

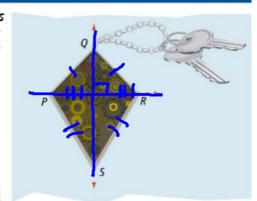
2) Do "Critique and Explain", page 137 in your student companion.

🌢) CRITIQUE & EXPLAIN

Manuel draws a diagram of kite PQRS with QS as the line of symmetry over a design of a kite-shaped key fob. He makes a list of conclusions based on the diagram.

PR ⊥ QS $\overline{QP} \cong \overline{QR}$ $\overline{SP} \cong \overline{SR}$

- \overline{PR} bisects \overline{QS} . ΔPQR is arrequilateral
- triangle.
- ΔPSR is an isosceles triangle.



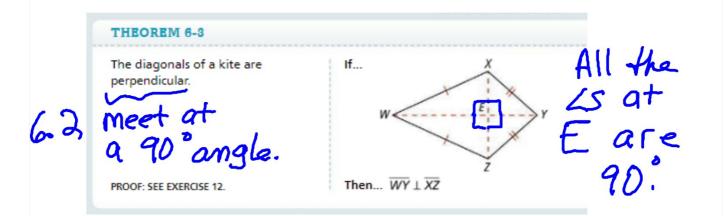
A. Which of Manuel's conclusions do you agree with? Which do you disagree with? Explain.

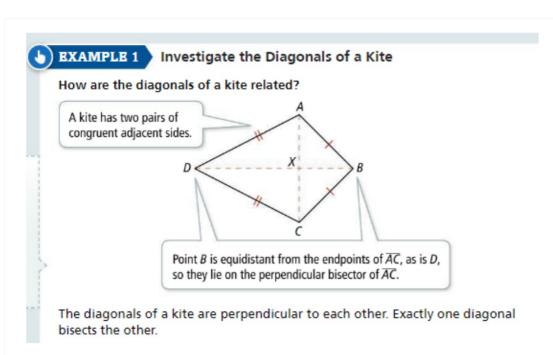
B. Use Structure What other conclusions are supported by the OS bisectoff

Habits of Mind

What theorems or definitions support your conclusions?

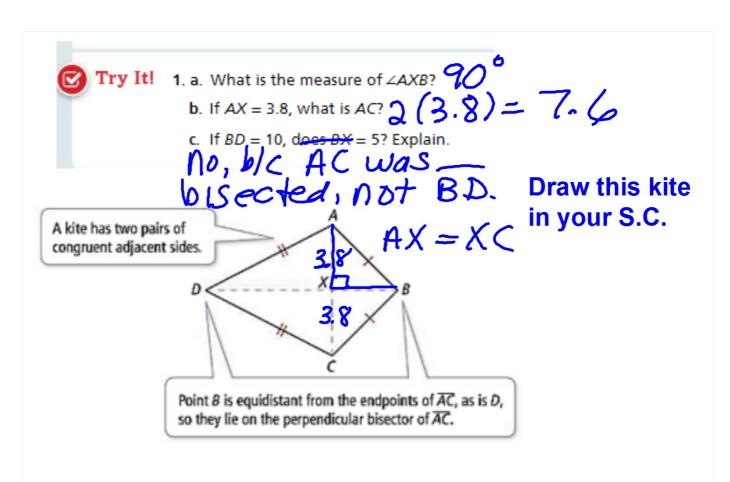
Isosceles As.





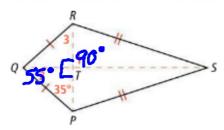
Put in your s.c. next to TI 1:

One of the diagonals gets bisected, or cut In half.



EXAMPLE 2 Use the Diagonals of a Kite

Quadrilateral PQRS is a kite with diagonals \overline{QS} and \overline{PR} .



A. What is m∠1?

The diagonals of a kite are perpendicular, so $m \angle 1 = 90^{\circ}$.

B. What is m∠2?

The sum of the angles of $\triangle PQT$ is 180°.

$$m\angle 2 + 35^{\circ} + 90^{\circ} = 180^{\circ}$$

 $m\angle 2 = 55^{\circ}$

C. What is $m \angle 3$?

Since $\triangle PQR$ is an isosceles triangle, $\angle 3 \cong \angle QPT$.

So,
$$m \angle 3 = 35^{\circ}$$
.

Draw this in you SC or take the examples sheet.

COMMON ERROR

You may incorrectly assume angles are congruent just from their appearance. Always check that you can prove congruence first.

