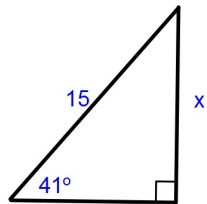
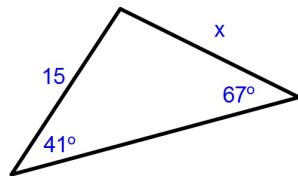


## SOHCAHTOA

works only works  
for right triangles.



What if it's not  
a right triangle?

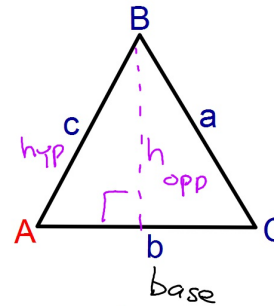


You must find another tool to use!

Write an expression for the  
area if:

you know angle **A**:

$$\text{Area} = \frac{1}{2}(\text{base})(\text{height})$$

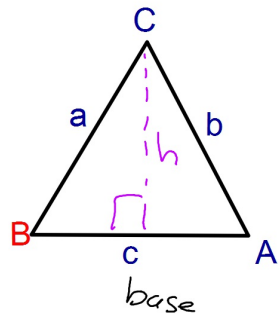


$$\sin A = \frac{h}{c}$$

Given the same triangle write  
an expression for the area if:

you know angle **B**:

$$\text{Area} = \frac{1}{2}(\text{base})(\text{height})$$

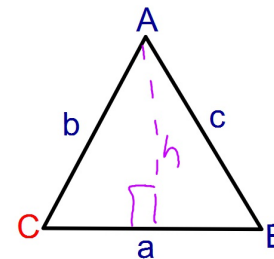


$$\sin B = \frac{h}{a}$$

Given the same triangle write  
an expression for the area if:

you know angle **C**:

$$\text{Area} = \frac{1}{2}(\text{base})(\text{height})$$



$$\sin C = \frac{h}{b}$$

All three areas should be the same.

$$A = \frac{1}{2}bc\sin A = \frac{1}{2}ac\sin B = \frac{1}{2}ab\sin C$$

Simplify: divide by  $\frac{1}{2}abc$

$$\frac{\frac{1}{2}bc\sin A}{\frac{1}{2}abc} = \frac{\frac{1}{2}ac\sin B}{\frac{1}{2}abc} = \frac{\frac{1}{2}ab\sin C}{\frac{1}{2}abc}$$

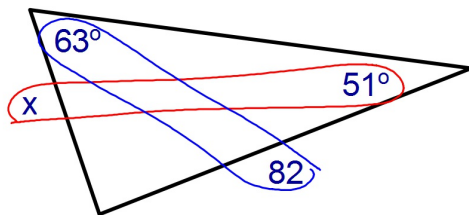
$$\frac{\sin A}{a} = \frac{\sin B}{b} = \frac{\sin C}{c}$$

## The Law of Sines:

$$\frac{\sin A}{a} = \frac{\sin B}{b} = \frac{\sin C}{c}$$

You will only be using two of the three ratios at any given moment.  
Therefore, Law of the Sines turns out to be a proportion.

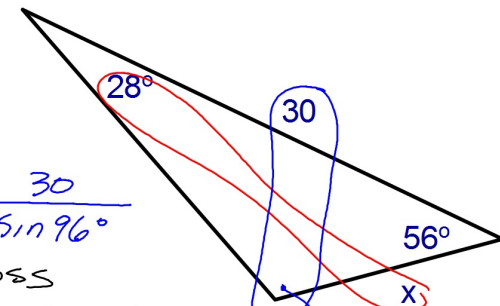
Find the value of x in this triangle to the nearest tenth.



$$\frac{\sin 51^\circ}{x} = \frac{\sin 63^\circ}{82}$$

Cross multiply  
to get  $x = 71.5$

Find the value of x in this triangle to the nearest tenth.



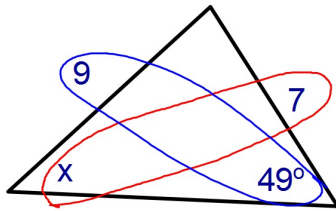
$$\frac{x}{\sin 28^\circ} = \frac{30}{\sin 96^\circ}$$

Now cross  
multiply to get

$$x = 14.2$$

You need this angle  
to use Law of Sines.  
 $180 - 56 - 28 = 96^\circ$

Find the value of x in this triangle to the nearest tenth.



$$\frac{7}{\sin x} = \frac{9}{\sin 49^\circ}$$

since you are trying to find an angle you'll eventually have to use Inverse Sine.

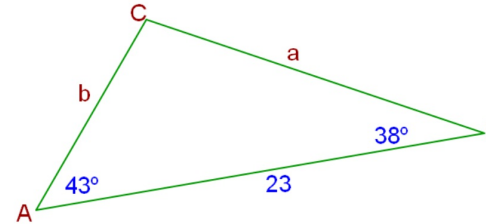
First solve for Sinx then do the inverse sine.

$$\sin x = \frac{7 \cdot \sin 49^\circ}{9}$$

$$x = \sin^{-1}(\quad)$$

$$x = 35.9^\circ$$

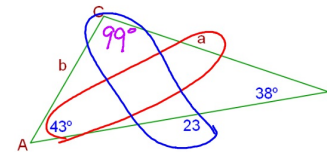
Use the Law of Sines to find the lengths of the missing sides in this triangle. Round to a tenth.



a =

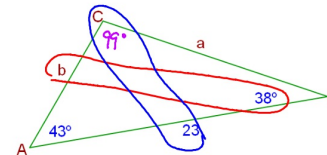
b =

You first need to find  $\angle C$ .  $\angle C = 180 - 38 - 43 = 99^\circ$



You can choose to find either missing side first. Let's find side a.

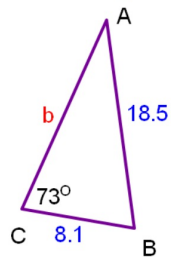
$$\frac{a}{\sin 43^\circ} = \frac{23}{\sin 99^\circ} \quad a = 15.9$$



Now find side b:

$$\frac{b}{\sin 38^\circ} = \frac{23}{\sin 99^\circ} \quad b = 14.3$$

Use the Law of Sines to find remaining sides and angles in this triangle. Round to a tenth.



with the given information you can only find angle A first.

$$\frac{\sin 73^\circ}{18.5} = \frac{\sin A}{8.1}$$

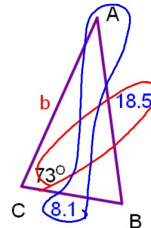
$$\sin A = \frac{8.1 \sin 73^\circ}{18.5}$$

$$\angle A = \sin^{-1}(\quad)$$

$$\angle A = 24.8^\circ$$

Now find  $\angle B$ :  $180 - 73 - 24.8$

$$\angle B = 82.2^\circ$$

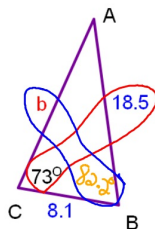


Finally, find side b:

$$\frac{\sin 73^\circ}{18.5} = \frac{\sin 82.2^\circ}{b}$$

Cross multiply:

$$b = 19.2$$



What is the least amount of information about a triangle that you need in order to use the Law of Sines?

$$\frac{\sin A}{a} = \frac{\sin B}{b}$$

To find an angle you need to know:

One other angle and the two sides opposite those angles

**SSA**

To find a side you need to know:

another side and the two angles opposite those sides.

**AAS**

You can now finish Hwk #26  
Sec 14-4

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Problems: 1, 3-5, 11, 12, 17, 18, 28