

P.6 : Factoring and Solving Polynomials

1) a. Graph $P(x)$ and find the roots (x-int, zeros)

$$P(x) = x^3 + 4x^2 - 11x - 30$$

$$x\text{-int} : -5, -2, 3$$
$$x = -5 \quad x = -2 \quad x = 3$$

b. Write $P(x)$ in factored form.

$$P(x) = (x+5)(x+2)(x-3)$$

2) Is $(x + 2)$ a factor of $P(x)$?

How do we check?

Yes

$$P(-2) = (-2)^3 + 4(-2)^2 - 11(-2) - 30$$

$$P(-2) = 0$$

3) How do we find the other factors of $P(x)$?

a. Divide

b. Write your answer as (divisor)(quotient)

c. Factor (GCF, x-box, special cases, quadratic formula)

$$\begin{array}{r} x^2 + 2x - 15 \\ \hline a) x+2 \sqrt{x^3 + 4x^2 - 11x - 30} \\ - (x^3 + 2x^2) \downarrow \\ - 2x^2 - 11x \\ - (2x^2 + 4x) \\ - 15x - 30 \\ - (-15x - 30) \\ \hline 0 \end{array}$$

b)

$$P(x) = (x+2)(x^2 + 2x - 15)^0$$

$a \cdot c$ $a=1$ $b=2$ $c=-15$

$$\begin{array}{c} -15 \\ \cancel{-3} \cdot \cancel{5} \\ + \\ \cancel{2} \\ \textcircled{c} \end{array} \quad (x-3)(x+5)$$

$$P(x) = (x+2)(x-3)(x+5)$$

4) Sketch the graph using the end behavior and the x-int.

