

5-7**Study Guide and Intervention****Least Common Multiple**

A **multiple** of a number is the product of that number and any whole number. The least nonzero multiple of two or more numbers is the **least common multiple (LCM)** of the numbers.

EXAMPLE 1 Find the LCM of 15 and 20 by listing multiples.

List the multiples.

multiples of 15: 15, 30, 45, **60**, 75, 90, 105, **120**, ...

multiples of 20: 20, 40, **60**, 80, 100, **120**, 140, ...

Notice that 60, 120, ..., are common multiples. So, the LCM of 15 and 20 is 60.

EXAMPLE 2 Find the LCM of 8 and 12 using prime factors.

Method 1 Write the prime factorization.

$$8 = 2 \times 2 \times 2 = 2^3$$

$$12 = 2 \times 2 \times 3 = 2^2 \times 3$$

The prime factors of 8 and 12 are 2 and 3. Multiply the greatest power of both 2 and 3.

The LCM of 8 and 12 is $2^3 \times 3$, or 24.

Method 2 Divide by prime numbers.

$$\begin{array}{r} 2 \quad 3 \\ 2 \overline{)4} \quad 6 \\ 2 \overline{)8} \quad 12 \end{array} \quad \leftarrow \text{Start here.}$$

Start dividing by prime factors until both numbers cannot be divided by the same divisor. Then multiply the divisors and quotients to get the LCM.

EXERCISES

Find the LCM of each set of numbers.

1. 4, 6

2. 6, 9

3. 5, 9

4. 8, 10

5. 12, 15

6. 15, 21

7. 4, 15

8. 8, 20

9. 8, 16

10. 6, 14

11. 12, 20

12. 9, 12

13. 14, 21

14. 6, 15

15. 4, 6, 8

16. 3, 5, 6