

Suppose you didn't know how to solve a system of equations using Substitution, how would you solve this system of equations using Elimination?

$$\begin{array}{l}
 y = 4x + 21 \\
 3x + 8y = -7
 \end{array}$$

Rewrite into $Ax + By = C$

$$\begin{array}{r}
 y = 4x + 21 \\
 -4x \quad -4x \\
 \hline
 -4x + y = 21
 \end{array}$$

Now solve using elimination

$$\begin{array}{r}
 4(3x + 8y = -7) \\
 3(-4x + y = 21) \\
 \hline
 12x + 32y = -28 \\
 -12x + 3y = 63 \\
 \hline
 35y = 35 \\
 y = 1
 \end{array}$$

Now find x:

$$\begin{array}{r}
 1 = 4x + 21 \\
 -21 \quad -21 \\
 \hline
 -20 = 4x \\
 \frac{-20}{4} = \frac{4x}{4} \\
 x = -5
 \end{array}$$

Solution: $(-5, 1)$

It would be easier to use Substitution but you can force Elimination to work if needed. That is why it's nice to know both methods.

The price of a Hot Dog is twenty three cents less than twice the cost of a bag of Chips. Two Hot Dogs and three bags of Chips cost \$9.97.

Write and solve a system of equations to find the cost for a Hot Dog and the cost for a bag of Chips.

$$\begin{array}{l}
 h = 2c - .23 \\
 2h + 3c = 9.97
 \end{array}$$

hot dogs are \$2.75 each
chips are \$1.49 each

$$\begin{array}{l}
 2(2c - .23) + 3c = 9.97 \\
 4c - .46 + 3c = 9.97 \\
 7c - .46 = 9.97 \\
 +.46 \quad +.46 \\
 7c = 10.43 \\
 \frac{7c}{7} = \frac{10.43}{7} \\
 c = \$1.49
 \end{array}$$

Find:

$$\begin{array}{l}
 h = 2(1.49) - .23 \\
 h = \$2.75
 \end{array}$$