

Y-Intercepts: Replace x with zero.

All that will remain are the two constants.

therefore, y-intercepts of rational functions are ratios of the constants.

A graph can have, at most, one y-intercept.

X-Intercepts: Replace y with zero.

This means you are setting the ratio equal to zero and solving for x.

The only way a ratio equals zero is if the NUMERATOR equals zero.

therefore, x-intercepts of rational functions are zeros of the numerator.

In general, the x-intercepts of a Rational Function are the:

Zeros of the numerator (as long as they don't match zeros of the denominator, otherwise, they are holes)

A graph can have multiple x-intercepts.

find the x and y-intercepts of each function, if any.

$$\begin{aligned} 1. \quad y &= \frac{x^2 + 6x + 8}{2x^3 - 18x} \\ &= \frac{(x+4)(x+2)}{2x(x^2-9)} \\ &= \frac{(x+4)(x+2)}{2x(x+3)(x-3)} \end{aligned}$$

y-int:

$$y = \frac{8}{0}$$

NO y-int

x-int:

$$x = -4, -2$$

Neither of these are zeros of the denominator so they are not holes.

$$2. \quad y = \frac{4x^2 + 12}{3x^2 - x - 24}$$

y-int:  $y = \frac{12}{-24} = -\frac{1}{2}$

x-int: the numerator will never = zero, therefore there are

NO x-int

Find the x-intercepts, if any.

$$\frac{x^2 - 4}{x^2 - 7x - 18} = \frac{(x+2)(x-2)}{(x+2)(x-9)}$$

Handwritten work shows the denominator factored as  $(x+2)(x-9)$  using the numbers -9 and +2 which multiply to -18 and add to -7.

X-int:  $x = 2$

( $x = -2$  is a hole not an x-int)

You can now finish:

Hwk #6.

Practice Sheet: Horizontal Asymptotes and x & y-intercepts

Due tomorrow

Find all VA, HA, x-int, and y-int.

$$y = \frac{x^0 + 1}{x^0 + x - 6} = \frac{x+1}{(x+3)(x-2)}$$

HA:  $y = 0$  the degree of the denominator is bigger than the degree of the numerator.

y-int:  $-\frac{1}{6}$

VA:  $x = -3, 2$

X-int:  $x = -1$

$$y = \frac{x+1}{x^2+x-6}$$

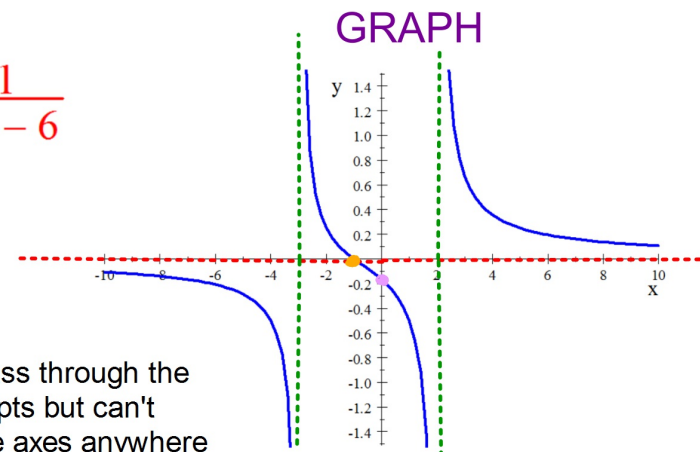
HA:  $y = 0$

VA:  $x = -3, 2$

x-int:  $x = -1$

y-int:  $y = -1/6$

A graph MUST pass through the axes at its intercepts but can't touch or cross the axes anywhere else.



Find all VA, HA, x-int, and y-int.

$$y = \frac{3x^2 - 12}{x^2 - x - 12} = \frac{3(x^2 - 4)}{(x-4)(x+3)} = \frac{3(x+2)(x-2)}{(x-4)(x+3)}$$

HA:  $y = \frac{3}{1} = 3$

y-int:  $y = \frac{-12}{-12} = 1$

VA:  $x = 4, -3$

x-int:  $x = \pm 2$

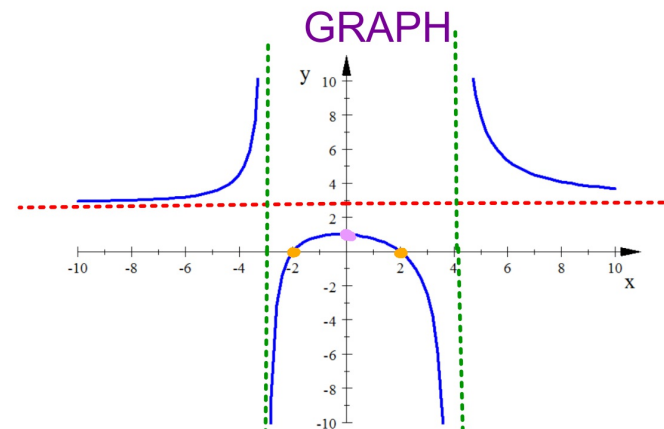
$$y = \frac{3x^2 - 12}{x^2 - x - 12}$$

HA:  $y = 3$

VA:  $x = -3, 4$

x-int:  $x = \pm 2$

y-int:  $y = 1$



#### Sec 9-4

##### Rational Expressions:

The ratio of two polynomials.

Polynomials: Have whole number exponents and real coefficients.

A rational expression is in its simplest form when:

The denominator and numerator have no common factors.

This is NOT a Rational Function, why?

$$\frac{\sqrt{x^2 - 5x + 3}}{2x - 9}$$

The numerator isn't a polynomial!

A radical represents a fractional exponent.

Sec 9-4  
Simplifying Rational Expressions

- Factor all numerators and denominators
- Cancel factors common to the numerator and denominator
- Restrictions are any values that make the denominator zero at any point (beginning to end)

Simplify. State restrictions on the variable.

1.  $\frac{9x^2y^8}{12x^5y^3}$

$$= \frac{3y^5}{4x^3}$$

$y, x \neq 0$

2.  $\frac{6x^4 - 150x^2}{4x^3 - 40x^2 + 100x}$

$$= \frac{6x^2(x^2 - 25)}{4x(x^2 - 10x + 25)}$$

$\begin{array}{r} +25 \\ -5 \quad -5 \\ \hline -10 \end{array}$

$$= \frac{6x^2(x+5)(x-5)}{4x(x-5)(x-5)}$$

$$= \frac{3x(x+5)}{2(x-5)}$$

$x \neq 0, 5$