

Difference of Squares $a^2 - b^2 = (a + b)(a - b)$	$4x^2 - 3$	
Factor By Grouping	$x^3 - 4x^2 - 9x + 36$	
Sum/Difference of Cubes	$64x^3 + 1$ $64x^3 - 1$	$a = 4x$ $b = 1$

$$a^3 - b^3 = (a - b)(a^2 + ab + b^2) \quad (4x - 1)(16x^2 + 4x + 1)$$

EX #1: What are the real or imaginary solutions of each equation?

$$i = \sqrt{-1}$$

$$i^2 = -1$$

Factored Form

A. $(x^2 - 1)(x^2 + 4) = 0$

$$x^2 - 1 = 0 \quad x^2 + 4 = 0$$

$$\underline{x^2 = 1} \quad \underline{\sqrt{x^2 = \sqrt{-4}}}$$

$$x = \sqrt{-1} \cdot \sqrt{4}$$

$$x = \pm 2i$$

$$\boxed{x = 1 \quad x = -1 \quad x = 2i \quad x = -2i}$$

Standard

B. $x^5 + 4x^3 = 5x^4 - 2x^3$

$$\begin{array}{r} -5x^4 + 2x^3 \\ \hline \end{array}$$

$$x^5 - 5x^4 + 6x^3 = 0$$

$$x^3(x^2 - 5x + 6) = 0$$

$$x^3(x-3)(x-2) = 0$$

$$\sqrt[3]{x^3} \quad x-3=0 \quad x-2=0$$

$$\boxed{x=0 \quad x=3 \quad x=2}$$

a.c

$$\begin{array}{r} 6 \\ -2 \times -3 \\ \hline 4 \\ -5 \\ 6 \end{array}$$

EX #2: Find the real or imaginary solutions for each polynomial equation.

A. $x^4 = 16$

$-16 \quad -16$

$x^4 - 16 = 0$

$(x^2)^2 - 4^2$

$(x^2 - 4)(x^2 + 4) = 0$

$\sqrt{x^2} = \sqrt{4}$

$\sqrt{x^2} = \sqrt{-4}$

$x = \pm 2$
 $x = \pm 2i$

B. $x^3 \pm 8x - 2x^2$

$-8x + 2x^2 \quad -8x - 2x^2$

$x^3 + 2x^2 - 8x = 0$

$x(x^2 + 2x - 8) = 0$

$\begin{array}{c} a \cdot c \\ -8 \\ 4 \quad -2 \\ + \\ 2 \\ b \end{array}$

$x(x+4)(x-2) = 0$

$x = 0 \quad x = -4 \quad x = 2$

C. $x(x^2 + 8) = 8(x + 1)$