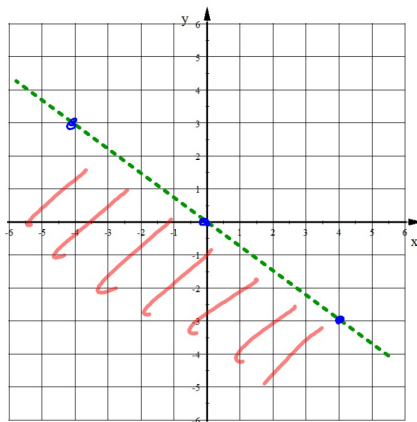
- If you say "y is greater..." shade ABOVE the line.

$y \geq \rightarrow y$ is greater...

- If you say "y is less..." shade BELOW the line.

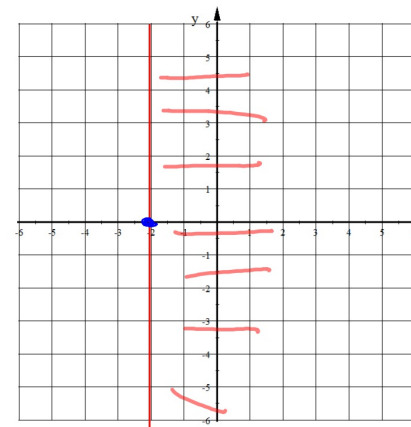
1. $y < -\frac{3}{4}x$

dashed line
 & below



2. $x \geq -2$

- VERTICAL line
 - solid line
 - to the right



Graphing linear inequalities that are in STANDARD FORM

Graph each inequality.

5. $12x - 30y \leq 60$

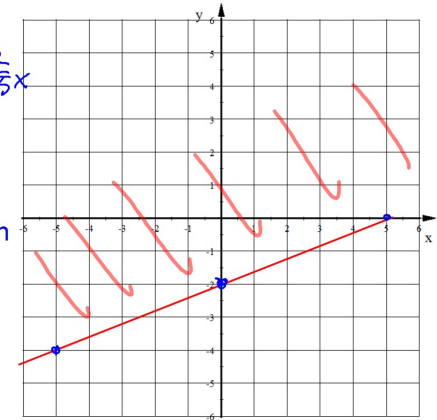
Method 1:

Step 1: Rewrite equation into
Slope-Intercept Form

$$y \geq -2 + \frac{2}{5}x$$

Step 2: Plot points and connect with
the correct kind of line

Step 3: Shade the correct side



5. $12x - 30y \leq 60$

Method 2:

Step 1: Find the x & y-intercepts &
plot them on the axes.

$$x\text{-int} = \frac{60}{12} = 5; y\text{-int} = \frac{60}{-30} = -2$$

Step 2: Connect with the correct
kind of line. **Solid Line**

Step 3: Test the origin.

If the origin "works" shade THAT side.

If the origin doesn't "work" shade
the other side of the line.

$$(0,0) \rightarrow 12(0) - 30(0) \leq 60 \\ 0 \leq 60$$

This is true, therefore,
Shade the side
that has the origin

