

- Objective 1: I can write quadratics in different forms.

Assignment # \_\_\_\_\_

Use the following situation for questions below. The formula for the height of a thrown object can be approximated by the formula:  $h(t) = -16t^2 + v_0t + h_0$  where  $h(t)$  is the height of the object in feet after  $t$  seconds,  $v_0$  is the initial velocity in feet/second and  $h_0$  is the initial height in feet. Suppose you throw a football at an initial velocity of 32 ft/s from a cliff that is 48 feet high.

- a) Write a quadratic function to model the height of the football after  $t$  seconds.

$$h(t) = -16t^2 + 32t + 48$$

- b) Write the function in factored form.

$$h(t) = -16(t^2 - 2t - 3)$$

$$a=1 \quad b=-2 \quad c=-3$$

$$\begin{array}{r} 1 \quad -3 \\ \times -2 \quad -3 \\ \hline \end{array}$$

$$h(t) = -16(t+1)(t-3)$$

- c) What are the zeros of the function? What does that tell us about the football?

$$-16(t+1)(t-3) = 0$$

$$t+1=0$$

$$\boxed{t=-1}$$

$$t-3=0$$

$$\boxed{t=3}$$

time when the ball hits the ground  
time before the ball was thrown

- d) What is the vertex of the function? What does that tell us about the football?

$$h(t) = -16t^2 + 32t + 48$$

$$\text{vertex} \quad -\frac{b}{2a} = -\frac{32}{2(-16)} = -\frac{32}{-32} = 1$$

$$\begin{aligned} -16(1)^2 + 32(1) + 48 \\ = -16 + 32 + 48 \\ = 64 \end{aligned}$$

$$\text{vertex } (1, 64)$$

the vertex is the maximum point. At 1 second, the ball reaches its maximum height of 64 ft.

- e) Write the function in vertex form.

$$h(t) = a(x-h)^2 + k$$

$$h(t) = -16(x-1)^2 + 64$$