

4.22.15

. What is the difference between theoretical and experimental probability?

Theoretical: Calculating using math formulas.

Experimental: Using an active experiment to determine probability.

. What is the difference between a permutation and a combination?

Combination: Order does not matter.

Permutation: Order matters.

Dependent Events When the outcome of one event affects the outcome of a second event.

Independent Events When the outcome of one event does not affect the second event.

Example 1) Classify and explain each set of events as dependent or independent:

Roll a number cube. Then toss a coin.

Independent

Spinning a 4 and then a 4 again on a spinner.

Independent

Selecting two Aces from a deck of cards when the 1st one is not replaced

Dependent

Your Turn 1) Classify and explain each set of events as dependent or independent:

*Selecting two Aces from a deck of cards when the 1st is replaced

independent

*Flipping a coin twice and it is heads both times.

Independent

*Select a marble from a bag that contains marbles of 2 colors. Put the marble aside and then select another marble.

Dependent

Probability of A and B given the two events are independent:

$$P(A) \cdot P(B)$$

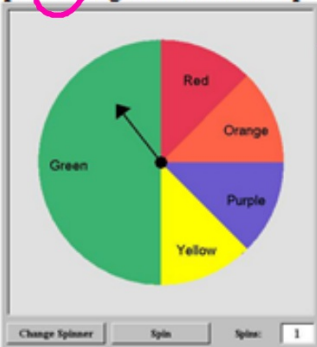
Example 1) If $P(A) = \frac{3}{4}$ and $P(B) = \frac{1}{3}$ then

$$P(A \text{ and } B) = \frac{P(A) \cdot P(B)}{= \frac{3}{4} \cdot \frac{1}{3} = \frac{3}{12} = \frac{1}{4}}$$

Your Turn 1) If $P(A) = \frac{1}{4}$ and $P(B) = \frac{2}{5}$ then

$$P(A \text{ and } B) = \frac{P(A) \cdot P(B)}{= \frac{1}{4} \cdot \frac{2}{5} = \frac{2}{20} = \frac{1}{10}}$$

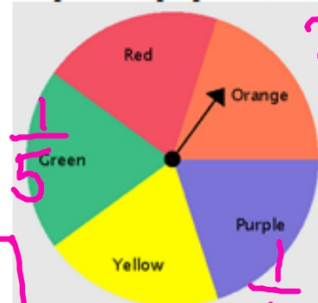
Example 2) Find the probability of getting a red on the 1st spin and a green on the 2nd spin.



$$P(R \text{ and } G) = \frac{1}{8} \cdot \frac{1}{2}$$

$$P(R \text{ and } G) = \frac{1}{16}$$

Your Turn 2) Find the probability of getting a green on the 1st spin and a purple on the 2nd spin.



$$P(G \text{ and } P)$$

$$\frac{1}{5} \cdot \frac{1}{5}$$

$$\frac{1}{5} P(G \text{ and } P) = \frac{1}{25}$$

$$P(G) = \frac{1}{2} \quad P(R) = \frac{1}{8}$$

Mutually Exclusive (M.E): Two events that cannot occur at the same time.

Not Mutually Exclusive (N.M.E): Two events that can occur at the same time.

Probability of A or B

Mutually Exclusive: $P(A \text{ or } B) = P(A) + P(B)$

Not Mutually Exclusive: $P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B)$

Example 3) A drink company applies one label to each bottle cap: "free drink", "free meal" or "try again". A bottle cap has a $\frac{1}{10}$ probability of being labeled "free drink", a $\frac{1}{25}$ probability of being labeled "free meal", and a $\frac{43}{50}$ probability of being labeled "try again".

- a) Are the events free drink and free meal mutually exclusive and why?

The events are mutually exclusive because they can't happen at the same time.

- b) What is the probability that a bottle cap is labeled free drink or free meal?

$$P(D) + P(M) = \frac{1}{10} + \frac{1}{25} = \frac{5}{50} + \frac{2}{50} = \frac{7}{50}$$

Your Turn 3)

- a) Are the events free drink and try again mutually exclusive and why?

The events are mutually exclusive because they can't happen at the same time.

- b) What is the probability that a bottle cap is labeled free drink or free try again?

$$P(D) + P(T) = \frac{1}{10} + \frac{43}{50} =$$

$$\frac{5}{50} + \frac{43}{50} = \left(\frac{48}{50} \right) = \frac{24}{25}$$

Example 4) For the set of events state whether they are mutually exclusive and then find the probability.

Rolling a 5 or an odd on a # cube:

Not mutually exclusive, they can happen at the same time.

$$P(5 \text{ or odd}) = \frac{1}{2}$$

Your Turn 4) For the set of events state whether they are mutually exclusive and then find the probability.

Rolling a prime or an odd on a # cube:

$$\begin{aligned} \Rightarrow P(5) &= \frac{1}{6} & P(5) + P(\text{odd}) - P(\text{both}) \\ P(\text{Odd}) &= \frac{3}{6} & \frac{1}{6} + \frac{3}{6} - \frac{1}{6} \\ P(5 \text{ and odd}) &= \frac{1}{6} & \frac{3}{6} = \boxed{\frac{1}{2}} \end{aligned}$$

$$\begin{array}{l} P(5) \quad 5 \\ P(\text{odd}) \quad 1 \quad 3 \quad \cancel{5} \end{array} \quad \frac{3}{6} = \frac{1}{2}$$