

NAME: \_\_\_\_\_

**Part A: Exponential Story Problems**

Write an exponential function for each situation. **Show your work for c and d on a separate sheet of paper.**

<p>1) Mary is investing in an account. She puts \$2000 in an account that <u>earns</u> 4% each year.</p> <p>a) Is this <u>growth</u> or decay? Why? <i>growth "earns"</i></p> <p>b) Write a function to model the value of the account after x years. <math>a = 2000</math> <math>A(t) = 2000(1.04)^t</math> <math>r = 0.04</math> <math>b = 1 + 0.04 = 1.04</math></p> <p>c) Find the value of the account after 5 years. <math>t = 5 \rightarrow 2000(1.04)^5 = 2433.31</math></p>	<p>2) Samantha bought a car for \$23,000. The car <u>depreciates</u> in value by 12% each year.</p> <p>a) Is this growth or <u>decay</u>? Why?</p> <p>b) Write a function to model the value of the car after x years. <math>a = 23000</math> <math>r = 12\% = 0.12</math> <math>b = 1 - 0.12 = 0.88</math> <math>A(t) = 23000(0.88)^t</math></p> <p>c) Find the value of the car after 2 years. <math>17811.20</math></p>
<p>3) Bilal bought a house for \$120,000. It <u>appreciates</u> in value by 3.2% each year.</p> <p>a) Is this <u>growth</u> or decay? Why? <i>appreciates</i></p> <p>b) Write a function to model the value of the house after x years. <math>a = 120000</math> <math>A(t) = 120000(1.032)^t</math> <math>b = 1 + 0.032 = 1.032</math></p> <p>c) Find the value of the house after 5 years. <math>t = 5 \rightarrow 120000(1.032)^5 = 140469</math></p>	<p>4) The small town of Rosea has a population of 45,000 people. It <u>grows</u> at a rate of 2.3% per year.</p> <p>a) Is this <u>growth</u> or decay? Why?</p> <p>b) Write a function to model the population of the town after x years. <math>a = 45000</math> <math>r = 2.3\% \Rightarrow 0.023</math> <math>b = 1 + 0.023 = 1.023</math> <math>45000(1.023)^t</math></p> <p>c) Find the population after 20 years. <math>45000(1.023)^{20} = 70912.80</math> people</p>
<p>5) An initial dose of 20 mg of medication <u>decays</u> at a rate of 40% each hour.</p> <p>a) Is this growth or <u>decay</u>? Why?</p> <p>b) Write a function to model the amount of medication in x hours. <math>a = 20</math> <math>A(t) = 20(0.6)^t</math> <math>r = 0.4</math> <math>b = 1 - 0.4 = 0.6</math></p> <p>c) Find the amount of medication in 3 hours. <math>t = 3 \rightarrow 20(0.6)^3 = 4.32</math></p> <p>d) In how many hours will there be less than 1 mg left in the blood stream? <math>t = 6</math> hours</p> <p><i>Graph <math>\rightarrow</math> look at TABLE for y less than 1</i></p>	<p>6) Cancer cells in a particular type of tumor <u>increase</u> at a rate of 12% each <u>week</u>. Suppose you start with 1 cancer cell.</p> <p>a) Is this <u>growth</u> or decay? Why?</p> <p>b) Write a function to model the number of cancer cells after x weeks. <math>a(t) = 1(1.12)^t</math></p> <p>c) Find the number of cells after 1 year. = 52 weeks = t <math>1(1.12)^{52} = 362.52</math> cells</p> <p>d) Find how many weeks it will take for there to be more than 100,000 cancer cells. <math>t = 102</math> weeks <math>100000 = 1(1.12)^t \rightarrow</math> look at table.</p>
<p>7) Sarah decided for her New Year's Resolution that she was going to start exercising and started with 10 minutes. She said "I'll do <u>10% more each day</u>."</p> <p>a) Is this <u>growth</u> or decay? Why?</p> <p>b) Write a function to model the # of minutes after x days. <math>a = 10</math> minutes <math>r = 10\% = 0.10</math> <math>b = 1 + 0.10 = 1.10</math> <math>10(1.10)^t</math></p> <p>c) Find the # of minutes she is exercising after a week. <math>t = 7</math> days <math>10(1.10)^7 = 19.4872</math> min</p> <p>d) Find how many days it will take for her to be exercising 24 hours a day! <math>t = 53</math> days <i>minutes <math>\rightarrow 24 \times 60 = 1440</math> minutes</i></p> <p><i>(look for MINUTES in table not hours)</i></p>	<p>8) Leila buys some office furniture for \$5000 for her business. A depreciation table shows that it <u>depreciates</u> in value by 9% each year.</p> <p>a) Is this growth or <u>decay</u>? Why?</p> <p>b) Write a function to model the value of the furniture after x years. <math>5000(0.91)^t</math> <math>b = 1 - 0.09</math></p> <p>c) Find the value of the furniture after 3 years. <math>5000(0.91)^3 = 3767.86</math></p> <p>d) Find how many years it will take for the furniture to be worth \$1000. <math>t = 17</math> years</p>



NAME:

HOUR:

DATE:

**PART B: Determining Growth and Decay Factors**

Use the given information to determine the rate of growth or decay,  $r$ , and the growth/decay factor,  $b$ . For the story problems, define the variables  $x$  and  $y$  and write an equation.  $r = b - 1$   $b = 1 + r$

	Growth or decay?	Rate ( $r$ )	Factor ( $b$ )	Equation?
1. $y = 6(1.3)^x$	Growth	$r = 0.3 = 30\%$	$b = 1.3$	
2. $y = 13,000(0.84)^x$	Decay	$r = -0.16 = -16\%$	$b = 0.84$	
3. $y = 98(1.06)^x$	Growth	$r = 0.06 = 6\%$	$b = 1.06$	
4. $y = 0.2(3)^x$	Growth	$r = 2 = 200\%$	$b = 3$	
5. A \$15,000 car depreciates at a rate of 8% per year. $x =$ <u>years</u> $y =$ <u>car value</u>	Decay	$r = -0.08$	$b = 1 - 0.08$ $b = 0.92$	$15000(0.92)^x$
6. Francois bought a Monet painting for \$100,000. It appreciates in value by 8% each year. $x =$ <u>years</u> $y =$ <u>painting value</u>	Growth	$r = 0.08$	$b = 1 + 0.08$ $b = 1.08$	$100000(1.08)^x$
7. The population of a town of 30,000 increases at a rate of 3% per year. Write an equation to model the situation. $x =$ <u>years</u> $y =$ <u>population</u>	Growth	$r = 0.03$	$b = 1 + 0.03$ $b = 1.03$	$30000(1.03)^x$
8. Frank turns into a Zombie and infects other people at a rate of 100% each week (every zombie infects one other person per week) $x =$ <u>weeks</u> $y =$ <u>Zombies</u>	Growth	$r = 100\%$ $r = 1$	$b = 1 + 1$ $b = 2$	$1(2)^x$
9. Shenja bought a computer for \$3000. It depreciates at a rate of 22% each year. $x =$ <u>years</u> $y =$ <u>computer value</u>	Decay	$r = -0.22$	$b = 1 - 0.22$ $b = 0.78$	$3000(0.78)^x$
10. A bird population starts at 45 in a particular region and is increasing at a rate of 5% each year. $x =$ <u>years</u> $y =$ <u>bird population</u>	Growth	$r = 0.05$	$b = 1 + 0.05$ $b = 1.05$	$45(1.05)^x$