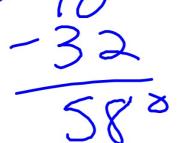


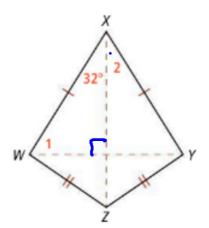
Try It! 2. Quadrilateral WXYZ is a kite.

a. What is m∠1?

b. What is $m \angle 2$? \nearrow ?







Habits of Mind
What ideas about triangles have you learned that could be useful in investigating kites?

THEOREM 6-4

In an isosceles trapezoid, each pair of base angles is congruent.

PROOF: SEE EXERCISE 13.

If... B C A D

Then... $\angle BAD \cong \angle CDA$, $\angle ABC \cong \angle DCB$

THEOREM 6-5

The diagonals of an isosceles trapezoid are congruent.

PROOF: SEE EXERCISE 18.

If... B C

Then... $\overline{AC} \cong \overline{DB}$

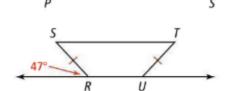
X there b) W	cause an isosceles trapezoid has 2 congruent sides, must be congruent hich angles do you think are congruent in the figure?
c) What kind of angles are $\angle X$ and $\angle W$?	Is there another pair of similar type angles?
d) Draw in the diagonals of the figure. Name them: and What do you think is true about these diagonals? Can we verify that? $e) \text{ If } m \angle W = 70^{\circ}, \text{ find the measures of the remaining angles.}$	

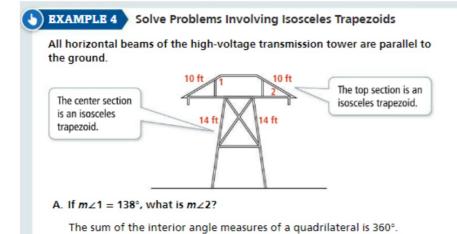


Try It! 3. a. Given isosceles trapezoid PQRS, what are m∠P, m∠Q,

and $m \angle S$?

b. Given $\overline{\mathit{ST}} \parallel \overline{\mathit{RU}}$, what is the measure of ∠TUR?





 $m\angle 1 + m\angle 1 + m\angle 2 + m\angle 2 = 360^{\circ}$ $138^{\circ} + 138^{\circ} + 2(m\angle 2) = 360^{\circ}$

The measure of $\angle 2$ is 42°.

 $276^{\circ} + 2(m \angle 2) = 360^{\circ}$

 $2(m\angle 2) = 84^{\circ}$ $m\angle 2 = 42^{\circ}$

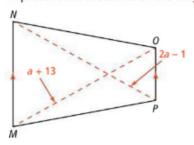
The base angles are congruent.

MAKE SENSE AND PERSEVERE

What other strategy might you use to solve this problem?



Try It! 4. Given isosceles trapezoid MNOP where the given expressions represent the measures of the diagonals, what is the value of a?



Habits of Mind

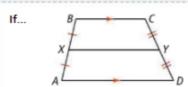
What is the minimum information you need to find the measures of all 4 interior angles in an isosceles trapezoid?



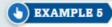
6.2

In a trapezoid, the midsegment is parallel to the bases, and the length of the midsegment is half the sum of the lengths of the bases.

PROOF: SEE LESSON 9-2.



Then... $\overline{XY} \parallel \overline{AD}$, $\overline{XY} \parallel \overline{BC}$, and $\overline{XY} = \frac{1}{2} (AD + BC)$



EXAMPLE 5 Apply the Trapezoid Midsegment Theorem

Paxton makes trapezoidal handbags for her friends. She stiches decorative trim along the top, middle, and bottom on both sides of the handbags. How much trim does she need for three handbags? Explain.

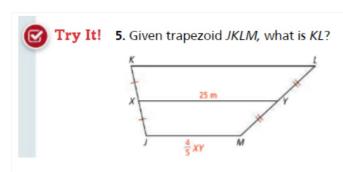


Formulate < The top and bottom sides of the handbag are the bases of a trapezoid. The left and right sides are the legs. Since the middle segment divides both legs in half, it is the midsegment of the trapezoid. The midsegment of a trapezoid is the segment that connects the midpoints of the legs. Let x represent the length of the midsegment in inches. Step 1 Find the value of x. Compute < Apply the Trapezoid Midsegment Theorem with the base lengths 6 and 9. Step 2 Find the amount of trim that she needs.

First, find the amount for one side.

Then, multiply by 2 for the number of sides per handbag and by 3 for the number of handbags.

Interpret < Paxton needs



Habits of Mind

What information is represented in the diagram but not given in words?



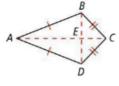
CONCEPT SUMMARY Kites and Trapezoids



WORDS Kites

A kite is a quadrilateral with two pairs of adjacent sides congruent and no pairs of opposite sides congruent. Exactly one diagonal is a perpendicular bisector of the other.

