

1. You start a business that manufactures and sells space heaters. The building and machinery cost \$550,000. Each month you pay \$2700 for utilities, insurance, and taxes. Your payroll each month is \$10,500. You sell your space heaters for \$120 each and your monthly sales average 350 space heaters.

Find the break-even point.

$$\text{Income} = \text{Exp.}$$

$$(120) \cdot 350m = 550,000 + 2700m + 10,500m$$

$$42,000m = 550,000 + 13,200m$$

$$28,800m = 550,000$$

$$m = 19.097$$

20 months

2. Your boat can travel 12mph in calm water. Today you took your boat to a river that has a current of 4 mph.

a) How long would it take you to travel 9 miles upstream?

$$d = r \cdot t$$

$$9 = 8 \cdot t \quad t = 1.125 \text{ hrs}$$

b) How long would it take you to return?

$$9 = 16 \cdot t$$

$$t = 0.5625 \text{ hrs.}$$

3. Your plane can fly 180 mph with no wind. Today there is a 25 mph wind.

a) How far can you travel in 4 hours if you fly with a tailwind?

$$d = (205)(4) = 820 \text{ mi.}$$

b) How long would it take you to return?

$$820 = (155) \cdot t$$
$$t = 5.29 \text{ hrs.}$$

4.) On a canoe trip I paddled upstream (against the current) for 6 hours and traveled 15 miles. Later I paddled downstream (with the current) for 4 hours and traveled 34 miles. Write and solve a system of equations to find the speed of the current and the speed that I can paddle in still water.

c = current
 b = boat

Downstream EQ:

$$34 = (b + c) \cdot 4$$

Upstream EQ:

$$15 = (b - c) \cdot 6$$

$$\begin{array}{r} 8.5 = b + c \\ 2.5 = b - c \end{array}$$

$$11 = 2b \quad b = 5.5 \text{ mph}$$
$$c = 3 \text{ mph}$$

5.) It takes you 3 hours in your canoe to travel 12.6 miles downstream. The return trip upstream takes you 7 hours. Write and solve a system of equations to find the speed of the canoe and the speed of the current.

Downstream EQ:

$$d = r \cdot t$$
$$12.6 = (b+c)3$$

Upstream EQ:

$$12.6 = (b-c)7$$

$$4.2 = b + c$$

$$1.8 = b - c$$

$$2b = 6$$

$$b = 3 \text{ mph}$$

$$c = 1.2$$

You mix together two acid solutions to get a final solution that is 9% acid by volume. If there ends up being 15 liters of this new solution how many liters of pure acid do you have?

$$15 \times 0.09$$

$$= 1.35 \text{ liters}$$

There is a flask with unknown amount of solution. This solution is 6% acid by volume. Write an expression that gives the amount of pure acid in the flask.

$$0.06x \quad x = \text{amt sol.}$$

You mix an unknown # of liters of a 9% acid solution with an unknown # of liters of a 15% acid solution. You end up with a total of 20 liters of solution.

$$x = 9\% \text{ sol.} \quad y = 15\% \text{ sol.}$$

Write an equation which represents the above information.

$$x + y = 20$$

You want to create 8 gallons of an acid solution that is 12% acid by volume. All you have on the shelf are solutions that are 15% acid and 10% acid by volume.

How many gallons of each should you mix together?

$x = 3.2 \text{ gal}$ $y = 4.8 \text{ gal}$
 $x = \text{gallons of 15\% solution}$ $y = \text{gallons of 10\% solution}$

Gallons of Solution

$$x + y = 8$$

Gallons of Pure Acid

$$0.15x + .10y = .12 \cdot 8$$

$$\begin{aligned} -0.05x &= -.16 \\ x &= 3.2 \end{aligned}$$

$$\begin{aligned} (x + y = 8) \cdot 10 \\ .15x + .10y &= .96 \\ -.10x + .10y &= .80 \\ - .15x + .10y &= .96 \end{aligned}$$

1.) Sally's favorite color is pink. Her favorite shade of pink is the paint that is 33% red. She wants to mix up 5 gallons of her favorite of pink but all that is available is paint that is 17% red and another is 37% red. How many gallons of each these paints should be mixed to get what she wants (33 % red)?

Gal of Paint

$$x + y = 5$$

Variables: $x = \text{Gal of 17\% red paint}$

$= 1 \text{ gal}$
 $= 4 \text{ gal}$

Amount of Red

$$0.17x + .37y = 1.65$$

$$\begin{aligned} .17x + .37(5 - x) &= 1.65 \\ .17x + 1.85 - .37x &= 1.65 \\ -.2x + 1.85 &= 1.65 \\ -.2x &= -.2 \\ x &= 1 \end{aligned}$$

2.) You are going to mix together two kinds of window cleaner. One of the cleaners has 2% ammonia and the other has 5% ammonia.

How many ounces of each acid solution should you use so that you will end up with 24 ounces of a mixture that is 3% ammonia?

x = ounces of 2% solution

y = ounces of 5% ammonia

Ounces of Solution:

Ounces of Pure Ammonia:

HW #6 -- due tomorrow

Section 7.4 (use the sheet I gave you)

#1-4 on the sheet; 5, 6, 15 from textbook.

IXL #4 - T.1 & T.3 due Friday, February 15th!