Reasoning in Algebra

*Be able to identify the steps in a proof using the Properties of Equality.

*Be able to identify properties of equality or congruence if given a statement.

*Be able to complete missing steps using the properties of equality or congruence.

Name each property being used.

1.
$$\overline{AB} \cong \overline{AB}$$

2. If x = 2 and x = y, then y = 2.

3. If x = 3 and 2x + 7 = 4y, then 2(3) + 7 = 4y.

4. If $\angle A \cong \angle B$, then $\angle B \cong \angle A$

5. Which of the following is an example of the Reflexive Property of Equality?

O If
$$x = -2$$
, then $x + 4 = -2 + 4$.

$$0x - 2 = x - 2$$

O If
$$y = x + 4$$
, then $x + 4 = y$.

O If
$$x - 2 = y$$
 and $y = 4$, then $x - 2 = 4$.

6. Fill in the missing information in the proof below.

Given:
$$AC = 36$$

$$3x 2x + 1$$

$$A B C$$

Statements

1.
$$AB + BC = AC$$

3.
$$5x + 1 = 36$$

Justifications

1.

2. Substitution

3. _____

4. Subtraction Property of Equality

5.

Use the given property to complete each statement.

7. Addition Property of Equality If x = 5, then x + 3 =_____

8. Division Property of Equality If
$$2(AX) = 4(BY)$$
, then $AX =$

9. Distributive Property

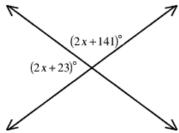
$$2(4x + 5) =$$

10. Transitive Property of Congruence If
$$\angle B \cong \angle T$$
 and $\angle B \cong \angle Y$, then ______

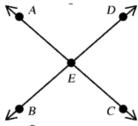
Proving Angles Congruent

*Be able to use the theorems in this section to find missing angle measures in diagrams.

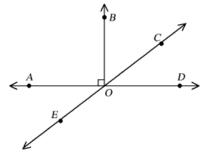
1. Find the value of x.



- 2. Supplementary angles are two angles whose measures have sum _____. Complementary angles are two angles whose measures have sum _____.
 - O 90; 180
 - C 180; 90
 - O 90; 45
 - C 180; 360
- 3. In the figure below, $m\angle AED = 97^{\circ}$. Which statement is false?

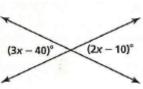


- \bigcirc $m \angle AEB = 83$
- \bigcirc m∠BEC = 97
- $\ddot{\Box}$ $\angle AEB$ and $m\angle DEC$ are congruent angles.
- \circ $\angle BEC$ and $m \angle CED$ are vertical angles.
- 4. Name an angle complementary to $\angle COD$.

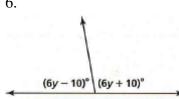


In questions 5 - 7 below, find the values of the variables.

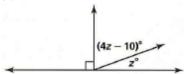
5.



6.

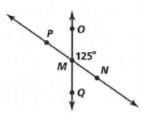


7.

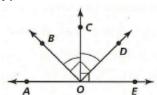


Write three conclusions that can be drawn from each diagram.

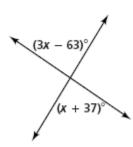
8.

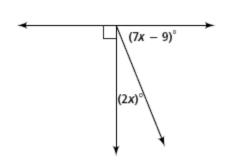


9.



For 1 and 2, find the value of x.





 $3.\,$ Fill in the missing information for the algebraic proof below.

Statements

Justifications

- 1) 0.5(4x-14)+3=6
- 1) Given

2) 2x - 7 + 3 = 6

- 2) _____
- 3) _____
- 3) Simplify like terms

4) 2x = 10

4)

5) _____

5) Division Property of Equality

4. Write a statement below that uses the Reflexive Property of Congruence.

For questions 5-7, use the given property to complete each missing statement.

5. Addition Property of Equality

If 4x - 3 = 10, then _____

6. Transitive Property of Congruence

If $\angle TQM \cong \angle X$ and $\angle X \cong \angle LTS$, then _____

7. Multiplication Property of Equality

If $\frac{1}{2}x = 6$, then _____