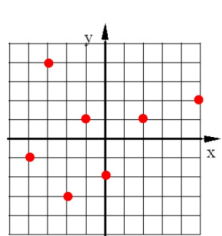


Some Relations are called Functions.

Every x value is paired with one and only one y value.

For every input there is only one output



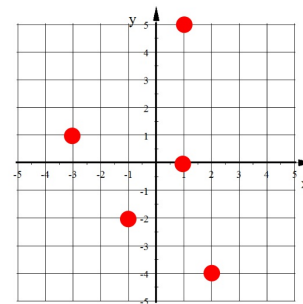
x	y
-4	-1
-2	-3
-1	1
0	-2
-2	1
5	2

Is this relation
a function?

YES

each x-value produces
only one y-value.

Is this relation a function?



x	y
-3	1
-1	-2
1	0
2	-4
1	5

NOT
A
Function

when $x=1$ two different y-values occur.
One input leads to two outputs.

Real-Life Functions and Non-Functions

You look up a word in the dictionary to get a definition:

Input (domain): A word

Output (range): Definition

Is a Dictionary a Function?

NO

A word (one input) might have more than
one definition (more than one output)

A policeman looks up a license plate number to find who it is registered to:

Input (domain): License plate number

Output (range): Who the car is registered to

Does this relationship represent a Function?

Yes

Each license plate number (one input) is registered
to only one person (one output)

The IRS looks up a Social Security Number to find out who the tax return is for:

Input (domain): Social Security Number

Output (range): Taxpayers Name

Does this relationship represent a Function?

Yes

One Social Security Number should give only one name in return.

You look up a friend's name in your address book to find a number you can call them at:

Input (domain): Friend's name

Output (range): Phone number

Does this relationship represent a Function?

NO

One name can lead to more than one phone number.

Which of the following is correct?

1. Every Relation is a Function

2. Every Function is a Relation ✓

Is this relation a function?

$(6,7)$ $(-4,3)$ $(1,-5)$ $(6,2)$

NO

When $x=6$ two different y -values result.
For one input there are two outputs.

Is this relation a function?

$(4, 0)$ $(2, 1)$ $(-8, 1)$ $(9, 5)$

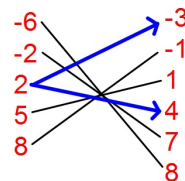
no x-value repeats so every input has only one output.

Yes, this represents a function

Using a Mapping Diagram to tell if a relation is a function.

$(5, 1)$, $(-2, 7)$, $(2, -3)$, $(8, -1)$, $(2, 4)$, $(-6, 8)$

Domain: Range:



If any domain value has more than one line coming from it then the relation is NOT a function

This would indicate that the same input (x) produces more than one output (y)

Is the following relation a function?

$(-4, 7)$, $(3, -9)$, $(-8, 2)$, $(5, 7)$, $(2, 4)$

Yes

No x-value repeats.

Is the following relation a function?

x	y
8	4
1	-9
-3	2
5	4

No x-value repeats.

Yes

Is the following relation a function?

x	y
-9	1
4	0
-2	-7
4	8

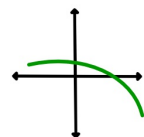
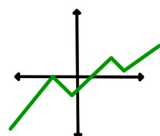
no

When x is 4 two different y-values are possible.

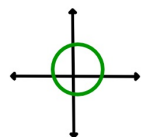
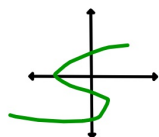
In other words, for one input there are two outputs.

How can you tell if a graph represents a function?

