

Standard Deviation

Standard Deviation is a measure of the dispersion of a set of data from its mean. Standard deviation tells you how spread out the data values are from the mean and is denoted by the symbol σ

Types of Standard Deviation

- **If the standard deviation is 0, then the data has no spread.**
- **If the standard deviation is small, then the data is close to the mean.**
- **If the standard deviation is large, then the data is more spread out from the mean.**

How to Calculate a Sample Standard Deviation

- Calculate the mean \bar{x}
- Calculate each data value's deviation from the mean by finding $x - \bar{x}$ for each data value of x
- Find $(x - \bar{x})^2$, the square of each deviation ^{sum}
- Find the mean of the squared deviation $\frac{\sum (x - \bar{x})^2}{n - 1}$
- Take the square root of the mean of the squared deviation

$$\sqrt{\frac{\sum (x - \bar{x})^2}{n - 1}}$$

1) A data set has 4 numbers {2, 5, 6, 7}. Find the standard deviation of the data.

n = # of terms or data points

$$\bar{x} = \frac{2+5+6+7}{4}$$

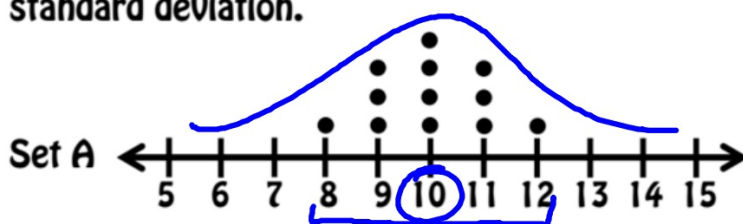
$$\bar{x} = 5$$

Data x	Data - Mean $x - \bar{x}$	(Data - Mean) ² $(x - \bar{x})^2$
2	2-5 = -3	(-3) ² = 9
5	5-5 = 0	(0) ² = 0
6	6-5 = 1	(1) ² = 1
7	7-5 = 2	(2) ² = 4

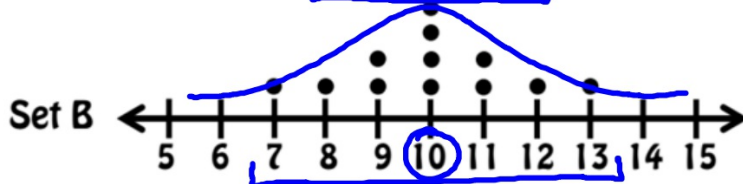
$$\frac{\sum (x - \bar{x})^2}{n-1} = \frac{9+0+1+4}{4-1} = \frac{14}{3}$$

$$\sigma = \sqrt{\frac{14}{3}} = \boxed{2.16}$$

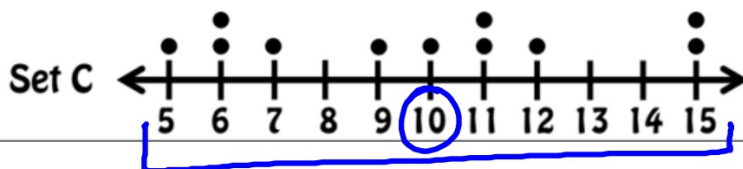
2) The mean of each set is 10. The standard deviations of the sets are 1.13, 1.65, and 3.49. Match each data set with its standard deviation.



$$\sigma = 1.13$$



$$\sigma = 1.65$$



$$\sigma = 3.49$$