

1

$$x + y = 75$$

The equation above relates the number of minutes,  $x$ , Maria spends running each day and the number of minutes,  $y$ , she spends biking each day. In the equation, what does the number 75 represent?

- A) The number of minutes spent running each day
- B) The number of minutes spent biking each day
- ☒ C) The total number of minutes spent running and biking each day
- D) The number of minutes spent biking for each minute spent running

2

Which of the following is equivalent to  $3(x + 5) - 6$ ?

- A)  $3x - 3$
- B)  $3x - 1$
- ☒ C)  $3x + 9$
- D)  $15x - 6$

$$3x + 15 - 6$$

$$3x + 9$$

3

$$x = y - 3$$

$$\frac{x}{2} + 2y = 6$$

Which ordered pair  $(x, y)$  satisfies the system of equations shown above?

- A)  $(-3, 0)$
- ☒ B)  $(0, 3)$
- C)  $(6, -3)$
- D)  $(36, -6)$

$$3(x - y = -3)$$

$$\frac{1}{2}x + 2y = 6$$


---


$$2x - 2y = -6$$

$$+ \frac{1}{2}x + 2y = 6$$


---


$$2.5x = 0$$

$$x = 0$$

4

Which of the following complex numbers is equal to  $(5 + 12i) - (9i^2 - 6i)$ , for  $i = \sqrt{-1}$ ?

- A)  $-14 - 18i$
- B)  $-4 - 6i$
- C)  $4 + 6i$
- ☒ D)  $14 + 18i$

$$i^2 = -1$$

$$5 + 12i - 9(-1) + 6i$$

$$5 + 12i + 9 + 6i$$

$$18i + 14$$

5

If  $f(x) = \frac{x^2 - 6x + 3}{x - 1}$ , what is  $f(-1)$ ?

- A) -5  
B) -2  
C) 2  
D) 5

$$f(-1) = \frac{(-1)^2 - 6(-1) + 3}{-1 - 1} = \frac{1 + 6 + 3}{-2} = \frac{10}{-2} = -5$$

7

$$x^2 + 6x + 4$$

Which of the following is equivalent to the expression above?

- A)  $(x+3)^2 + 5$   
B)  $(x+3)^2 - 5$   
C)  $(x-3)^2 + 5$   
D)  $(x-3)^2 - 5$

$$x^2 + 6x + 9 - 5$$

$$x^2 + 6x + 9$$

6

A company that makes wildlife videos purchases camera equipment for \$32,400. The equipment depreciates in value at a constant rate for 12 years, after which it is considered to have no monetary value. How much is the camera equipment worth 4 years after it is purchased?

- A) \$10,800  
B) \$16,200  
C) \$21,600  
D) \$29,700

$$32400 - 12x = 0 \quad \leftarrow \text{time}$$

$$32400 = 12x$$

$$x = 2700 \quad \leftarrow \$ \text{ every year}$$

$$32400 - 2700(4) = 21600$$

8

Ken is working this summer as part of a crew on a farm. He earned \$8 per hour for the first 10 hours he worked this week. Because of his performance, his crew leader raised his salary to \$10 per hour for the rest of the week. Ken saves 90% of his earnings from each week. What is the least number of hours he must work the rest of the week to save at least \$270 for the week?

- A) 38  
B) 33  
C) 22  
D) 16

$$0.9(10x + 80) \geq 270$$

$$9x + 72 \geq 270$$

$$9x \geq 198$$

$$x \geq 22$$

1. Look around your school or house. What are some structures you see that use triangles?

Roof of your house

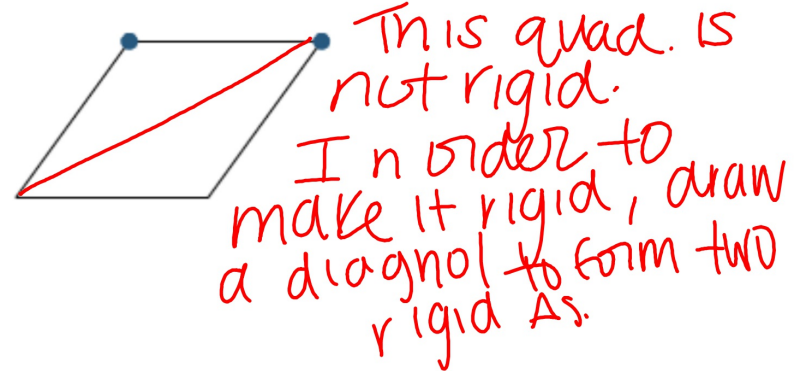
2. Why is the triangle the shape of choice for structures such as bridges and the Eiffel Tower?