DIAGRAMS Quadrilateral ABCD is a kite.

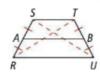


 $\overline{AC} \perp \overline{BD}$ BE = ED

Trapezoids

A trapezoid is a quadrilateral with exactly one pair of parallel sides. The length of the midsegment is the average of the lengths of the two bases. A trapezoid with congruent legs is an isosceles trapezoid that has congruent base angles and congruent diagonals.

Quadrilateral RSTU is an isosceles trapezoid.



$$\overline{SU} \cong \overline{RT}$$

$$AB = \frac{1}{2}(ST + RU)$$

$$\overline{AB} \parallel \overline{ST} \parallel \overline{RU}$$

 $m \angle S = m \angle T$

$$m \angle R = m \angle U$$

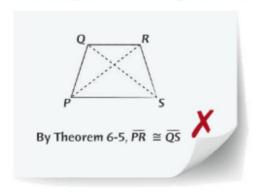
In your Book

Read Concept Summary and #1-11 page 259 (page 140 in your student companion). Tomorrow's assignment is page 260 #14, 16, 17, 19, 20, 22 (1760 yd = 1 mile), 24, 25, 26A



Do You UNDERSTAND?

- 1. P ESSENTIAL QUESTION How are diagonals and angle measures related in kites and trapezoids?
- 2. Error Analysis What is Reagan's error?



- Vocabulary If XY is the midsegment of a trapezoid, what must be true about point X and point Y?
- Construct Arguments Emaan says every kite is composed of 4 right triangles. Is he correct? Explain.

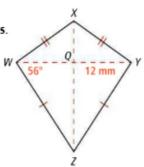
Do You KNOW HOW?

For Exercises 5–7, use kite WXYZ to find the measures.

5. m∠XQY

6. m∠YZQ

7. WY

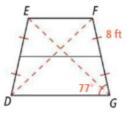


For Exercises 8–10, use trapezoid **DEFG** with **EG** = 21 ft and $m \angle DGF = 77^{\circ}$ to find each measure.

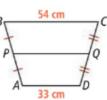
8. ED

9. DF

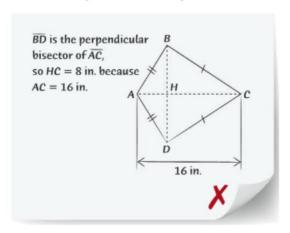
10. m∠DEF



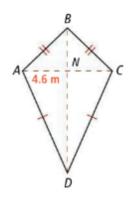
11. What is the length of \overline{PQ} ?



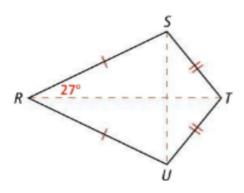
14. Error Analysis What is Emery's error?



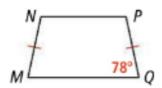
16. Given kite ABCD, in which AN = 4.6 m, what is AC? SEE EXAMPLE 1



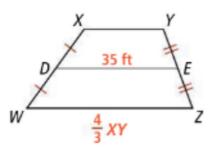
17. Given kite RSTU, what is m∠RUS? SEE EXAMPLE 2



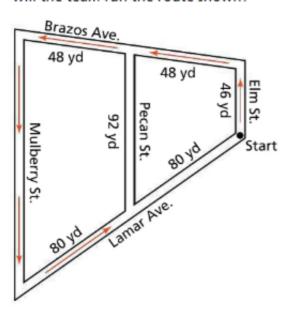
Given trapezoid MNPQ, what is m∠MNP?
 SEE EXAMPLE 4



20. Given trapezoid WXYZ, what is XY? SEE EXAMPLE 5

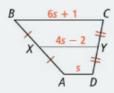


22. Reason Coach Murphy uses the map to plan a 2-mile run for the track team. How many times will the team run the route shown? 1760 yd = 1 mile

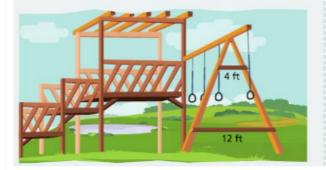




25. SAT/ACT Given trapezoid ABCD, what is the length of XY?



- (A) $3\frac{3}{5}$
- (B) $4\frac{2}{3}$
- © 5
- © 11 © 18
- 26. Performance Task Cindy is a member of a volunteer group that built the play structure shown.



Part A Cindy wants to add three more trapezoid boards evenly spaced between the bottom and top boards of the triangular frame. Based on the average lengths of the top and bottom boards shown, what will be the average lengths of each of the three additional boards? Explain.