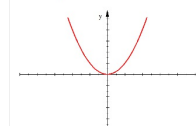
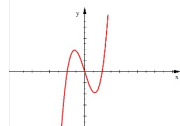
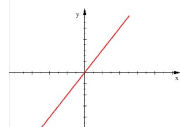
Is a Function



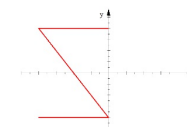
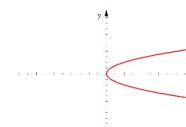
Is NOT a Function



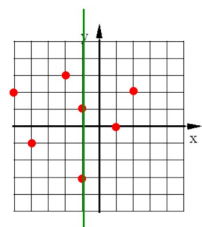
Is a Function



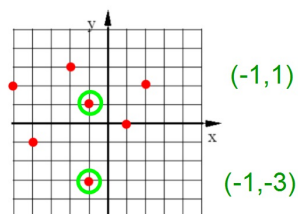
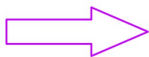
Is NOT a Function



Vertical Line Test: If any vertical line can touch the graph more than once the relation is not a function.



Is this graph a function?



When two points line up vertically they have the same x-coordinate.

8. Is each of these relations a function?

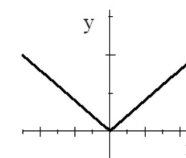
a)

X	Y
-2	4
3	1
7	-6
4	1

Yes

No x-values repeat

b)



Yes

No vertical line touches the graph more than once.

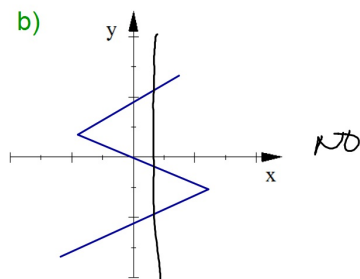
Is each of these a function?

a)

X	Y
-7	4
-2	-3
11	1
-7	6
8	-5

NO

b)



How do you say $f(x)$?

"f of x"

f is the function name

x is the Independent variable (the input)

$f(x)$ doesn't mean f times x

What is another way to write $f(x) = 7x - 8$?

$$y = 7x - 8$$

$f(x) =$ is just another way to write $y =$

If $f(x) = -2x + 3$ what does $f(5)$ mean?

evaluate the function f
when $x=5$.

Find $f(5)$.

$$\begin{aligned} f(5) &= -2(5) + 3 \\ &= -10 + 3 \\ f(5) &= -7 \end{aligned}$$

Use this function:

$$g(k) = 4k - 3$$

Find $g(9)$

$$\begin{aligned} g(9) &= 4(9) - 3 \\ &= 36 - 3 \\ g(9) &= 33 \end{aligned}$$

Find $g(-7)$

$$\begin{aligned} g(-7) &= 4(-7) - 3 \\ &= -28 - 3 \\ g(-7) &= -31 \end{aligned}$$

Use this function: $w(b) = -2b^2 + 5$

Find $w(3)$

$$\begin{aligned} -2(3)^2 + 5 \\ -18 + 5 \\ -13 \end{aligned}$$

$$w(3) = -13$$

Find $w(-5)$

$$\begin{aligned} -2(-5)^2 + 5 \\ -50 + 5 \\ -45 \end{aligned}$$

$$w(-5) = -45$$

Use this function: $m(y) = y^2 - 3y + 1$

Find $m(-2)$

$$\begin{aligned} m(-2) &= (-2)^2 - 3(-2) + 1 \\ &= 4 + 6 + 1 \end{aligned}$$

$$m(-2) = 11$$

Find $m(4)$

$$\begin{aligned} &= 4^2 - 3(4) + 1 \\ &= 16 - 12 + 1 \\ &= 4 + 1 \end{aligned}$$

$$m(4) = 5$$

13. If $f(x) = x^2 + 3x$

find the range for this given domain: Domain: $\{-4, 0, 2\}$

Find each of the following:

$$f(-4) = (-4)^2 + 3(-4) = 4$$

$$f(0) = 0^2 + 3(0) = 0$$

$$f(2) = (2)^2 + 3(2) = 10$$

Range:

$$\{0, 4, 10\}$$

Given the functions: $g(x) = -10x - 1$

and $k(r) = -2r^2 + 5$

3. Find x if $g(x) = 29$

$$29 = -10x - 1$$

$$\begin{aligned} 30 &= -10x \\ -10 &= -10 \end{aligned}$$

$$x = -3$$

You can now finish Hwk #19

Sec 5-2

pages 244-245

problems 2, 4, 24, 28-30, 32, 38-41, 44