Rigid  
Triangles are the only  
polygons that are  
rigid.

3. What does it mean for a triangle to be rigid?

A figure is rigid if it  
cannot be distorted  
under stress.

4. Is the figure below a rigid figure? If not, what can you do to make it rigid?



5. Do you remember what makes each of the following triangles special?

a. Isosceles triangle

2  $\cong$  sides 

b. Equilateral triangle

all sides  $\cong$  

c. Scalene triangle

none of sides  $\cong$ .

d. Right triangle

one angle that  $= 90^\circ$

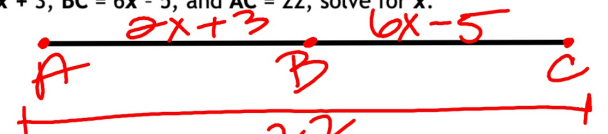
e. Acute triangle

all angles measure  $< 90^\circ$

f. Obtuse triangle

one angle is  $> 90^\circ$

6. **REVIEW** Suppose points A, B, and C are collinear, where B is between A and C. If  $AB = 2x + 3$ ,  $BC = 6x - 5$ , and  $AC = 22$ , solve for x.



$$AB + BC = AC$$

$$2x + 3 + 6x - 5 = 22$$

$$8x - 2 = 22$$

$$8x = 24$$

$$x = 3$$

### Properties of a triangle

Student Activity Sheet 2; Exploring "A triangle, or not?"

Page 1 of 2

1. Write a good definition of a triangle

a figure (or a polygon)  
closed  
w/ three sides

2. It is possible to create a triangle with side lengths 6 units, 6 units, and 2 units. Decide whether the other combinations of side lengths in the table create triangles or not. Mark your answers in the table.

| Side lengths<br>(in units) | Forms a triangle? |    |
|----------------------------|-------------------|----|
|                            | YES               | NO |
| 6, 6, 2                    | X                 |    |
| 4, 6, 8                    |                   |    |
| 8, 9, 2                    |                   |    |
| 4, 2, 8                    |                   |    |
| 6, 8, 9                    |                   |    |
| 6, 4, 4                    |                   |    |
| 2, 4, 6                    |                   |    |
| 4, 4, 9                    |                   |    |
| 2, 8, 8                    |                   |    |

3. Explain why some of the side length combinations in the table above do not form triangles.

If the sum of two sides of a figure is less than the third side, then there is no way the two shorter sides can meet to form a  $\Delta$ .

4. Write a conjecture about the relationship among the lengths of the sides of a triangle. This conjecture can be proven, so we will call this the Triangle Inequality Theorem. You will prove this conjecture in a later topic.

The sum of the lengths of any two sides of a  $\Delta$  is greater than the length of the third side

$$\begin{array}{l} 2 \quad 4 \quad 6 \\ 6 > 2 \\ 4 + 6 > 2 \end{array}$$

$$\begin{array}{l} 4 + 2 \neq 6 \\ A + B > C \\ B + C > A \\ A + C > B \end{array} \left. \begin{array}{l} \\ \\ \\ \end{array} \right\} \begin{array}{l} \text{must} \\ \text{be} \\ \text{satis-} \\ \text{fied} \end{array}$$

5. **REINFORCE** The lengths of two sides of a triangle are 7 cm and 10 cm. What are the upper and lower bounds on the third side of the triangle?

$$\begin{array}{l} S + 7 > 10 \\ S > 3 \\ 7 + 10 > S \\ 17 > S \\ \cancel{10 + 7 > S} \end{array} \quad \begin{array}{l} S = \text{third} \\ \text{side} \\ \underline{3 < S < 17} \end{array}$$

6. **REINFORCE**  $\overline{MO}$  is twice as long as  $\overline{MN}$ .  $NO = 36$  cm. Find  $MO$  and  $MN$ . Can you solve this problem? If so, give the solution. If not, explain why not.

We don't know  
If  $\angle M$  is b/w  $N$  &  $O$

7. **REINFORCE**  $\overline{MO}$  is twice as long as  $\overline{MN}$ .  $\overline{NO} = 36$  cm. What lengths must  $\overline{NM}$  be between in order for  $\triangle MNO$  to be formed?

$$\begin{aligned} 12 < \overline{NM} < 36 \\ \uparrow \\ x & \quad \overline{NM} = \overline{NM} \\ & \quad \overline{NM} + \overline{MO} > \overline{NO} \\ & \quad x + 2x > 36 \\ & \quad 3x > 36 \\ & \quad x > 12 \end{aligned}$$

## Hwk #24 - Classifying Triangles Worksheet