

Bellwork Alg 2 Monday, May 13, 2019

Simplify each trigonometric expression into a single trigonometric function or constant.

1. $\frac{\sec x - \cos x}{\sec x}$

2. $\tan \theta \sin \theta + \frac{1}{\sec \theta}$

3. $\frac{\sin^2 \theta (\tan \theta + \cot \theta)}{\sec \theta}$

Simplify each trigonometric expression into a single trigonometric function or constant.

1. $\frac{\sec x - \cos x}{\sec x}$

$$= \frac{\left(\frac{1}{\cos} - \cos\right)}{\frac{1}{\cos}} \cdot \frac{\cos}{\cos}$$

$$= \frac{1 - \cos^2}{1}$$

$$= \boxed{\sin^2 x}$$

2. $\tan \theta \sin \theta + \frac{1}{\sec \theta}$

$$= \frac{\sin}{\cos} \cdot \sin + \frac{1}{\frac{1}{\cos}}$$

$$= \frac{\sin^2}{\cos} + \cos \cdot \frac{\cos}{\cos}$$

$$= \frac{\sin^2}{\cos} + \frac{\cos^2}{\cos}$$

$$= \frac{\sin^2 + \cos^2}{\cos} = \frac{1}{\cos}$$

$$= \boxed{\sec \theta}$$

3. $\frac{\sin^2 \theta (\tan \theta + \cot \theta)}{\sec \theta}$

$$= \frac{\sin^2 \left(\frac{\sin}{\cos} + \frac{\cos}{\sin} \right)}{\frac{1}{\cos}} \cdot \frac{\cos}{\cos}$$

$$= \sin^2 \cos \left(\frac{\sin}{\cos} + \frac{\cos}{\sin} \right)$$

$$= \sin^3 + \sin \cos^2$$

$$= \sin (\sin^2 + \cos^2)$$

$$= \sin (1)$$

$$= \boxed{\sin \theta}$$